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ECONOMIC EFFICIENCY
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***INTERNATIONAL TRADE AND
REGIONAL ECONOMICS***



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ABSTRACT

Banking Permits: Economic Efficiency and Distributional Effects*

Most analyses of the Kyoto flexibility mechanisms focus on the cost effectiveness of "where" flexibility (e.g. by showing that mitigation costs are lower in a global permit market than in regional markets or in permit markets confined to Annex 1 countries). Less attention has been devoted to "when" flexibility, i.e. to the benefits of allowing emission permit traders to bank their permits for future use. In the model presented in this paper, banking of carbon allowances in a global permit market is fully endogenised, i.e. agents may decide to bank permits by taking into account their present and future needs and the present and future decisions of all the other agents. It is therefore possible to identify under what conditions traders find it optimal to bank permits, when banking is socially optimal, and what are the implications for present and future permit prices. We can also explain why the equilibrium rate of growth of permit prices is likely to be larger than the equilibrium interest rate. Most importantly, this paper analyses the efficiency and distributional consequences of allowing markets to optimally allocate emission permits across regions and over time. The welfare and distributional effects of an optimal intertemporal emission trading scheme are assessed for different initial allocation rules. Finally, the impact of banking on carbon emissions, technological progress, and optimal investment decisions is quantified and the incentives that banking provides to accelerate technological innovation and diffusion are also discussed. Among the many results, we show that not only does banking reduce abatement costs, but it also increases the amount of GHG emissions abated in the short-term. It should therefore belong to all emission trading schemes under construction.

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1. Introduction

In a multi-period market for pollution rights, the possibility to transfer emission allowances to the future is referred to as banking of emission units. The early use of allowances issued for later periods is instead referred to as borrowing of emission units. A market of permits where both banking and borrowing of emission rights are allowed is characterised by full intertemporal flexibility. In this market, the so-called “when flexibility” is therefore added to the so-called “where flexibility” (achieved when different countries trade pollution rights). A fully flexible market is shown to be superior, in terms of efficiency, to a market in which the transfer of pollution rights is restricted, in either dimension (see, for instance, Leiby and Rubin, 2001). The importance of the “when flexibility” is also recognised by the Kyoto Protocol, which specifies that in the event that a Party has a surplus of carbon allowances at the end of the first commitment period, a portion of these credits may be carried-over to a subsequent commitment period after 2012.¹

Despite its relevance, banking is rarely considered in the empirical literature that quantifies the costs of mitigation policies. In a few cases, intertemporal flexibility is introduced, but the number of permits that are moved across time, and the future use of the extra-allowances, is exogenously determined by the modeller (Babiker et al., 2002; Manne and Richels, 2001; Springer, 2003; Carraro and Galeotti, 2004).

The theoretical literature on emission trading is instead rich in contributions on banking. These contributions generally show that a permit system with intertemporal flexibility increases welfare.² However, the assumptions commonly used in this literature are far from realistic and do not mimic the conditions under which a carbon market with intertemporal flexibility is reasonably expected to operate. For this reason, the objective of this paper is twofold: first, by introducing a fully endogenous market of carbon permits with banking in WITCH – the integrated assessment climate-economy hybrid model used in this paper – the welfare impacts of a fully intertemporal emission trading scheme can be estimated for various stabilisation targets and allocation rules. Second, the functioning of pollution permit markets with intertemporal flexibility can be analysed under some realistic assumptions that cannot be imposed in analytical models for tractability reasons.

¹ Cfr. Article 3(13) of the Kyoto Protocol.

² See Newell, Pizer and Zhang (2003), for a survey.

In their seminal paper, Cronshaw and Kruse (1996) set the standard framework along which research on banking of tradable permits has developed so far.³ They assume a (1) *constant number of* profit-maximising firms acting with perfect foresight in a competitive market for permits. Firms hurt the environment by releasing pollutants as a side effect of their production activity; however, they can also acquire inputs to mitigate emissions. Each firm receives an (2) *equal endowment* of permits for each period and it can buy or sell permits from other firms at a given price. Permits can be transferred across time by either *banking* them for future use or by (3) *borrowing* future allowances for use in the present. The authors show that, at the equilibrium, the present value permit prices must be non-increasing over time. Were discounted prices increasing, firms could (4) *buy from the market today to sell in future periods* thus increasing profits. This would lead to an unboundedly large demand for permits in the first period that would increase today's price. Hence, this cannot be an equilibrium. Thus, assuming that (5) *marginal abatement costs are constant over time*, banking takes place if and only if permit prices rise over time with the interest rate, i.e. discounted prices are constant.

This result is a very useful benchmark, but it relies on a set of assumptions which typically do not hold in the case of carbon markets induced or established by climate policy. Consider first that *marginal abatement costs can hardly be constant* over time. They are usually non-linear, with a time-trend determined by the alternating predominance of two opposite forces: on the one hand, diminishing returns tend to increase abatement costs over time; on the other hand, technological change works in the opposite direction and lowers abatement costs over time. Secondly, contrary to what assumed by Cronshaw and Kruse, climate policy is realistically expected to become increasingly tighter over time, with a time-varying, rather than constant, endowment of annual emission permits. Thirdly, and most importantly, it is highly unrealistic that any future regulation of carbon trading will allow “*speculative banking*”, i.e. the possibility of buying and banking emission permits for pure speculation on the future price of carbon. The Kyoto Protocol already explicitly forbids this type of banking, thus ruling out one of the pillars that support Cronshaw and Kruse's result. Finally, *borrowing* is also likely to be restricted since it has the potential to become a serious threat to the achievement of ambitious stabilisation targets and an incentive to defect from the climate agreement.

For these reasons, this paper proposes a more articulated set-up to analyse the role of banking in carbon markets. By using a computational model that delivers numerical solutions to the problem, we lose some transparency but we gain in realism. The analysis of the role of banking will be carried out by using WITCH, a regional model of the world economy in which 12 macro-regions have agreed on a

³ For further developments see Rubin (1996), Kling and Rubin (1997), Liski and Montero (2003). For an analysis with uncertainty see Godby *et al* (1997) and Innes (2003).

mitigation policy based on tradable emission rights. Regions differ in population, technology, income and energy demand. They can buy and sell permits in a competitive world carbon market, which sets marginal abatement costs equal worldwide. First, we study regions' optimal choices – i.e. their investments, R&D expenditures, net demand of permits, etc. – when there is no “when” flexibility. Then, we introduce “when” flexibility by allowing banking (but not borrowing) of carbon emissions. Speculative banking is not permitted either. Finally, we examine the effect of banking on the price of permits, on the time path of CO₂ abatement, on optimal investments, on the diffusion of technical change, etc..

This paper has a final additional objective. An important issue in the present debate on climate policy is the participation of developing countries in the cooperative effort to reduce global GHG emissions. These countries' decision crucially depends on the way in which the burden of controlling GHG emissions is shared among all countries and regions. The burden-sharing issue is equivalent to the allowance allocation issue if the policy adopted worldwide to control emissions is a global carbon market. Therefore, in this paper we analyse the efficiency and distributional implications of banking for three different allocations of carbon rights and investigate the role of banking under these distribution rules. By changing the distribution of permits among regions, we stress the effect of asymmetries among players in determining optimal banking decisions and the consequent price of permits over time.

From a policy perspective, we find that banking is a key instrument to comply with increasingly stringent emission reduction targets. Significant cost savings are possible by allowing greater intertemporal flexibility. A more original result is that banking provides relevant incentives to the early adoption of cleaner technologies, thus inducing a positive intertemporal spillover effect. This effect is stronger when the allocation rule is such that mostly OECD countries find it optimal to bank permits. The reason is that, in this case, banking also fosters a positive international technology spillover effect.

Our findings only partly confirm what is predicted by the analytical literature on the efficiency of “when” flexibility. Some new results – for example on the relationship between banking and technological change, on the implications of banking for the choice of the allocation rule, and also on the future equilibrium path of the permit price – are presented in this paper. In particular, contrary to what stated by Cronshaw and Kruse (1996), we find that an increasingly discounted price path for carbon rights is perfectly consistent with a well-defined carbon market. Moreover, discontinuities in the price path may arise, due to discontinuities in the evolution of marginal abatement costs and in the total number of emission allowances.

This paper is organised as follows. Section 2 illustrates the basic set-up of the WITCH model employed for our numerical analysis. Section 3 presents our results on banking of carbon rights and how (partial) “when flexibility” affects carbon emissions, the carbon market and the permit price. Section 4 discusses how banking changes optimal investment and R&D decisions, with consequent impacts on the speed of diffusion of technical change. Section 5 shows the effects of banking on stabilisation costs for three emission rights allocation rules. A concluding section summarises the most important findings of our analysis and outlines some policy implications.

2. The WITCH model and Climate Policy Scenarios

The WITCH – World Induced Technical Change Hybrid – model is a regional integrated assessment model that captures the channels of transmission of climate policy into the economic system and provides normative information on the optimal responses of world economies to climate damages and policy (for a complete list of model equations the reader is referred to the Appendix). It is a hybrid model because it combines features of both top-down and bottom-up modelling. The top-down component consists of an inter-temporal optimal growth model of the world economy. Within this framework, the energy input of the aggregate production function has been expanded to provide a bottom-up like description of the energy sector. World countries are grouped in 12 regions that strategically interact. A game-theoretic approach is used to describe these interactions. A climate module and a damage function provide the feedback on the economy of carbon dioxide emissions into the atmosphere.

WITCH top-down framework guarantees a coherent, fully intertemporal allocation of investments that have an impact on the level and cost of mitigation – i.e. R&D efforts, investments in energy technologies, fossil fuel expenditures. The regional specification of the model and the presence of strategic interaction among regions –through CO₂, exhaustible natural resources, carbon trading and technological spillovers– allows us to account for free-riding incentives. Investment strategies are optimised by taking into account both economic and environmental externalities. Optimal strategies belong to the open-loop Nash equilibrium of the dynamic game defined by the model.

By endogenously modelling fuel (oil, coal, natural gas, uranium) prices, as well as the cost of storing the CO₂ captured, the model can be used to evaluate the implications of mitigation policies on the energy system in all its components.⁴

In this paper, WITCH is used to analyse the cost of stabilising concentrations of CO₂ emissions in the atmosphere at 450ppmv by the end of the century (on this issue see also Bosetti *et al.*, 2007b). For simplicity and without affecting the main conclusions of the paper, we assume that all countries and regions agree to achieve the stabilisation objective by establishing a world carbon market that allows regions to exchange carbon rights. Banking of emission permits is allowed. “Speculative banking”, i.e. buying and banking permits at the same time, as well as “borrowing”, are not allowed.

In order to contribute to the burden-sharing debate, we compute stabilisation costs and their geographical distribution for three different allocation rules: *Equal Emissions per Capita*, *Contraction and Convergence* and *Sovereignty*. These are the most commonly studied allocation rules in the environmental economics literature. Independently of the allocation scheme and to gain in realism, we assume that until 2030 the whole abatement effort is undertaken by High Income (HI) regions alone, while Low Income countries are allocated their baseline emissions.⁵

In the *Equal Emissions per Capita* (EPC) scenario, allowances are distributed among regions in proportion to their population, so that each individual is endowed with the same CO₂ emission rights. This scenario turns out to be very stringent for industrialised countries, because of their modest share of world population, which will further decline over the next century.

The *Sovereignty* (SOV) allocation scheme has opposite implications: allowances are distributed to each region according to their present share of total emissions. Developing regions may be penalised because of rapid population and economic growth, while industrialised countries may reduce emissions at moderate costs.

The *Contraction and Convergence* allocation scheme (CC) stands between these two extremes. According to this widely discussed policy option, emission rights are first distributed according to the sovereignty rule in order not to constrain industrialised economies excessively; then, greater weight is

⁴ For a thorough description of the model see Bosetti *et al.* (2006, 2007a) and Bosetti, Massetti and Tavoni (2007).

⁵ High Income regions are: USA, OLDEURO, NEWEURO, KOSAU (South Korea, South Africa and Australia), CAJAZ (Canada, Japan, New Zealand). Low Income regions are: TE (Transition Economies), MENA (Middle East and North Africa), SSA (Sub-Saharan Africa), SASIA (South Asia), CHINA, EASIA (East Asia) and LACA (Latin America and the Caribbean). The aggregation of world regions is discussed in detail in Bosetti, Massetti and Tavoni (2007). For an analysis of the distributional impacts of climate policy see Bosetti *et al.* (2007b).

given to the equal emissions per capita allocation rule, eventually switching to a full application of this rule by the end of the century.

The reference scenarios are the stabilisation scenarios without “when” flexibility (one for each allocation rule) and, for the estimate of stabilisation costs, the benchmark is the WITCH Baseline scenario, in which no climate policy is imposed.

3. Banking, Emissions, and Carbon Prices

As said, in our scenarios all countries are committed to stabilise GHG concentrations at 450 ppm. The consequent optimal strategic choices in all countries and regions are described in this section. These choices include the optimal investment profile for all energy technologies, the optimal R&D investments, the net demand of permits and the number of permits to be banked in each period of time. Let us start by analysing this latter variable.

3.1 Banking of Carbon Rights

At the equilibrium, a considerable number of permits is banked in the first decades of the century under all allocation schemes (see Figure 1). The largest number of banked permits is recorded under the Sovereignty rule (20 GtC, or 4.2% of total emission allowances). Under the EPC and CC rules, banking is lower but non-negligible (14.63 GtC, or 3.1% of total emission allowances and 14.93 GtC, or 3.2% of total emission allowances, respectively).

The banking of permits during the first decades of the century, and the consequent forward transfer of allowances, generates lower emissions in the first decades of the century, as shown in Figure 2 and Table 1. However, since all banked emissions must be used by the end of the century, the situation is reversed from 2042-2052 onward, when CO₂ emissions in the atmosphere grow at a faster rate, with respect to the no-banking scenario. Both emission paths, with and without banking, ensure compliance with the stabilisation target.

However, banking smoothes the transition path to an economy with a lower carbon intensity by redistributing the effort from later to earlier periods. This causes an overall welfare improvement (Section 5 contains a detailed discussion of welfare effects). Banking is particularly useful for countries endowed with a surplus of allowances (with respect to their needs). As shown in Figure 1, banking is higher under the SOV scenario, which endows High Income countries with most of the allowances.

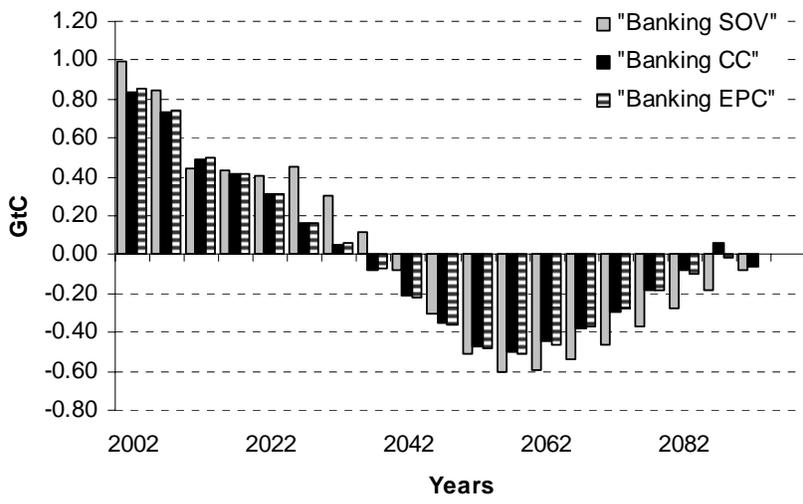


Figure 1. Savings of Carbon Credits (GtC, average per year).

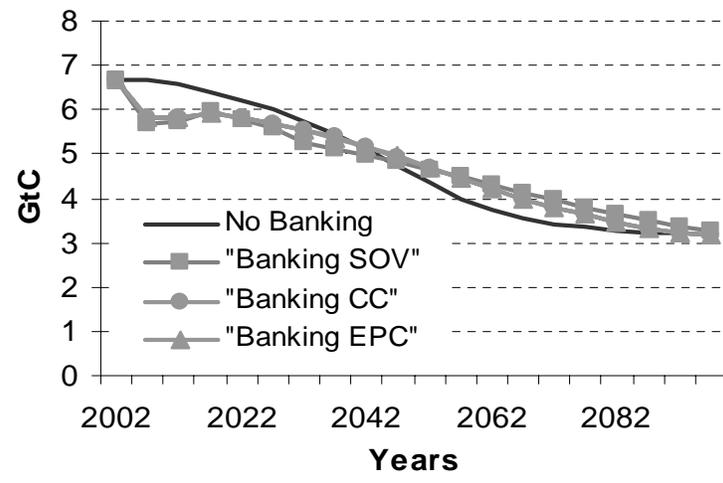


Figure 2. Industrial CO₂ emissions under different allocation schemes with and without banking

	SOV	CC	EPC
2002-2031	-9%	-8%	-8%
2032-2051	-4%	0%	0%
2052-2071	13%	11%	12%
2072-2097	2%	5%	5%
2002-2097	0%	0%	0%

Table 1. Variations of Industrial CO₂ emissions with Banking

3.2 Carbon Market

Banking also affects the size of the emission trading market. The number of emission rights traded over the whole century is rather constant (slightly lower with reductions of 1.4%, 3.0% and 1.5% for SOV, CC and EPC, respectively), but significant variations are recorded on shorter time periods, as shown in Figures 3 to 5. Banking reduces the market size in the first decades, while it increases the number of permits exchanged in later periods.

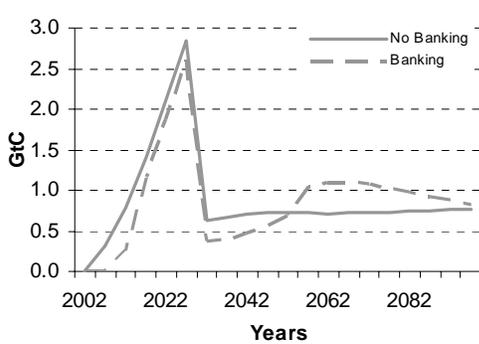


Figure 3. Trade of Carbon Credits – SOV

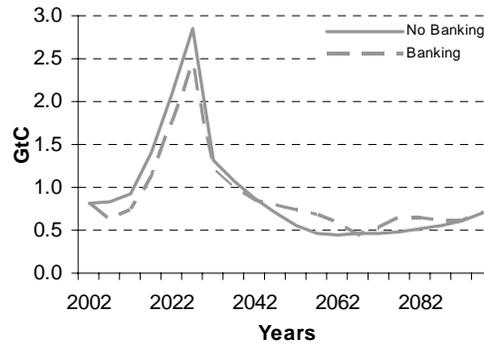


Figure 4. Trade of Carbon Credits – CC

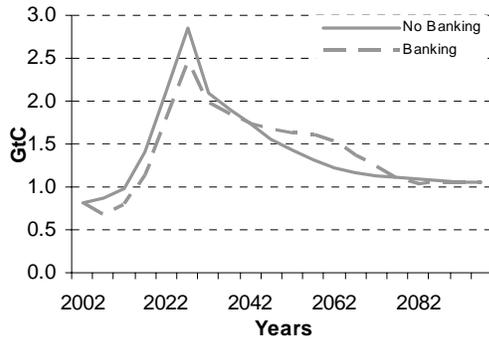


Figure 5. Trade of Carbon Credits – EPC

Table 2 shows the variations in the number of traded permits induced by banking. These changes are modest if we consider the whole century, but they significantly change the size of the market year by year. Banking is thus likely to have a strong effect on the market of emission credits. Let us therefore analyse the implications for the time profile of the permit price.

	SOV	CC	EPC
2002-2031	-26%	-19%	-18%
2032-2051	-52%	-3%	-1%
2052-2071	36%	28%	20%
2072-2097	23%	-20%	-20%
2002-2097	-1%	-3%	-1%

Table 2. Variations of Trade of Carbon Credits

3.3 Carbon Price

Without the possibility to transfer permits intertemporally, the quantity of carbon emitted in each period must be the same under all three allocation scenarios. The Coase Theorem states that the equilibrium amount of emissions (and the level of abatement) of each region is independent of the initial distribution of permits (Coase, 1960). Accordingly, the price of carbon does not depend on the distribution of permits. When intertemporal transfer of permits is allowed, the amount of emissions in

each time period is not independent of the distribution of permits. As a consequence, the price of carbon needs not to be the same under different initial allocations of permits. This is clearly visible from Figures 6 and 7. Different time paths for carbon prices will in turn imply different optimal investment strategies and different total stabilisation costs, as we will see in detail in the next sections.

As shown above, in the presence of “when” flexibility, emission rights are initially banked, supply drops and prices in the carbon market go up. Banking induces a strong increase in the carbon price in the first decades of the century, up to 94% higher, as shown in Figure 8. Subsequently, banked allowances are released, supply increases and the price goes down. Since carbon prices are very high in the second half of the century, the apparently small percentage variations imply massive drops in carbon prices. As a result, banking induces a smoother intertemporal path of the carbon price, as predicted by the analytical models. The rate of growth of carbon prices is strongly reduced, as Figure 9 portrays. However, it remains always higher than interest rates (capital markets are not integrated and thus each region has its own interest rate); this contradicts theory and requires some explanation.

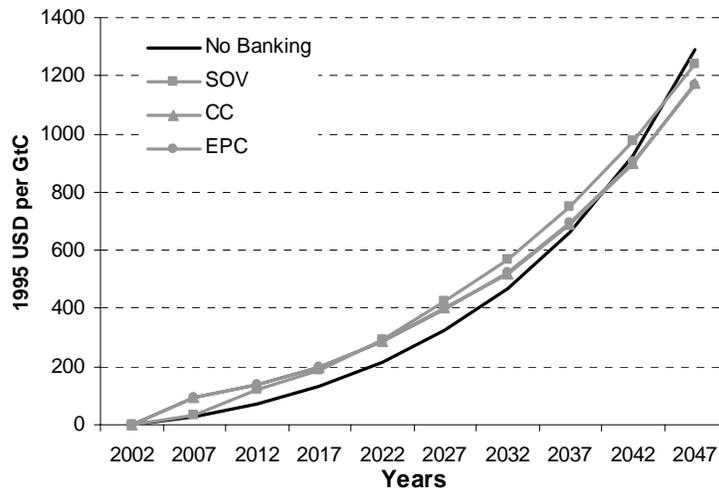


Figure 6. Price of Carbon for different Allocation Schemes (2002-2047).

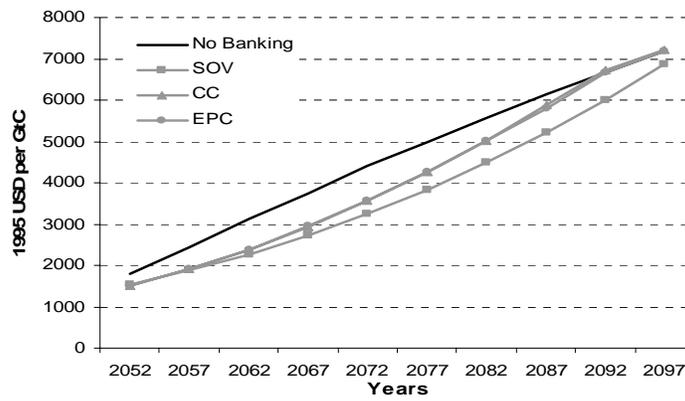


Figure 7. Price of Carbon for different Allocation Schemes. (2052-2097)

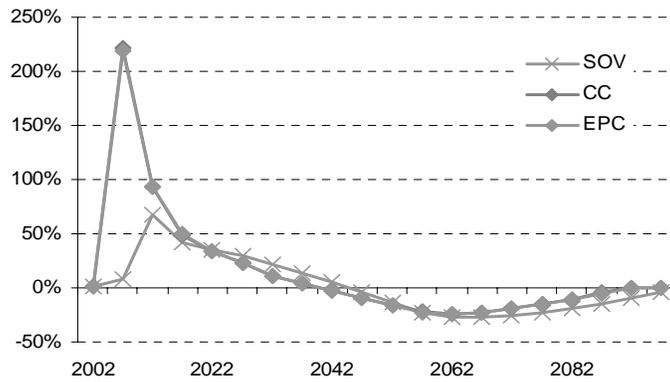


Figure 8. Change of Carbon Price, Banking wrt No Banking

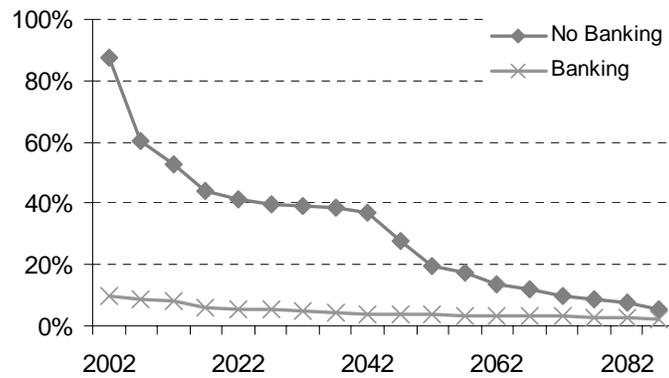


Figure 9. Rate of Growth of Carbon Price -SOV

It may be argued that the reason is the absence of borrowing and of speculative banking, or the strategic interactions among countries and regions. Therefore, a useful term of reference is the shadow price of carbon that emerges in the *cooperative* solution of the model when *full* intertemporal flexibility is allowed.⁶ Our results show that the carbon price still rises faster than the interest rate. The main reason therefore appears to be the presence of heterogeneous agents and of increasing marginal abatement costs when a strong policy to control a stock pollutant is implemented. Thus, our model does not predict a constant path of the discounted price of permits even when full intertemporal flexibility is allowed. The restrictions on borrowing and on speculative banking, introduced in the optimisation runs described in sections 3.1 and 3.2, are additional reasons for the discounted time path of permit prices to be higher than the interest rate.⁷

It appears that a “premium” in terms of rate of growth of permits over the interest rate is necessary for emissions to be banked. This finding emerges from all our optimisation runs and is synthesised in Figure 10 and 11, which show banked emissions together with the rate of growth of the carbon price (under the SOV scenario) and the rate of interest for MENA (Middle East and North Africa) and NEWEURO.⁸

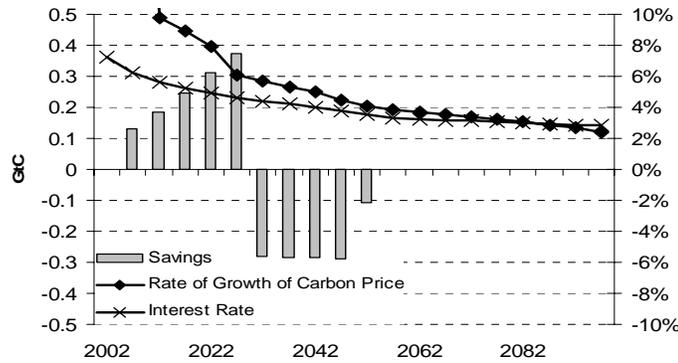


Figure 10. Carbon Market Data for Middle East and North Africa

⁶ In this kind of exercise, a global social planner maximises the sum of welfare of the twelve macro-regions. This rules out free-riding behaviours, which would instead strongly emerge in a non-cooperative solution of the model.

⁷ For all regions, in both cooperative and non-cooperative settings, the interest rate is always greater than the intertemporal discount rate. Per capita consumption is rising for all countries.

⁸ The rate of growth of carbon prices in the first two periods is not shown here because it exceeds the area of the graph (it is 102% in 2002-2006 and becomes 30% in 2007-2011). Rates of growth of carbon price are average per year. Compound interest has been used.

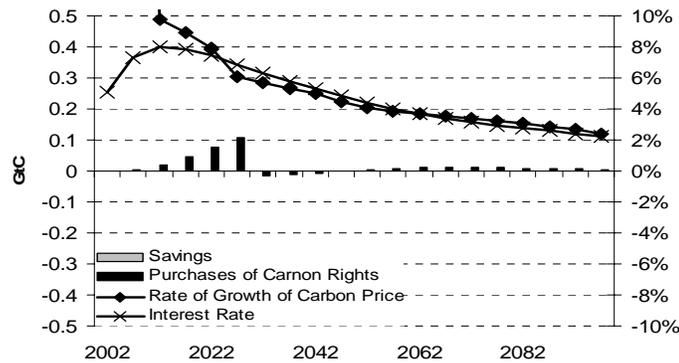


Figure 11. Carbon Market Data for New Europe

MENA uses banked emissions well before the interest rate becomes higher than the rate of carbon price growth. NEWEURO never banks its emission allowances, although during the first period the rate of growth of carbon price is much higher than its interest rate, and despite being a net buyer of carbon rights most of the time.

A second interesting feature of the permit market with banking is synthesised by Figure 12, which refers to the US, again under the SOV scenario. The growth rate of the carbon price is higher than the interest rate throughout the century. Why then are not all the saved allowances released at the same time in the last period?

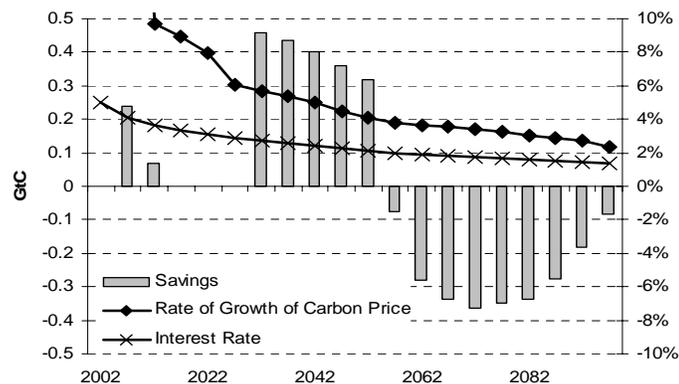


Figure 12. Carbon Market Data for the US

There are two explanations for a gradual release of saved permits. First, without an international financial market, it is impossible to finance earlier consumption so as to spread the extra revenues from permit sales over the last period of trade. In our macroeconomic, aggregated, context, there are only two ways to smooth consumption over time: through savings, embodied in capital goods, and through savings of emission allowances. Since both work only forward, allowing to postpone consumption but not to anticipate future positive income shocks, it is not possible for regions to sell at the most convenient moment and to anticipate consumption in earlier times. Second, an extremely high supply of permits in a single time period would make the carbon price sink;⁹ as can be inferred from Figure 1, the amount of permits banked is substantial and if concentrated only in a single time period it would outweigh demand by a factor of two, or more. Thus, contrary to what would be optimal for a single firm with open access to credit markets and with virtually no impact on prices, regions release banked emission permits gradually through time.

A closer look at banking decisions of single regions gives additional useful insights. Consider the behaviour of the US and of CHINA when permits are distributed according to the Sovereignty rule. Under this rule, the first region is predominantly a seller of permits, while the second is predominantly a buyer. Figure 13 shows the US optimal decisions in the permit market in the no-banking scenario. It pictures the emission constraint faced by the US, its actual emissions, purchases and sales of emission rights. Despite the effort to reduce GHG emissions with respect to the baseline, the steep decline of emissions imposed by the stringent climate policy can only be fulfilled by purchasing emission rights in the market. However, when the burden of reducing GHG emissions starts to fall also on Low Income countries, the peculiar distribution of permits implied by the Sovereignty principle rewards the early efforts of High Income countries and leaves space for net sales of permits. Figure 13 clearly shows the US effort to smooth the emission path throughout the century using the market instrument.

The picture changes significantly with the introduction of banking (Figure 14). Emissions are further smoothed over the century: between 2007-2017 there is a sudden drop of emissions, no purchases and instead saving of allowances. The uneven path of emissions during these two time periods is due to the “no-speculation” rule imposed to prevent regions from buying and saving permits at the same time. From 2017 till 2032 there are again purchases of emission rights, but in a smaller quantity compared to the no banking scenario. Starting from 2032 until 2052, emission rights in excess are saved for use in later periods, instead of being sold in the market. Indeed, the emission path remains lower than what

⁹ It is important to note that this happens in a perfectly competitive market. Even if regions behave as price takers, the solution algorithm for the market of permits (a Walrasian *tat nement* process) gives a price feedback signal that induces the choice of a new optimal supply (demand) of allowances, until market clearance.

recorded in the no-banking case until 2047. This implies that an extra effort is made to reduce emissions and the incentive to use them in later periods is stronger than the incentive to sell them in the market when banking is not allowed. From 2052 onward banked emissions are sold in the market and are used to cover extra emissions.

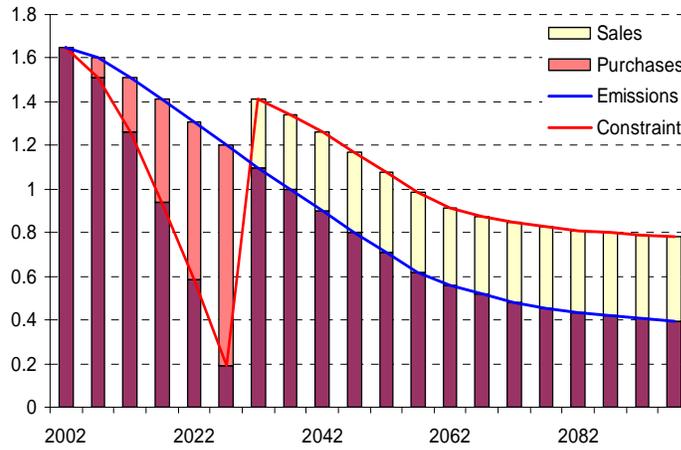


Figure 13. USA with no Banking.

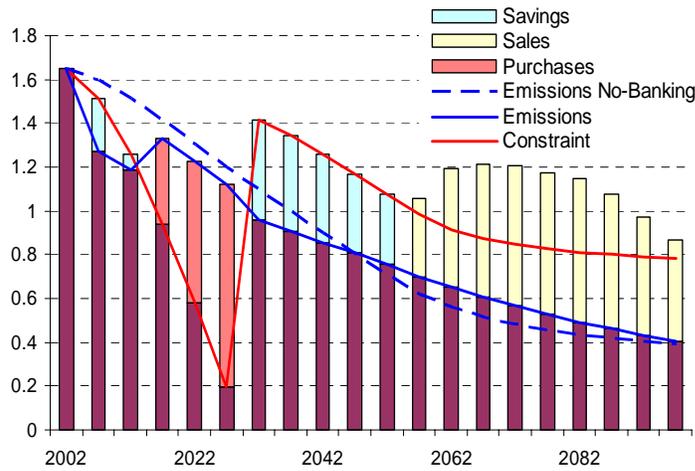


Figure 14. USA with Banking.

Also net buyers bank permits. Consider the case of CHINA. Until 2032 Low Income countries participate in the climate agreement without any constraint on emissions, but they are allowed to trade credits if they reduce emissions below their BAU level (in the form of CDM, for example). With banking, CHINA has the incentive to save some emission rights for later periods when the price of carbon increases. Figures 15 and 16 show optimal trading and saving decisions both with and without banking. The extra-sales between 2022-2031 are possible thanks to the emission rights stored beforehand. An extra amount of savings is released in 2032, when the emission target becomes binding for China as well: without banking China is a buyer of permits, with banking a seller. With banking, emissions are lower from 2002 until 2041, but are higher from 2042 onward, thanks to a lower carbon price.

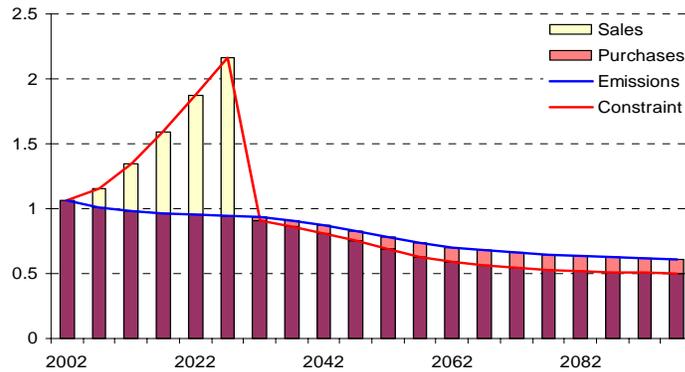


Figure 15. CHINA with no Banking.

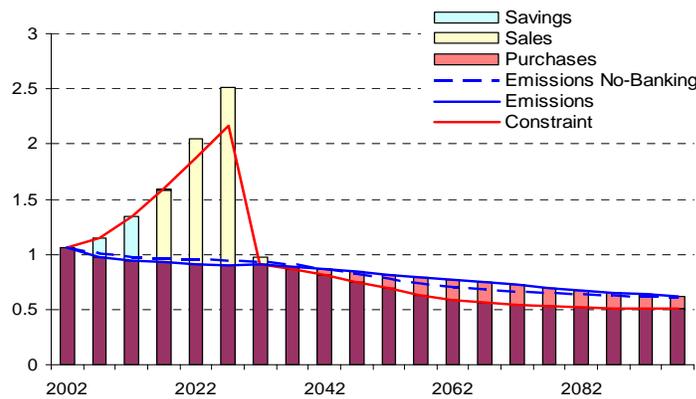


Figure 16. CHINA with Banking.

4. Investments in Energy R&D and in Renewables.

As shown in Section 3, when banking is allowed, prices are higher in the first part of the century and lower in the second part, with some differences that depend on the adopted allocation rule. How does the modified price path affect technological change? Does it increase energy efficiency and/or foster the adoption of low carbon energy sources? The answer is positive. Banking indeed stimulates earlier investments in energy R&D, in R&D to lower the cost of advanced biofuels and in Wind and Solar electricity generation technologies (W&S). As an example, let us analyse what happens to investments in Energy R&D (see Figure 17). With respect to the corresponding no-banking scenarios, R&D investments increase substantially in the first decades of the century and then decrease. The stocks of R&D capital follow the movement of R&D investments with a small time delay (see Figure 18). It is worth noting that the inertia is increased by the presence of intertemporal R&D spillovers in the R&D sector. Similar results also hold for investments in all carbon-free technologies that are modelled in WITCH.

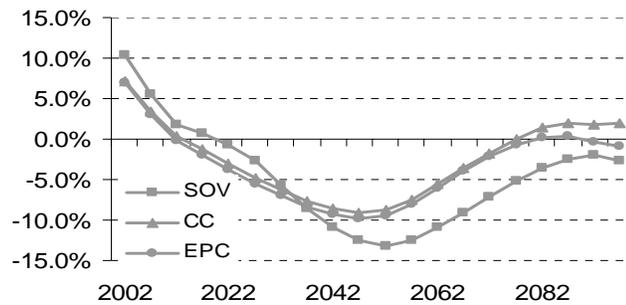


Figure 17. Change in Energy R&D Investments, Banking wrt to No Banking

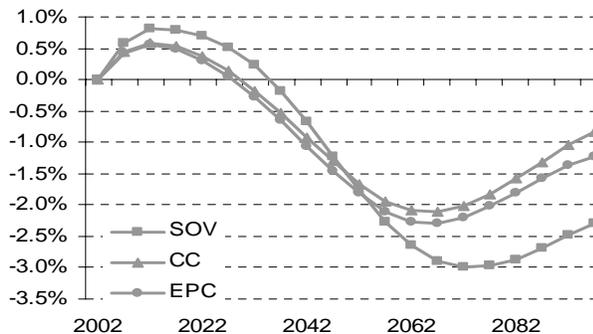


Figure 18. Change in Energy R&D Capital, Banking wrt to No Banking

The main conclusion is that banking plays an important role in accelerating the adoption and diffusion of energy efficient and/or carbon-free technologies. By inducing higher carbon prices in the short term, banking provides the right incentives for firms to switch to climate friendly technologies earlier than in the absence of banking. This has important macroeconomic and environmental effects. Earlier adoption of new technologies can indeed reduce stabilisation costs and enhance the environmental effectiveness of climate policy. These issues will be discussed in the next section.

5. The Cost of Climate Policy and Equity Considerations

Let us summarise all the results provided above by investigating how banking changes the costs of stabilisation policy and the distribution of these costs among regions. Table 3 shows our results.

Undiscounted	USA	OLDEURO	NEWEURO	KOSAU	CAJAZ	TE	MENA	SSA	SASIA	CHINA	EASIA	LACA	HI	LI	World
"SOV"	1.75%	-0.18%	6.12%	3.79%	0.70%	10.24%	15.34%	10.71%	8.26%	9.70%	9.68%	7.66%	1.93%	9.78%	5.57%
"CC"	4.20%	0.98%	8.06%	4.87%	1.76%	13.21%	14.68%	-4.73%	4.23%	9.54%	8.56%	6.86%	3.61%	7.72%	5.52%
"EPC"	10.04%	3.85%	13.01%	7.46%	4.29%	21.35%	12.79%	-44.84%	-5.61%	9.45%	5.94%	4.96%	7.76%	2.64%	5.38%
"Banking SOV"	0.59%	-0.42%	5.79%	3.49%	0.63%	10.08%	13.32%	9.31%	7.20%	8.73%	8.50%	6.45%	1.45%	8.54%	4.74%
"Banking CC"	4.14%	0.48%	7.59%	4.36%	1.66%	12.57%	12.81%	-3.55%	4.04%	8.79%	7.92%	5.27%	3.31%	6.88%	4.97%
"Banking EPC"	9.39%	2.97%	12.00%	6.62%	3.91%	19.86%	11.24%	-39.60%	-4.77%	8.66%	5.57%	3.48%	6.99%	2.31%	4.82%

Discounted	USA	OLDEURO	NEWEURO	KOSAU	CAJAZ	TE	MENA	SSA	SASIA	CHINA	EASIA	LACA	HI	LI	World
"H"	1.48%	0.29%	4.49%	2.64%	0.67%	8.08%	11.07%	8.14%	6.17%	6.44%	7.06%	5.22%	1.50%	6.90%	3.59%
"CC"	3.17%	0.99%	6.11%	3.49%	1.34%	10.33%	10.48%	-7.82%	2.14%	6.22%	5.99%	4.54%	2.63%	4.97%	3.54%
"EPC"	5.91%	2.26%	9.12%	4.98%	2.47%	15.04%	9.23%	-37.69%	-4.82%	6.08%	4.20%	3.37%	4.60%	1.60%	3.44%
"Banking SOV"	1.48%	0.32%	4.38%	2.53%	0.72%	8.19%	9.37%	6.99%	5.28%	5.53%	6.19%	4.34%	1.52%	5.90%	3.21%
"Banking CC"	3.28%	0.88%	5.79%	3.23%	1.35%	9.82%	8.92%	-6.73%	1.88%	5.53%	5.43%	3.57%	2.57%	4.30%	3.24%
"Banking EPC"	5.70%	1.98%	8.43%	4.53%	2.35%	13.94%	7.89%	-33.10%	-4.26%	5.38%	3.85%	2.47%	4.30%	1.31%	3.14%

Table 3. Stabilisation Cost, measured as GDP loss.

[For discounted values, a discount rate of 3% decreasing over time has been applied; negative figures correspond to gains]

As expected, Table 3 shows that greater market flexibility, i.e. banking, reduces policy costs. Higher early carbon prices induce early investment in R&D and in low carbon technologies, thus producing an indirect benefit on future abatement costs that adds to the direct benefit from banking. Savings in early periods are remarkable and suggest that banking might be a key option for reducing the total cost of climate policy. Table 3 suggests that the undiscounted aggregate cost, measured as GWP loss, declines from 5.57% to 4.74%, for the SOV allocation rule, from 5.52% to 4.97%, in the case of CC and from 5.38% to 4.82% for the EPC rule. This is equivalent to a net reduction of stabilisation costs

of 15.0%, 10.0% and 10.4%, for SOV, CC and EPC, respectively. Discounted costs decrease by 10.5%, 8.5% and 8.6%, for SOV, CC and EPC, respectively. At a more disaggregated level, without discounting, all regions, except the big sellers of permits in the CC and EPC scenarios, namely SASIA and SSA, are better off with banking than without. Discounting changes the net position of those regions whose benefits come late in the future.

Banking also affects the distribution of stabilisation costs. Our results (see Table 4) show that greater intertemporal flexibility provides larger benefits to regions with the most favourable initial distribution of emission rights. High Income regions reduce their (already low) share of stabilisation costs when banking is allowed under the SOV rule, as do Low Income regions when permits are distributed according to the EPC rule. It thus seems that banking favours sellers of permits, which can maximise their revenues by optimally distributing carbon rights across time.

	HI	LI
"H"	19%	81%
"CC"	35%	65%
"EPC"	77%	23%
"Banking SOV"	16%	84%
"Banking CC"	36%	64%
"Banking EPC"	78%	22%

Table 4. Distribution of Undiscounted Stabilisation Costs

The impact of banking on overall inequality is modest. Table 5 shows that, after 2030, the allocation of permits that yields the lowest Gini Coefficient, and thus the fairest distribution, is the EPC, both with and without banking. The most inequitable is instead SOV, as expected. Banking has a very mild effect on the distribution of policy costs. The only remarkable difference is a decrease of inequality when banking is allowed under the SOV scenario, because during the second half of the century carbon permit buyers (developing countries) can benefit from a lower carbon price. Inequality increases with banking in the EPC scenario, because the lower price of carbon yields a drop in the inflow of revenues to SSA and SASIA – two among the poorest regions of the world. Any difference in effort across allocation schemes is smoothed out during the second half of the century, due to the predominance of Low Income regions as emitters.

	BaU	"SOV"	"CC"	"EPC"	"Banking SOV"	"Banking CC"	"Banking EPC"
2050	0.485	0.493	0.476	0.464	0.487	0.477	0.465
2100	0.406	0.425	0.420	0.358	0.426	0.420	0.359

Table 5. Gini Indicators for 2050 and 2100 across different allocation schemes, with and without banking.

Without banking, the least costly policy is obtained when permits are distributed following the EPC principle. It is however noticeable how policy costs are extremely high for High Income countries, while some Low Income countries gain disproportionately from this allocation rule. By contrast, the SOV allocation, which would be the most likely to be accepted by OECD countries, appears to be the worst allocation in terms of overall policy costs.

With banking, the greater flexibility allows to smooth out the variance of policy costs across allocation schemes. Moreover, there are two different rankings, depending on whether costs are discounted or not. By looking at Table 6 we see that the SOV allocation becomes the first best strategy the less myopic the decision maker is. The reason is clear if we look at Figures 6 and 7 above. In the SOV scenario, banking creates a sharp increase of carbon price in the first years, but also the strongest drop after mid-century.

Policy Costs Differences w r t "EPC"	Discounted	Undiscounted
"SOV"	4.30%	3.51%
"CC"	2.84%	2.54%
"EPC"	-	-
"Banking SOV"	2.14%	-1.70%
"Banking CC"	3.03%	3.03%
"Banking EPC"	-	-

Table 6. Policy Cost Differences Across Allocation Schemes wrt the EPC allocation scheme

[For discounted figures a discount rate of 3% decreasing over time has been applied, negative differences represent gains]

The CC scheme is the one performing worst both with and without banking. Indeed, it benefits OECD countries immediately after 2030, but not enough to leave them the possibility to save the amount of permits required to cope with higher prices of permits.

Summing up, banking provides an incentive in favour of the early adoption of cleaner technologies, thus generating a positive intertemporal spillover effect. This effect is stronger when the allocation is such that mostly OECD countries bank permits. As a consequence, banking favours the adoption of the SOV allocation scheme, which gives OECD countries the incentive to bank, thus raising the price of permits in early periods and stimulating the development of climate friendly technologies. Technological spillovers then slowly diffuse innovation across regions (see Bosetti *et al.*, 2007a for a detailed description of this mechanism), thus further increasing the effectiveness of climate policy.

6. Conclusions

The previous sections of this paper have provided some new insights on the implications of allowing permit traders to bank tradable pollution rights. First, the efficiency gains – in terms of lower abatement costs – of adding (partial) “when flexibility” to the “where flexibility” of a fully integrated carbon market have been quantified. Second, the effects of banking on some key economic variables have been analysed under conditions that are not easily investigated in an analytical framework. In particular, the effects of banking on the timing of investments in carbon-free technologies and on R&D investments have been identified.

If the objective of climate policy is an ambitious GHG stabilisation target, our results show that intertemporal flexibility, even if partial, substantially increases efficiency. Cost reductions in terms of avoided GWP losses with respect to an inter-temporally rigid carbon market range – depending on the initial distribution of emission allowances – between 15% and 10% when discounting is not applied and between 10.5% and 8.5% when future losses are discounted.

Banking not only increases economic efficiency, but also the environmental effectiveness of climate policy, particularly in the short-term. Indeed, banking increases the amount of emissions abated in the first decades of this century, thus reducing the risk of irreversible environmental impacts of climate change.

Despite most of the world regions are better off with banking, independently of the initial distribution of permits, we have shown that intertemporal flexibility provides a relative advantage to those regions with a relatively more favourable distribution of emission rights. Banking empowers sellers more than buyers. Also the ranking of distribution rules – in terms of GWP losses – changes with banking; in

particular, our results suggest that with banking, the less myopic the social planner is, the more the Sovereignty rule outperforms other distribution rules. This is explained by the new incentives introduced by banking that stimulate the early adoption of carbon-free technologies (more in developed countries, where R&D is more effective in reducing the cost of these technologies).

Banking yields all the expected smoothing effect on emissions, abatement effort, price of carbon. Emission rights are first banked and then released in later periods, when the policy constraint becomes very stringent. The carbon market adapts, by first shrinking and then expanding in later periods. The price of carbon is higher in the first decades but lower in the second half of the century. Contrary to what predicted by analytical models, we find that an increasing time profile for the discounted price of carbon is fully consistent with banking. A “premium” over the interest rate is indeed necessary for agents to bank emission permits at the equilibrium.

Finally, let us stress we adopted a normative approach and not a descriptive one. Our findings belong to an ideal world in which all agents behave optimally and with perfect foresight over their future actions, the other agents’ decisions, and future states of the world. Nevertheless, we have been able to show that, when a richer framework of analysis is used, “when flexibility” yields some interesting unexpected results. We believe that these results can be useful both to economists – who will find a stimulus to build richer analytical models – and to policymakers – who may find in this paper useful information to design post 2012 carbon markets.

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Appendix: Model Equations and List of Variables.

In this Appendix we reproduce the main equations of the model. For a full description of the model please refer to Bosetti, Massetti and Tavoni (2007). The list of variables is reported at the end. In each region, indexed by n , a social planner maximises the following utility function:

$$W(n) = \sum_t U[C(n,t), L(n,t)] R(t) = \sum_t L(n,t) \{ \log[c(n,t)] \} R(t), \quad (\text{A1})$$

where t are 5-year time spans and the pure time preference discount factor is given by:

$$R(t) = \prod_{v=0}^t [1 + \rho(v)]^{-5}, \quad (\text{A2})$$

where the pure rate of time preference $\rho(v)$ is assumed to decline over time. Moreover, $c(n,t) = \frac{C(n,t)}{L(n,t)}$ is per capita consumption.

Economic module

The budget constraint defines consumption as net output less investments:

$$C(n,t) = Y(n,t) - I_C(n,t) - I_{R\&D} - \sum_j I_{R\&D,j}(n,t) - \sum_j I_j(n,t) - \sum_j O\&M_j(n,t) \quad (\text{A3})$$

Where j denotes energy technologies.

Output is produced via a nested CES function that combines a capital-labour aggregate and energy; capital and labour are obtained from a Cobb-Douglas function. The climate damage Ω reduces gross output; to obtain net output we subtract the costs of the fuels f and of CCS:

$$Y(n,t) = \frac{TFP(n,t) \left[\alpha(n) \cdot \left(K_C^{1-\beta(n)}(n,t) L^{\beta(n)}(n,t) \right)^{\rho} + (1 - \alpha(n)) \cdot ES(n,t)^{\rho} \right]^{1/\rho}}{\Omega(n,t)} - \sum_f \left(P_f(n,t) X_{f,extr}(n,t) + P_f^{int}(t) X_{f,neimp}(n,t) \right) - P_{CCS}(n,t) CCS(n,t) \quad (\text{A4})$$

Total factor productivity $TFP(n,t)$ evolves exogenously with time. Final good capital accumulates following the standard perpetual rule:

$$K_C(n,t+1) = K_C(n,t)(1 - \delta_C) + I_C(n,t) \quad (\text{A5})$$

Labour is assumed to be equal to population and evolves exogenously. Energy services are an aggregate of energy and a stock of knowledge combined with a CES function:

$$ES(n,t) = \left[\alpha_H HE(n,t)^{\rho_{ES}} + \alpha_{EN} EN(n,t)^{\rho_{ES}} \right]^{1/\rho_{ES}} \quad (\text{A6})$$

The stock of knowledge $HE(n,t)$ derives from energy R&D investment:

$$HE(n,t+1) = a I_{R\&D}(n,t)^b HE(n,t)^c + HE(n,t)(1 - \delta_{R\&D}) \quad (\text{A7})$$

Energy is a combination of electric and non-electric energy:

$$EN(n,t) = \left[\alpha_{EL} EL(n,t)^{\rho_{EN}} + \alpha_{NEL} NEL(n,t)^{\rho_{EN}} \right]^{1/\rho_{EN}}. \quad (A8)$$

Each factor is further decomposed into several sub-components. Figure 2 portrays a graphical illustration of the energy sector. Factors are aggregated using CES, linear and Leontief production functions.

For illustrative purposes, we show how electricity is produced via capital, operation and maintenance and resource use through a zero-elasticity Leontief aggregate:

$$EL_j(n,t) = \min\{\mu_{n,j} K_j(n,t); \tau_{n,j} O\&M_j(n,t); \varsigma_j X_{j,EL}(n,t)\}. \quad (A9)$$

Capital for electricity generation technologies accumulates as follows:

$$K_j(n,t+1) = K_j(n,t)(1-\delta_j) + \frac{I_j(n,t)}{SC_j(n,t)}, \quad (A10)$$

where, for selected technologies, the new capital investment cost $SC(n,t)$ decreases with the world cumulated installed capacity by means of Learning-by-Doing:

$$SC_j(n,t) = B_j(n) \sum_t \sum_n K_j(n,t)^{-\log_2 PR_j}. \quad (A11)$$

Operation and maintenance is treated as an investment that fully depreciates every year. The resources employed in electricity production are subtracted from output in equation A3 and A4. Their prices are calculated endogenously using a reduced-form cost function that allows for non-linearity in both the depletion effect and in the rate of extraction:

$$P_f(n,t) = \chi_f(n) + \pi_f(n) \left[\frac{Q_f(n,t-1)}{\bar{Q}_f(n,t)} \right]^{\psi_f(n)} \quad (A12)$$

where Q_f is cumulative extraction of fuel f :

$$Q_f(n,t-1) = Q_f(n,0) + \sum_{s=0}^{t-1} X_{f,extr}(n,s). \quad (A13)$$

Each country covers consumption of fuel f , $X_f(n,t)$, by either domestic extraction or imports, $X_{f,netimp}(n,t)$, or by a combination of both. If the country is a net exporter, $X_{f,netimp}(n,t)$ is negative.

$$X_f(n,t) = X_{f,extr}(n,t) + X_{f,netimp}(n,t) \quad (A14)$$

Climate Module

GHGs emissions from combustion of fossil fuels are derived by applying stoichiometric coefficients to the total amount of fossil fuels utilised minus the amount of CO₂ sequestered:

$$CO_2(n,t) = \sum_f \omega_{f,CO_2} X_f(n,t) - CCS(n,t). \quad (A15)$$

The damage function impacting output varies with global temperature:

$$\Omega(n,t) = \frac{1}{1 + (\theta_{1,n} T(t) + \theta_{2,n} T(t)^2)}. \quad (A16)$$

Temperature increases through augmented radiating forcing $F(t)$:

$$T(t+1) = T(t) + \sigma_1 \{ F(t+1) - \lambda T(t) - \sigma_2 [T(t) - T_{LO}(t)] \} \quad (A17)$$

which in turn depends on CO₂ concentrations:

$$F(t) = \eta \left\{ \log \left[M_{AT}(t) / M_{AT}^{PI} \right] - \log(2) \right\} + O(t), \quad (\text{A18})$$

caused by emissions from fuel combustion and land use change:

$$M_{AT}(t+1) = \sum_n \left[CO_2(n,t) + LU_j(t) \right] + \phi_{11} M_{AT}(t) + \phi_{21} M_{UP}(t), \quad (\text{A19})$$

$$M_{UP}(t+1) = \phi_{22} M_{UP}(t) + \phi_{12} M_{AT}(t) + \phi_{32} M_{LO}(t), \quad (\text{A19})$$

$$M_{LO}(t+1) = \phi_{33} M_{LO}(t) + \phi_{23} M_{UP}(t). \quad (\text{A20})$$

Model variables are denoted with the following symbols:

W = welfare

U = instantaneous utility

C = consumption

c = per-capita consumption

L = population

R = discount factor

Y = production

I_c = investment in final good

$I_{R\&D}$ = investment in energy R&D

I_j = investment in technology j

$O\&M$ = investment in operation and maintenance

TFP = total factor productivity

K_c = final good stock of capital

ES = energy services

Z = flow of new knowledge

Ω = damage

P_j = fossil fuel prices

X_j = fuel resources

P_{CCS} = price of CCS

CCS = CO₂ sequestered

HE = energy knowledge

EN = energy

EL = electric energy

NEL = non-electric energy

K_j = stock of capital of technology j

SC_j = investment cost

CO_2 = emissions from combustion of fossil fuels

M_{AT} = atmospheric CO₂ concentrations

LU = land-use carbon emissions

M_{UP} = upper oceans/biosphere CO₂ concentrations

M_{LO} = lower oceans CO₂ concentrations

F = radiative forcing

T = temperature level