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## ABSTRACT

### The Empirical Failure of the Expectations Hypothesis of the Term Structure of Bond Yields\*

This paper tests the expectations hypothesis (EH) using US monthly data for bond yields spanning the 1952-2003 sample period and ranging in maturity from 1 month to 10 years. We apply the Lagrange multiplier test developed by Bekaert and Hodrick (2001) and extend it to increase the test power: (a) by introducing economic variables as conditioning information; and (b) by using more than two bond yields in the model and testing the EH jointly on more than one pair of yields. While the conventional bivariate procedure provides mixed results, the more powerful testing procedures suggest rejection of the EH throughout the maturity spectrum examined.

JEL Classification: E43 and G10

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# 1 Introduction

The expectations hypothesis (EH) of the term structure of interest rates is the proposition that the long-term rate is determined by the market's expectation for the short-term rate plus a constant risk premium. The EH plays an important role in economics and finance, so it is not surprising that it has been investigated thoroughly using a variety of tests and data (e.g., Campbell and Shiller, 1991; Frankel and Froot 1987; Froot, 1989; Bekaert and Hodrick, 2001). It is well known that the tests that are commonly used to investigate the EH tend to generate paradoxical results (Campbell and Shiller, 1991). Recently, Bekaert, Hodrick and Marshall (1997) have shown that one of these tests can yield results that are unduly favorable to the EH when it is true, while Thornton (2005a) has shown that this test can yield results that are favorable to the EH when it is false.<sup>1</sup>

Given the statistical problems afflicting conventional tests of the EH, in this paper we employ a test that was originally proposed by Campbell and Shiller (1987) and recently made operational by Bekaert and Hodrick (2001). Bekaert and Hodrick (2001) develop a procedure for testing the parameter restrictions that the EH imposes on a vector autoregression (VAR) of the short- and long-term interest rates using a Lagrange multiplier (LM) test. The procedure is flexible and its size and power properties have been thoroughly investigated by Bekaert and Hodrick (2001). We apply this test to a data set for US bond yields ranging in maturity from 1 month to 10 years over the sample period 1952-2003.<sup>2</sup>

In order to increase the power of the EH testing procedure, we move beyond the bivariate comparisons of short- and long-term yields which dominate the existing literature. First, inspired by the growing literature linking macroeconomic fundamentals to the behavior of the term structure of interest rates (e.g. Kozicki and Tinsley, 2001; Evans and Marshall, 2002; Ang and Piazzesi, 2003; Ang,

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<sup>1</sup>Moreover, Kool and Thornton (2004) and Thornton (2005b) show how conventional tests may have generated misleading results in applied work.

<sup>2</sup>In a previous draft of this paper, we used the data set used by Campbell and Shiller (1991) in their seminal work to see how the conclusions of the EH are affected by the test used. The results on that data set are qualitatively identical to the ones reported here. However, in this paper we use a longer sample of data, which is identical to the Campbell-Shiller data up to 1991 but it extends to 2003. See Section 3 for a more detailed description of our data.

Piazzesi and Wei, 2003; Bekaert, Cho and Moreno, 2004; Rudebusch and Wu, 2004; Carriero, Favero and Kaminska, 2005; Dewachter and Lyrio, 2005; Diebold, Rudebusch and Aruoba, 2005; Clarida, Sarno, Taylor and Valente, 2006), we investigate the possibility of increasing the power of the EH testing procedure by examining the linkage between the term structure and macroeconomic variables, used as conditioning information. Second, we attempt to increase test power by using more than two yields in the VAR model and testing the EH on more than one pair of rates.

To anticipate our results, we find that the conventional bivariate procedure provides mixed results, suggesting that the EH is rejected at the short end of the maturity spectrum but not at the longer end. Specifically, consistent with a vast body of previous results (e.g. Campbell and Shiller, 1991), the EH is nearly always rejected when the maturity of the long-term rate is 24 months or shorter, but it is usually not rejected when the long-term rate is longer than 24 months. The more powerful procedures based on expanded VARs either with macroeconomic factors or with more than two bond yields suggest a more widespread rejection of the EH. In particular, the test based on a VAR including more than two bond yields suggests rejection of the EH throughout the maturity spectrum from 1 month to 10 years. Finally, the increase in power is documented using a simple Monte Carlo exercise designed to quantify the power gain obtained by moving from the bivariate VAR for bond yields to VARs that involve economic variables or more than two bond yields.

The outline of the paper is as follows. Section 2 presents the essential ingredients of the LM test proposed by Bekaert and Hodrick (2001). Section 3 briefly describes the data and preliminary unit root tests on our bond yields, designed to verify the validity of the stationarity condition required by the LM testing procedure. In Section 4, the LM test is applied to our data in three different settings: (i) the conventional bivariate VAR designed to make all possible pairwise comparisons among our 12 bond yields; (ii) the expanded VAR that includes other economic variables as conditioning information; and (iii) the expanded VAR that includes more than two bond yields. We report some Monte Carlo results to measure the empirical power of our testing procedures and some robustness checks in Section 5. The conclusions are presented in Section 6.

## 2 The VAR Test of the EH

The EH asserts that the long-term rate is determined by the market's expectation for the short-

term rate over the holding period of the long-term asset plus a constant risk premium:

$$(1) \quad r_t^n = (1/k) \sum_{i=0}^{k-1} E_t r_{t+mi}^m + \pi^{n,m},$$

where  $r_t^n$  is the  $n$ -period (long-term) rate;  $r_t^m$  is the  $m$ -period (short-term) rate;  $\pi^{n,m}$  is the constant risk premium that may vary with the maturity of the rates;  $E_t$  is the expectations operator; and  $k = n/m$  is an integer.<sup>3</sup> Much of the relevant literature relies on tests of the EH that are derived by parameterizing an algebraic manipulation of equation (1). In contrast, Bekaert and Hodrick's (2001) procedure assumes that the long- and short-term rates can be represented by a general VAR specification and test the restrictions implied by the EH on the VAR. Because a general VAR encompasses a wider range of potential data generating processes (DGPs) than equation (1), it is reasonable to conjecture that tests based on the VAR specification will be more powerful than tests derived from equation (1). In addition, the VAR approach has the advantage of being easy to extend—albeit computationally more intensive—by including more than two interest rates or incorporating conditioning variables that might affect market expectations.

The VAR restrictions implied by the EH are highly nonlinear, and Bekaert and Hodrick (2001) propose and study the properties of various tests for these restrictions. Their Monte Carlo evidence suggests that, while the distance metric, Wald and LM tests all exhibit size distortions, the LM test displays considerably better size properties. For a five percent nominal test, the empirical size of the LM test varied between 0.7 percent and 7.9 percent. In half of the cases, the empirical size was within one percentage point of the nominal size. Moreover, the LM test had reasonable power. To fit a VAR to interest rates data that satisfy the restrictions imposed by the EH, we use the constrained Generalized Method of Moments (GMM) estimation described in Bekaert and Hodrick (2001). As this procedure is relatively new, it is briefly presented here. Considering the EH for two bond yields, the VAR takes the form

$$(2) \quad (I - \Theta(L))y_{t+1} = \eta_{t+1}$$

for  $y_t \equiv (r_t^m, r_t^n)'$ ;  $I$  is the  $2 \times 2$  identity matrix;  $\Theta(L)$  is a lag polynomial; and  $\eta_{t+1}$  is a vector of

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<sup>3</sup>Shiller, Campbell, and Schoenholtz (1983) show that equation (1) is exact in some special cases and that it can be derived as a linear approximation to a number of nonlinear expectations theories of the term structure of interest rates.

error terms. Let  $g(z_t, \theta) \equiv \eta_t \otimes x_{t-1}$ , where  $x_{t-1}$  is a vector formed from stacking lagged values of  $y_t$ , and possibly with a constant term.  $z_t$  is defined as  $(y'_t, x'_{t-1})'$ ; and  $\theta$  is a vector formed from the parameters in  $\Theta(L)$ . GMM estimation imposes orthogonality conditions of the form  $E[g(z_t, \theta)] = 0$ . Using the sample moment condition

$$(3) \quad g_T(\theta) \equiv \frac{1}{T} \sum_{t=1}^T g(z_t, \theta),$$

GMM estimation proceeds by choosing  $\theta$  to minimize the following GMM criterion function:

$$(4) \quad J_T(\theta) \equiv g_T(\theta)' W g_T(\theta).$$

The optimal weighting matrix,  $W$  is defined as the inverse of  $\Omega \equiv \sum_{k=-\infty}^{k=\infty} E[g(z_t, \theta)g(z_{t-k}, \theta)']$  (Hansen, 1982). We can use GMM to estimate restricted VARs by forming a Lagrangian from the usual GMM quadratic objective function and a vector of parameter constraints. The Lagrangian is defined as

$$(5) \quad L(\theta, \gamma) = -\frac{1}{2} g_T(\theta)' \Omega_T^{-1} g_T(\theta) - a_T(\theta)' \gamma,$$

where  $\gamma$  is a vector of LMs and the constraints on  $\theta$  have been represented by the vector-valued function,  $a_T(\theta) = 0$ . Here the matrix  $\Omega_T$  is a consistent estimate of the matrix  $\Omega$  defined above.

In constructing our constrained estimates, we began with the unconstrained VAR parameters and iterated until the constraints were satisfied. The constraints that the EH imposes on a VAR can be seen by writing the VAR in first-order form, that is

$$(6) \quad \begin{pmatrix} r_t^m \\ r_t^n \\ r_{t-1}^m \\ r_{t-1}^n \\ \vdots \\ r_{t-k}^m \\ r_{t-k}^n \end{pmatrix} = \begin{pmatrix} \theta_1 & \theta_2 & \cdots & \theta_r \\ I & 0 & & 0 \\ 0 & I & & \vdots \\ \vdots & & \ddots & \\ 0 & & & I & 0 \end{pmatrix} \begin{pmatrix} r_{t-1}^m \\ r_{t-1}^n \\ r_{t-2}^m \\ r_{t-2}^n \\ \vdots \\ r_{t-k-1}^m \\ r_{t-k-1}^n \end{pmatrix} + \begin{pmatrix} \eta_t \\ 0 \\ \vdots \\ 0 \end{pmatrix}$$

or simply  $x_{t+1} = \Gamma x_t + v_{t+1}$ . Note that  $E_t(x_{t+k}) = \Gamma^k x_t$ , so that  $E_t(r_{t+k}^m) = e_1' \Gamma^k x_t$  for  $e_1 = (1, 0, \dots, 0)'$ . Note, too, that  $r_t^n = e_2' x_t$  for  $e_2 = (0, 1, 0, \dots, 0)'$ . Consequently, for any two bond

yields such that  $k = n/m$  is an integer, the EH implies that

$$(7) \quad r_t^n = \frac{1}{k} \sum_{i=0}^{k-1} E_t(r_{t+mi}^m),$$

so that the EH can be equivalently expressed as

$$(8) \quad e_2' x_t = \frac{1}{k} \sum_{i=0}^{k-1} e_1' \Gamma^{mi} x_t.$$

The constraints that satisfy the EH are given by

$$(9) \quad a_T(\theta) \equiv e_2' - \frac{1}{k} \sum_{i=0}^{k-1} e_1' \Gamma^{mi} = 0.$$

No simple closed form exists for the Jacobian of these constraints. Consequently, they are calculated numerically. The iterative method used in this paper is the Broyden-Fletcher-Goldfarb-Shanno (BFGS) method for numerical optimization. If the constraints have a significant impact on parameter estimation, then the estimated LMs should be significantly different from zero. Bekaert and Hodrick (2001) derive the asymptotic distribution of the LM test statistic for the null hypothesis that the multipliers are jointly zero, i.e. for the hypothesis that the EH of the term structure of interest rates is valid. The LM test statistic is asymptotically distributed as  $\chi^2(l)$ , where  $l$  is the number of constraints.<sup>4</sup>

### 3 Data and Preliminary Unit Root Tests

We use continuously compounded yields on riskless pure discount bonds for the US. These yields were calculated using end-of-month observations for bonds ranging in maturity from 1 to 120 months (or 10 years) over the period 1952:01 to 2003:12, taken from Bloomberg. The continuously compounded yields on riskless pure discount bonds were obtained using FORTRAN codes kindly provided

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<sup>4</sup>See Bekaert and Hodrick (2001) for a full technical exposition of the iterative procedure and the asymptotic distribution of the LM statistic. Note that the above analysis presumes that the short- and long-term rates are stationary, or I(0). If rates are I(1), the above procedure needs amending, which may be done building on the work of Campbell and Shiller (1987). See also Hall, Anderson, and Granger (1992), Engsted and Tangaard (1994), Sarno and Thornton (2003), Clarida, Sarno, Taylor and Valente (2006).

by Robert Bliss and Dan Waggoner, based on Bliss (1997) and Waggoner (1997). The estimation method is based on the McCulloch cubic spline parameters, estimated using programs originally provided by J. Huston McCulloch.

In order to check the quality of our resulting data set we compare our time series for continuously compounded yields on riskless pure discount bonds to the equivalent time series obtained by McCulloch and Kwon (1993) in constructing an update of the data used by Campbell and Shiller (1991). Figure 1 graphs our time series of bond yields over the full sample period 1952:1-2003:12 (dotted line) and the corresponding bond yields calculated by McCulloch and Kwon (1993) over the shorter sample period 1952:1-1991:02 (solid bold line). The graphs confirm that the time series are virtually identical for the overlapping period, so that our series may be considered as a consistent update of the data used by Campbell and Shiller (1991) and McCulloch and Kwon (1993).

As an important preliminary to the implementation of the procedure for testing the EH, we tested for unit root behavior of each of the bond yields examined.<sup>5</sup> This exercise is relevant since the VAR test described in Section 2 and its expanded version considered in the empirical work rely on the assumption that bond yields are stationary. While finance theory is generally based on the assumption that interest rates are stationary, and we have a strong economic prior that this is the case, it is often difficult to provide empirical evidence against the hypothesis that interest rates have a unit root. This is likely to be due to the low power of most conventional unit root tests in the presence of finite-sample realizations of persistent—albeit stationary—processes with a root strictly below but very close to unity (e.g., Stock and Watson, 1988, 1999).

We rely on two different unit root tests: the test proposed by Kwiatkowski, Phillips, Schmidt and Shin (1992), the KPSS test, for the null hypothesis of stationarity; and the point optimal unit-root test proposed by Elliott, Rothenberg and Stock (1996), the  $P_T$  test, for the null hypothesis of a unit root. The latter test is the unit-root test which was found to exhibit the best power properties among the several tests investigated by Elliott, Rothenberg and Stock (1996).

The results from applying both test statistics are reported in Table 1. For each time series considered, we selected the lag length on the basis of the Akaike information criterion. The results

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<sup>5</sup>In all statistical tests executed in this and subsequent sections, we use a five percent nominal significance level, unless otherwise specified.

indicate that the KPSS test fails to reject the null of stationarity in each case, whereas the  $P_T$  test statistic rejects the null hypothesis of a unit root for each bond yield examined at conventional significance levels. Therefore, these tests suggest that all bond yields examined are realizations from stationary stochastic processes, consistent with our economic prior and with the assumption underlying the VAR test of the EH proposed by Bekaert and Hodrick (2001).

## 4 The VAR Test Results

In this section we report the LM tests for the null hypothesis that the EH holds in three different settings: (i) the conventional bivariate VAR, designed to make all possible pairwise comparisons among our 12 bond yields; (ii) the expanded VAR that includes other economic variables as conditioning information; and (iii) the expanded VAR that includes more than two bond yields.

The data were adjusted for their mean prior to carrying out the VAR tests. The order of the VAR is determined by minimizing the Akaike information criterion.

### A VAR tests for Bivariate Comparisons of Bond Yields

Bekaert, Hodrick and Marshall (1997) show significant bias in standard tests of the EH because of the extreme persistence in short-term rates. Bekaert and Hodrick (2001) show that this bias is reduced, but not eliminated in the VAR test they propose. Following Bekaert and Hodrick (2001) we correct for this bias by using the unconstrained estimates of the VAR for each rate pair to generate 100,000 artificial data sets of the sample size corresponding to each pair of rates using i.i.d. bootstraps of the residuals. The VAR parameters are re-estimated to determine the bias—the difference between the average value of these parameters and the known values of the data generating process. These estimates are used to correct for the bias of the original VAR estimates. Bias-corrected parameters that satisfy the EH are obtained by using the unconstrained, bias-corrected parameters and residuals to simulate a series of 71,000 observations, with the initial 1,000 observations discarded. The bias-corrected, constrained parameters are obtained from implementing the procedure described in Section 2. The empirical distribution for the bias-corrected LM statistics is then obtained from 25,000 replications of this procedure applied to artificial data obtained using the bias-corrected, constrained parameters and the corresponding residuals. The empirical distribution and critical values for the LM statistics were relatively unaffected by the choice of maturity pair. Nevertheless, the asymptotic

critical values were always smaller than the bootstrapped critical values. Hence, while in many cases, consistent with Bekaert and Hodrick’s (2001) findings, the size distortions of the LM test were relatively small, this was not uniformly the case. These results suggest that using the asymptotic critical values can be misleading and, therefore, we rely on the empirical distribution in our analysis.

The LM test results are presented in Table 2, where we report the  $p$ -values for the null hypothesis that the EH holds for all possible combinations of the integer  $k = n/m$  (there are 48 such combinations). The figures in bold denote cases where the null hypothesis is not rejected at the five percent significance level. Consistent with Campbell and Shiller (1991), the EH is always rejected at the shorter end of the maturity spectrum, but not at the longer end. Specifically, the EH is rejected in every case where the long-term rate is two years or shorter or, put another way, the EH is not rejected only in instances where the long-term rate is three years or longer.

Another way to evaluate the EH is by assessing its forecasting accuracy: if the EH is valid, one should be able to forecast the long-term rate by making the forecasts conditional on the information embedded in the EH. To this end, Campbell and Shiller (1987, 1991) suggest comparing the ratio of the variance of the “theoretical” long-term rate to the variance of the actual data, where the “theoretical” long-term rate is the rate under the assumption that the EH holds.<sup>6</sup> In order to formally test the EH using the ratios of the variances, we obtained the distributions of these ratios under the null that the EH holds. Specifically, we calculated these ratios for each of 25,000 replications of data generated using the bias-corrected, constrained VAR. Three features of these results are noteworthy.<sup>7</sup> First, consistent with the results of Campbell and Shiller (1991), these ratios are always less than unity, suggesting that the long-term rate is too variable to be consistent with the EH. Second, the forecast accuracy declines as  $k$  increases or as  $(n - m)$  increases for a given value of  $k$ . This is reflected by the fact that these ratios decline as  $n$  increases for a given  $m$ , suggesting that the forecasting accuracy declines as the forecast horizon lengthens. Third, these ratios tend to be closer to unity when the EH is rejected by the LM test than when it is not. Hence, the size of the ratio appears to be a misleading indicator of the validity of the EH. Consistent with the results of the LM test, the results indicate that the EH is rejected at the short end of the maturity spectrum but not at the longer end.

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<sup>6</sup>The theoretical rate is  $r_t^{n'} = (1/k)e_1'(I - \Gamma^n)(I - \Gamma^m)^{-1}y_t$ , where  $e_1$  and  $\Gamma$  are as defined in Section 2.

<sup>7</sup>These results are not reported to conserve space, but they remain available from the authors upon request.

However, our results suggest that these ratios may be misleading in evaluating the validity of the EH and may be less deserving of attention than the other VAR-based tests. This finding confirms the results of Bekaert, Wei and Xing (2004), who also investigate the term structure at the long and short end (together with uncovered interest rate parity) and document large biases and wide finite-sample distributions of these variance ratio statistics.

## B Extension to Allow Macroeconomic Variables as Conditioning Information

Conceptually, the VAR can also include other economic variables. There is a large and rapidly developing literature on various aspects of the relationship between macroeconomic variables and the yield curve (e.g. Kozicki and Tinsley, 2001; Evans and Marshall, 2002; Ang and Piazzesi, 2003; Ang, Piazzesi and Wei, 2003; Bekaert, Cho and Moreno, 2004; Rudebusch and Wu, 2004; Carriero, Favero and Kaminska, 2005; Dewachter and Lyrio, 2005; Diebold, Rudebusch and Aruoba, 2005; Clarida, Sarno, Taylor and Valente, 2006). This interest is in part motivated by the realization that, while the term structure can be well characterized by a few latent factors, such analyses provide little insight into the forces that shift or rotate the term structure. It is also motivated by the realization that macroeconomic forces may drive the principal determinants of nominal interest rates (inflation and the real economy), and by the fact that monetary policy actions—which are in large part driven by these same forces—have consequences for short-term rates which are crucial to the rest of the term structure.

For example, Gurkaynak, Sack, and Swanson (2005) show that long-term rates respond significantly to macroeconomic surprises that should have only a transitory effect on short-term interest rates. They interpret this to be evidence that market participants adjust their expectations of long-run inflation in response to such shocks. Clarida, Sarno, Taylor and Valente (2006) examine the relationship between interest rates of different maturities for the US, Germany and Japan over the period 1982-2000, using a multivariate modelling framework capable of simultaneously allowing for asymmetric adjustment and regime shifts which allows for time-varying term premia and other short-run deviations from the EH of the term structure. They show how the term structure of interest rates displays regime switches closely related to key state variables driving monetary policy decisions. This evidence adds to previous findings that the behavior of the entire yield curve is associated with

the state of the business cycle, which may have statistically and economically important first-order effects on expectations of inflation, monetary policy and nominal interest rates (e.g. Bansal and Zhou, 2002). In any event, recent research suggests an important relationship between macroeconomic variables and the term structure. To our knowledge, only Carriero, Favero, and Kaminska (2005) directly investigate the effects of including such variables on the EH. They do not test the EH *per se*, however. Rather, they assess the benefits from including the macroeconomic variables for forecasts of the short-term rate.

Following Carriero, Favero and Kaminska (2005) we used the CPI inflation rate and the unemployment rate which, like interest rates, are not subject to revision. Preliminary to testing the EH, we tested whether the economic variables were significant in interest rate equations of the VAR using the block exogeneity test suggested by Hamilton (1994). The results, reported in Table 3, indicate that in nearly all cases the null hypothesis of no effect is rejected at the five percent significance level. Hence, including these variables could affect tests of the EH.

The LM tests for the expanded VAR are presented in Table 4, which reports the bootstrapped  $p$ -values calculated using the same procedure described in Section 4B. Again, the figures in bold denote cases where the null hypothesis is not rejected at the five percent significance level. The EH is rejected in every case where the long-term rate is three years or shorter and in most cases when the long-term rate is 4 years. It is generally not rejected when the maturity of the long-term rate is 5 or 10 years.

Hence, when the interaction between the term structure and the macro economy is accounted for, the VAR tests yield a stronger rejection of the EH. As for the simple bivariate VAR tests in the previous sub-section, the EH is rejected at the shorter end but not at the longer end of the maturity spectrum, but the shorter end is now up to 3 years and arguably 4 years. This suggests that the structure of interest rates reflects information contained in these macroeconomic variables and that the test power may be increased by conditioning on macroeconomic information. When this information is accounted for, the marginal information in the long-term rate has relatively little additional information useful for predicting the short-term rate.

## C Extension to Three Bond Yields

Tests of the EH need not be limited to comparisons of two rates, although this is what is typically

done in the relevant literature. In this sub-section we extend the VAR test to three (or more) bond yields. When applying the test to, say, three interest rates with maturities  $n > h > m$ , there are two ways to impose the EH on the  $n$ -period rate. Because the Bekaert-Hodrick (2001) test procedure determines the restrictions that satisfy the EH, it can be shown that the results are invariant to how the EH is imposed on the  $n$ -period rate.<sup>8</sup>

We applied the Bekaert-Hodrick test to all of the 91 possible three-interest-rate combinations. The  $p$ -values of the LM tests that the EH holds are reported in Table 5. Unfortunately, the procedure failed to converge in 15 of the 91 cases—denoted as NC in Table 5. In all of these cases where the procedure converged, the EH was overwhelmingly rejected at very low significance levels. Interpreting non-convergence as a rejection of the EH, the evidence is overwhelmingly against the EH when three rates are considered.<sup>9</sup> The non-convergence does not appear to be related to the model stability. Indeed, the largest root of the unrestricted VAR tended to be smaller for the three-interest rates VARs. The evidence suggests that when more than two bond yields are considered, it is less likely that the estimated parameters of the unrestricted VAR will satisfy the restrictions implied by the EH. Note that the increase in power in this case is coming from the fact that the null hypothesis is now a joint hypothesis that the EH holds for two pairs of bond yields. Hence, this is a more stringent test of the EH than the tests based on the bivariate VAR with two bond yields and the VAR with macroeconomic factors, which test the validity of the EH on one pair of bond yields at the time.<sup>10</sup>

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<sup>8</sup>It can be shown that when the EH holds for  $r^m$  and  $r^h$  and for  $r^m$  and  $r^n$ , it automatically holds for  $r^h$  and  $r^n$ .

<sup>9</sup>The BFGS method is widely known to have good convergence properties when started near an optimum point and works reasonably well even for ‘ill-behaved problems’ (Greene, 2000, p. 192). It is plausible to think that Bekaert and Hodrick’s modification of it would have good convergence properties near an optimum as well. Thus, the non-convergence of the method may be due to unrestricted VAR coefficients being “too far” from any set of coefficients that satisfy the EH. We are inclined to think that even if a different method were able to derive a set of restricted coefficients, their distance from the unrestricted set would most likely cause the LM test to reject the EH. We investigate the robustness of the choice of the iteration method later in the paper.

<sup>10</sup>Because the test on the trivariate VAR is a joint test, the increase in power reported here may be due to the joint nature of the test and/or the expansion in the information set. At the suggestion of the referee, we investigate the source of the increase in power by expanding the information set of the bivariate VAR by including a third bond

## D Summing Up the Empirical Results from the VAR Tests

Overall, the VAR tests of the EH carried out in this section provide three clear findings. First, incorporating macroeconomic factors as conditioning information in the VARs enhances the power of the tests for the hypothesis that the EH holds. This is consistent with the exploding literature linking macroeconomic factors to the term structure of interest rates, cited earlier. Second, moving beyond bivariate analysis towards VAR models that incorporate more than two bond yields appears to also yield a substantial increase in test power. Third, taking together our results from the three different variants of the VAR-based LM tests, we observe a rejection of the EH of the term structure of interest rates not only at the short end of the term structure—as it is often recorded by the relevant literature—but throughout the maturity spectrum from 1-month to 10-year yields.<sup>11</sup>

We now turn to some Monte Carlo evidence and robustness checks on our core results.

## 5 Monte Carlo Evidence and Robustness Checks

In this section we investigate further our claim that the two tests based on expanded VARs, either with macroeconomic fundamentals or with more than two bond yields, lead to an increase in power relative to the simple bivariate VAR tests. To this end, we conduct Monte Carlo experiments designed to measure the empirical power of the three VAR-based LM tests employed in the empirical analysis. We also report some robustness checks carried out to assess the sensitivity of our core results, presented in Section 4, to the potential presence of structural breaks in the VARs and to the choice of the optimization method used in performing the LM tests.

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yield. This conditioning information is interesting because affine term structure models predict that term structure information should exhaust the information set. Specifically, we included the 12-month yield in each equation of the VAR. The test results—available from the authors upon request—are similar to the results reported in Table 4. The EH is rejected in every case where the long-term rate is 3 years or shorter and in one case when the long-term rate is 4 years, but not when the maturity of the long-term yield is 5 or 10 years. While preliminary, these findings suggest that the increase in power is likely due to both to the expansion of the information set and the joint nature of the test.

<sup>11</sup>Given the rejections of the EH, the VARs employed in this paper might provide insights on the behavior of observed term premia. We leave this possibility for future research.

## A The Empirical Power of the VAR Tests

We calculate the empirical power of the LM tests as the percent of Monte Carlo experiments carried out under the alternative hypothesis that the EH does not hold where the test statistic exceeds the empirical critical value, calculated by bootstrap as described in Section 4. Table 6 reports the values of the empirical power of the LM tests for the three different VARs considered in this paper. Following Bekaert and Hodrick (2001), we use the unconstrained VAR as the alternative hypothesis.<sup>12</sup>

The LM test calculated from the bivariate VAR with two bond yields (Case 1 in Table 6) displays an empirical power of about 65 percent at the one percent level, 71 percent at the five percent level, and 73 percent at the ten percent level. These results are comparable to the empirical power recorded by Bekaert and Hodrick (2001), who report similar empirical power for EH tests.

For the expanded VAR with macroeconomic factors as conditioning information (Case 2 in Table 6), power increases to about 78 percent at the one percent level, 82 percent at the five percent level, and about 85 percent at the ten percent level. This is consistent both with the conjecture that macroeconomic conditioning information enhances the power of the EH tests and with the findings presented in Section 4B.

Finally, the highest power is obtained for the VAR with three bond yields (Case 3 in Table 6), where the empirical power is 87 percent at the one percent level, and about 96 and 98 percent at the five and ten percent levels, respectively, for the null hypothesis that the EH holds on two pairs of bond yields. Again, this is consistent both with our priors and with the finding that the EH is rejected throughout the US yield curve, reported in Section 4C.

Overall, the Monte Carlo evidence confirms that the two expanded VARs lead to more powerful LM tests.

## B Structural Breaks

Campbell and Shiller (1991) found evidence that the EH performed better during the 1952-78 sample period than during the entire sample period. To investigate the robustness of the results

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<sup>12</sup>Specifically, the results reported were obtained using the unconstrained VAR for bond yields with maturities of 1 and 2 months for the simple bivariate VAR with two bond yields and the expanded VAR with macroeconomic factors, whereas we used the unconstrained VAR for bond yields with maturity of 1, 2 and 3 months for the case with three bond yields. This choice was made on the basis of the fact that these were the combinations where our code ran faster.

to the sample period, we test for structural breaks in the VARs using the procedure for endogenous break testing suggested by Andrews and Ploberger (1994). This procedure is applied to each of the 48 rate combinations for the bivariate VARs.<sup>13</sup>

The results, reported in Table 7, suggest a variety of structural breaks which cluster around two periods, 1980-81 and 1961-62. Because the qualitative results were relatively insensitive to the specific choice of the break date, the results are presented only for two periods. The first period, 1952:01-1978:12, is consistent with the Campbell-Shiller's argument that the EH may have performed better before 1978 than after. The second period, 1982:01-2003:12, takes into account the finding that the main structural break appears to be around 1980-81, which is consistent with a widely held view that the behavior of interest rates may have changed in the early 1980s (e.g. Ang and Bekaert, 2002).<sup>14</sup>

The  $p$ -values from the LM statistics for the bivariate VARs are presented in Table 8 for both sub-samples examined (Panels A-B). The qualitative conclusions about the EH are similar for the two periods. For most interest rate combinations where the EH was not rejected in the first period, it was also not rejected in the second period. Moreover, the EH is generally rejected at the short end of the maturity spectrum but not at the longer end. However, there is some evidence in favor of the Campbell-Shiller conjecture that the EH performed better in the pre-1978 period since the rejection of the EH in that period is very robust only when the longer rate has maturity of 1 year or less, whereas in the post-1982 sample period we find a rejection of the EH that is quite robust when the longer rate has a maturity of 2 years or shorter. Overall, these findings resemble the results for the full sample reported in Table 2.

While Table 8 reports the sub-samples results only for the bivariate LM test with two bond yields,

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<sup>13</sup>Essentially we applied the structural break tests following the same reasoning as Bernanke and Mihov (1998, p. 889), by examining all possible combinations.

<sup>14</sup>The three years from 1979:01 to 1982:12 were excluded because of the well known volatility in bond yields during this period and because of the uncertainty in the exact timing of the structural break noted by Ang and Bekaert (2002, p. 163), who observe that: 'The behavior of interest rates in the 1979-1982 period in the US [...] seems to indicate a structural break in the time series.' Nevertheless, we performed the LM test for the break point selected for each interest rate pair and for some other choices of the break points. The qualitative conclusions were fairly robust to alternative choices of the break points.

we also performed the sub-sample analysis on the LM tests for the expanded VAR with macroeconomic fundamentals and with three bond yields for some of the rates combinations considered. For the rates combinations examined, the results across the two sub-samples were consistent with the full-sample results in Tables 4-5.

## C Optimization Method and Convergence

The LM testing procedure failed to converge in 15 of the 91 cases when using the VAR with three bond yields. However, because the LM test results were obtained using the BFGS method, we investigate the convergence properties of the LM tests when using two alternative optimization methods, namely the Newton and the Davidon-Fletcher-Powell (DFP) methods. The Newton method did not converge in 55 cases whereas the DFP method did not converge in 19 of the 91 cases examined. In all cases where the two alternative procedures converge, the EH is rejected.

Also, in Section 4C we interpreted non-convergence as a possible rejection of the EH. In this regard, it is interesting to note that in the 8 instances where the DFP method converged when the BFGS method did not, the EH is rejected with a very low  $p$ -value. These results are consistent with our suggestion in Section 4C that non-convergence may be due to the unrestricted VAR coefficients being “too far” from any set of coefficients that satisfy the EH. Of course, these results do not prove that non-convergence implies a rejection of the EH constraints since non-convergence may be caused by factors other than large violations of the constraints.<sup>15</sup>

## 6 Conclusions

The EH plays important roles in economics and finance and, not surprisingly, has been widely tested using a variety of tests and data. This paper extends this literature by testing the restrictions implied by the EH on a VAR of the long- and short-term rate using the Lagrange multiplier test recently proposed by Bekaert and Hodrick (2001). The VAR test rejects the EH at the shorter end of the maturity spectrum (when the long rate is 2 years or shorter), but not at the longer end, consistent with the mixed results often recorded in the relevant literature (Campbell and Shiller, 1987, 1991).

In order to increase the test power, we extended the analysis in two directions. First, inspired by the growing literature linking macroeconomic fundamentals to the behavior of the term structure of

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<sup>15</sup>We are thankful to James McCulloch, Roel Oomen and Mark Salmon for a useful conversation on this issue.

interest rates, we investigate the possibility of increasing test power by expanding the VAR model to allow macroeconomic variables as conditioning information. Second, we increase the size of the VAR by using more than two yields and testing the EH on more than one pair of rates. Our results are less encouraging for the EH when the interaction between the term structure and the macroeconomy is considered and when the VARs were extended to include more than two bond yields. When the relationship between the term structure and the unemployment and inflation rates is accounted for, the EH was rejected in nearly all cases when the longer rate has a maturity of 4 years and in all cases when the longer rate is 3 years or shorter. In addition, for the model with three bond yields, either the EH was strongly rejected at very low marginal significance levels or the procedure failed to converge. In addition, the increase in test power obtained from conditioning on macroeconomic variables and from including more than two bond yields is supported by a Monte Carlo analysis which suggests that empirical power is higher for the expanded VARs.

The evidence in this paper confirms the usefulness of the recently developed testing procedure proposed by Bekaert and Hodrick (2001) and the potential to enhance its power properties by extending the underlying models to allow for macroeconomic factors or several interest rates. More importantly, our empirical results suggest that departures from the EH of the term structure of interest rates are statistically important and pervasive throughout the US yield curve from 1-month to 10-year rates. This may be due to various reasons, including the violation of the assumption of a constant risk premium underlying the EH and the possibility that the models we use, albeit richer than many others examined in the literature, may still provide a poor approximation to the potentially much more complex process that drives the term structure of interest rates. Much more work needs to be done to understand the term structure of bond yields. The evidence presented here suggests that the term structure is likely to be considerably more complex than the EH suggests.

**Table 1. Unit root tests**

$m$	$P_T$	$KPSS$
1	4.590	0.174
2	5.112	0.157
3	5.383	0.154
4	5.560	0.152
6	5.593	0.150
9	5.823	0.149
12	6.404	0.151
24	8.246	0.161
36	9.837	0.172
48	11.380	0.182
60	12.875	0.193
120	18.390	0.246

**Notes:** The figures reported are unit root test statistics.  $m$  denotes the maturity of the zero-coupon bond.  $P_T$  is the Elliott, Rothenberg and Stock (1996) point optimal unit-root test of the null hypothesis that the time series contains a unit root.  $KPSS$  is the Kwiatkowski, Phillips, Schmidt and Shin (1992) test of the null hypothesis that the series is stationary. Both test statistics have been computed by estimating the residual spectrum at frequency zero by means of the Andrews' (1991) rule with a quadratic spectral kernel. The five percent critical values are 3.26 (Elliott, Rothenberg and Stock, 1996; Table 1) and 0.463 (Kwiatkowski, Phillips, Schmidt and Shin, 1992; Table 1) for the  $P_T$  and  $KPSS$  test respectively.

**Table 2. LM test statistics: bivariate VAR**

$n/m$	1	2	3	4	6	9	12	24	60
2	0								
3	0								
4	0	0							
6	0	0	0						
9	0		0						
12	0	0	0	0	0				
24	0.025	0.047	0.018	0.008	0.001		0		
36	<b>0.104</b>	<b>0.204</b>	<b>0.143</b>	<b>0.124</b>	<b>0.118</b>	<b>0.092</b>	<b>0.053</b>		
48	<b>0.264</b>	<b>0.370</b>	<b>0.304</b>	<b>0.294</b>	<b>0.335</b>		0.022	<b>0.064</b>	
60	<b>0.433</b>	<b>0.489</b>	<b>0.427</b>	<b>0.429</b>	<b>0.497</b>		<b>0.114</b>		
120	<b>0.828</b>	<b>0.795</b>	<b>0.731</b>	<b>0.751</b>	<b>0.836</b>		<b>0.064</b>	<b>0.057</b>	<b>0.162</b>

**Notes:** The tests were performed in a bivariate VAR comprising two bond yields. The figures reported are  $p$ -values of Bekaert and Hodrick's (2001) LM tests of the null hypothesis that the EH is validated by the data for each of the possible 48 combinations of our 12 bond yields where  $n/m$  is an integer. The  $p$ -values are calculated by bootstrap as described in the text. 0 denotes  $p$ -values below  $10^{-4}$ . Figures in bold denote cases where the EH is not rejected at the five percent significance level.

**Table 3. Block exogeneity tests**

$n/m$	1	2	3	4	6	9	12	24	60
2	<b>0.111</b>								
3	<b>0.070</b>								
4	0.038	0.007							
6	<b>0.053</b>	0.041	<b>0.077</b>						
9	0.020		0.023						
12	0.001	0.001	0.001	0	0				
24	0	0	0	0	0		0		
36	0	0	0	0	0	0	0		
48	0	0	0	0	0		0	0	
60	0	0	0	0	0		0		
120	0	0	0	0	0		0	0.001	0.001

**Notes:** The tests were performed in a bivariate VAR comprising two bond yields and allowing for two macroeconomic fundamentals (unemployment rate and inflation rate) in each of the two VAR equations. The figures reported are  $p$ -values for the likelihood ratio (LR) test of the null hypothesis that the coefficients in the bond yields equations attached to the macroeconomic fundamentals are jointly equal to zero. The test statistics were calculated by using the small-sample correction proposed by Sims (1980, p. 17). 0 denotes  $p$ -values below  $10^{-4}$ . Figures in bold denote cases where the null hypothesis of no block exogeneity is not rejected at the five percent significance level.

**Table 4. LM test statistics: bivariate VAR with macroeconomic fundamentals as conditioning information**

$n/m$	1	2	3	4	6	9	12	24	60
2	0								
3	0								
4	0	0							
6	0	0	0						
9	0		0						
12	0	0	0	0	0				
24	0.001	0	0	0	0		0		
36	0.014	0.006	0.017	0.033	0.024	0.011	0.015		
48	0.041	0.017	0.032	0.011	<b>0.114</b>		<b>0.125</b>	0.003	
60	<b>0.088</b>	0.043	<b>0.117</b>	<b>0.227</b>	<b>0.257</b>		<b>0.308</b>		
120	<b>0.304</b>	<b>0.180</b>	<b>0.378</b>	<b>0.571</b>	<b>0.639</b>		<b>0.762</b>	<b>0.519</b>	<b>0.583</b>

**Notes:** The tests were performed in a bivariate VAR comprising two bond yields and allowing for two macroeconomic fundamentals (unemployment rate and inflation rate) in each of the two VAR equations. The figures reported are  $p$ -values of Bekaert and Hodrick's (2001) LM tests of the null hypothesis that the EH is validated by the data for each of the possible 48 combinations of our 12 bond yields where  $n/m$  is an integer. The  $p$ -values are calculated by bootstrap as described in the text. 0 denotes  $p$ -values below  $10^{-4}$ . Figures in bold denote cases where the EH is not rejected at the five percent significance level.

**Table 5. LM test statistics: trivariate VAR**

$(n, m)/h$	4	6	9	12	24	36	48	60	120
(1,2)	0	0		0	0	0	0	0	NC
(1,3)		0	0	0	0	0	NC	NC	0
(1,4)				0	0	0	0	0	0
(1,6)				0	0	0	0	0	NC
(1,9)						0			
(1,12)					0	0	0	0	0
(1,24)							0		0
(1,60)									NC
(2,4)				0	0	0	0	0	NC
(2,6)				0	0	0	0	0	0
(2,12)					0	0	0	0	0
(2,24)							0		0
(2,60)									NC
(3,6)				0	0	0	0	0	0
(3,9)						0			
(3,12)					0	0	0	0	0
(3,24)							NC		NC
(3,60)									NC
(4,12)					0	0	0	0	NC
(4,24)							0		NC
(4,60)									NC
(6,12)					0	0	0	0	0
(6,24)							0		0
(6,60)									NC
(12,24)							0		0
(12,60)									NC

**Notes:** The tests of the null hypothesis that the EH is valid for two pairs of bond yields were performed in a trivariate VAR comprising three bond yields. The figures reported are  $p$ -values of Bekaert and Hodrick's (2001) LM tests of the null hypothesis that the EH is validated by the data for each of the possible 91 three-interest-rate combinations of our 12 bond yields where  $n/m$  is an integer. The  $p$ -values are calculated by bootstrap as described in the text. 0 denotes  $p$ -values below  $10^{-4}$ . NC indicates cases where convergence was not achieved.

**Table 6. Empirical Power of LM tests of the EH**

Nominal Level		
0.01	0.05	0.10
<i>Case 1</i>		
0.648	0.707	0.734
<i>Case 2</i>		
0.779	0.820	0.854
<i>Case 3</i>		
0.870	0.955	0.981

**Notes:** The figures denote the empirical power of the LM test statistic when the data are generated under the alternative hypothesis, as described in the text, under three different cases. *Case 1* relates to a bivariate VAR with two bond yields. *Case 2* relates to a bivariate VAR with two bond yields and macroeconomic fundamentals (unemployment rate and inflation rate), and *Case 3* relates to a trivariate VAR with three bond yields.

**Table 7. Structural break tests**

$n/m$	1	2	3	4	6	9	12	24	60
2	0.026 [1980 : 3]								
3	0.019 [1980 : 3]								
4	0.007 [1982 : 4]	0.063 [1981 : 8]							
6	0.020 [1981 : 8]	0.236 [1981 : 8]	0.028 [1980 : 3]						
9	0 [1981 : 8]		0.045 [1980 : 3]						
12	0 [1981 : 8]	0.044 [1981 : 8]	0.050 [1981 : 8]	0.017 [1981 : 8]	0 [1961 : 10]				
24	0 [1981 : 8]	0.006 [1981 : 8]	0.003 [1981 : 8]	0.003 [1981 : 8]	0 [1961 : 10]		0 [1981 : 8]		
36	0 [1981 : 8]	0 [1981 : 8]	0.003 [1981 : 8]	0.002 [1981 : 8]	0 [1961 : 10]	0 [1981 : 8]	0 [1962 : 2]		
48	0 [1981 : 8]	0 [1981 : 8]	0.001 [1981 : 8]	0.001 [1981 : 8]	0 [1961 : 10]		0 [1962 : 2]	0 [1962 : 2]	
60	0 [1981 : 8]	0 [1981 : 8]	0.002 [1981 : 8]	0.002 [1981 : 8]	0 [1961 : 10]		0 [1962 : 2]		
120	0 [1981 : 8]	0.002 [1981 : 8]	0.004 [1981 : 8]	0.002 [1981 : 8]	0 [1961 : 10]		0 [1962 : 2]	0 [1962 : 2]	0 [1981 : 8]

**Notes:** The tests were performed in a bivariate VAR comprising two bond yields. The figures reported are the smallest  $p$ -values of Andrews and Ploberger's (1994) tests for the null hypothesis of no structural break at unknown point. The test statistic is calculated as in Bernanke and Mihov (1998) imposing a trimming parameter of 0.15. The  $p$ -values are calculated using the asymptotic approximation by Hansen (1997). 0 denotes  $p$ -values below  $10^{-4}$ . Values in square brackets under the  $p$ -values indicate the date of the identified breakpoints.

**Table 8. LM test statistics: sub-periods***Panel A) 1952:01 - 1978:12 sample period*

$n/m$	1	2	3	4	6	9	12	24	60
2	0								
3	0								
4	0	0							
6	0	0	0						
9	0		0						
12	0.012	0	0	0	<b>0.352</b>				
24	0.025	<b>0.087</b>	<b>0.097</b>	<b>0.168</b>	<b>0.287</b>		0		
36	<b>0.104</b>	<b>0.204</b>	<b>0.201</b>	<b>0.240</b>	<b>0.318</b>	0.042	0.028		
48	<b>0.164</b>	<b>0.170</b>	<b>0.304</b>	<b>0.344</b>	<b>0.425</b>		<b>0.207</b>	<b>0.064</b>	
60	<b>0.233</b>	<b>0.384</b>	<b>0.347</b>	<b>0.392</b>	<b>0.497</b>		0.041		
120	<b>0.284</b>	<b>0.495</b>	<b>0.298</b>	<b>0.351</b>	<b>0.368</b>		<b>0.184</b>	0.037	0.021

*Panel B) 1982:01 - 2003:12 sample period*

$n/m$	1	2	3	4	6	9	12	24	60
2	0								
3	0								
4	0	0							
6	0	0	0						
9	0		0						
12	0	0	0	0	0				
24	0.015	0.037	0.017	0.018	0.012		0		
36	<b>0.122</b>	<b>0.214</b>	<b>0.113</b>	<b>0.124</b>	<b>0.118</b>	<b>0.102</b>	<b>0.083</b>		
48	<b>0.254</b>	<b>0.370</b>	<b>0.304</b>	<b>0.192</b>	<b>0.235</b>		0.012	0.040	
60	<b>0.383</b>	<b>0.419</b>	<b>0.470</b>	<b>0.392</b>	<b>0.417</b>		<b>0.144</b>		
120	<b>0.780</b>	<b>0.750</b>	<b>0.710</b>	<b>0.692</b>	<b>0.860</b>		<b>0.061</b>	<b>0.087</b>	<b>0.122</b>

**Notes:** The tests were performed in a bivariate VAR comprising two bond yields. The figures reported are  $p$ -values of Bekaert and Hodrick's (2001) LM tests of the null hypothesis that the EH is validated by the data for each of the possible 48 combinations of our 12 bond yields where  $n/m$  is an integer. The  $p$ -values are calculated by bootstrap as described in the text. 0 denotes  $p$ -values below  $10^{-4}$ . Figures in bold denote cases where the EH is not rejected at the five percent significance level.

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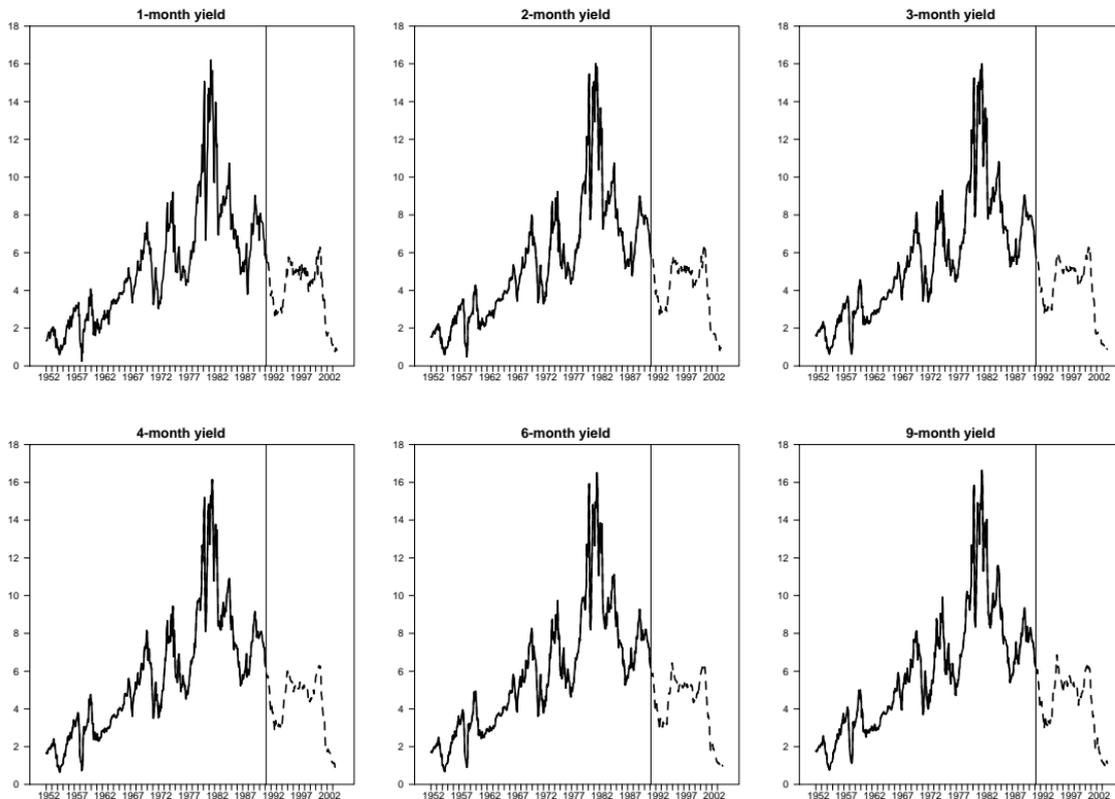
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# Figure 1. US bond yields in percentage points (continued ...)

*(boldline - McCulloch and Kwon (1993) data sample, dotted line - extended sample)*



## ... Figure 1 continued

(boldline - McCulloch and Kwon (1993) data sample, dotted line - extended sample)

