

# DISCUSSION PAPER SERIES

No. 3003

## COLLECTIVE DECISIONS WITH INTERDEPENDENT VALUATIONS

Hans Peter Grüner and Alexandra Kiel

*INTERNATIONAL MACROECONOMICS  
AND PUBLIC POLICY*



**C**entre for **E**conomic **P**olicy **R**esearch

[www.cepr.org](http://www.cepr.org)

Available online at:

[www.cepr.org/pubs/dps/DP3003.asp](http://www.cepr.org/pubs/dps/DP3003.asp)

# COLLECTIVE DECISIONS WITH INTERDEPENDENT VALUATIONS

**Hans Peter Grüner**, Universität Mannheim, IZA, Bonn, and CEPR  
**Alexandra Kiel**, Universität Mannheim

Discussion Paper No. 3003  
October 2001

Centre for Economic Policy Research  
90–98 Goswell Rd, London EC1V 7RR, UK  
Tel: (44 20) 7878 2900, Fax: (44 20) 7878 2999  
Email: [cepr@cepr.org](mailto:cepr@cepr.org), Website: [www.cepr.org](http://www.cepr.org)

This Discussion Paper is issued under the auspices of the Centre's research programme in **International Macroeconomics** and **Public Policy**. Any opinions expressed here are those of the author(s) and not those of the Centre for Economic Policy Research. Research disseminated by CEPR may include views on policy, but the Centre itself takes no institutional policy positions.

The Centre for Economic Policy Research was established in 1983 as a private educational charity, to promote independent analysis and public discussion of open economies and the relations among them. It is pluralist and non-partisan, bringing economic research to bear on the analysis of medium- and long-run policy questions. Institutional (core) finance for the Centre has been provided through major grants from the Economic and Social Research Council, under which an ESRC Resource Centre operates within CEPR; the Esmée Fairbairn Charitable Trust; and the Bank of England. These organizations do not give prior review to the Centre's publications, nor do they necessarily endorse the views expressed therein.

These Discussion Papers often represent preliminary or incomplete work, circulated to encourage discussion and comment. Citation and use of such a paper should take account of its provisional character.

Copyright: Hans Peter Grüner and Alexandra Kiel

## ABSTRACT

### Collective Decisions with Interdependent Valuations\*

Many collective decision problems have the common feature that individuals' desired outcomes are correlated but not identical. This Paper studies collective decisions with private information about these desired policies. Each agent holds private information that mainly concerns their own bliss point, but this private information also affects all other agents' bliss points. We concentrate on two specific mechanisms, the mean and the median mechanism. We establish the existence of two symmetric Bayesian Nash equilibria of the corresponding game and compare the performance of the mechanisms for different degrees of interdependencies. Applications of our framework include the assignment of voting rights in the council of the European Central Bank and the design of decision processes in teams, firms and international organizations.

JEL Classification: D78 and D82

Keywords: asymmetric information, collective decisions and interdependent valuations

Hans Peter Grüner  
Department of Economics  
University of Mannheim  
Seminargebäude A5  
D-68131 Mannheim  
GERMANY  
Tel: (49 62) 1189 1886  
Fax: (49 62) 1189 1884  
Email: hgruener@rumms.uni-mannheim.de

Alexandra Kiel  
Department of Economics  
University of Mannheim  
Seminargebäude A5  
D-68131 Mannheim  
GERMANY  
Tel: (49 62) 1181 1867  
Fax: (49 62) 1181 1884  
Email: akiel@econ.uni-mannheim.de

For further Discussion Papers by this author see:  
[www.cepr.org/pubs/new-dps/dplist.asp?authorid=144072](http://www.cepr.org/pubs/new-dps/dplist.asp?authorid=144072)

For further Discussion Papers by this author see:  
[www.cepr.org/pubs/new-dps/dplist.asp?authorid=155817](http://www.cepr.org/pubs/new-dps/dplist.asp?authorid=155817)

\* We wish to thank Roman Inderst, Benny Moldovanu and Jörg Nikutta for very valuable remarks. We also wish to thank seminar participants at Mannheim, Munich and Silvaplana for numerous comments.

Submitted 18 September 2001

# 1 Introduction

## 1.1 Decisions with public values

Many collective decision problems have in common that there is some agreement between the individuals who are supposed to take decisions as well as some disagreement. Our paper models such situations in an environment of asymmetric information by including interdependencies between individual preferences. This means that the individually preferred decision of a group member does not only depend on his own private information but also on the other members' private information. The questions are how the decision mechanism should be designed and how existing mechanisms perform when individual preferences are correlated.

We consider a specific class of collective decision problems where each of these has the following properties: In order to take a common decision, all agents obtain private information (a signal) about their most desired policy. However, no individual is perfectly informed about what would be the privately optimal policy. This imperfection is due to spillover effects between the desired policies. The information of all individuals could be used to calculate the private bliss points whereby each individuals' private information yields more information about its own bliss point than any other individual's private information. Decision problems are characterized by one single parameter which measures the extent to which private information affects all individuals.

In this setting we analyze a specific class of mechanisms. Participation is not voluntary, therefore we can ignore any individual rationality constraints. Moreover, our mechanisms do not condition monetary transfers on the agents' announcements, in fact all monetary transfers are ruled out a-priori. Instead, the mechanisms map individual announcements of the private information into the collective decision.

We concentrate on two mechanisms, i.e. the median and the mean mechanism. The median mechanism implements the median announcement, whereas the mean mechanism implements the average of all announcements. The main difference between these two mechanisms is how they deal with the announcements of private information. Under the median mechanism changes in extreme positions are disregarded, since the median alone determines the final decision. On the contrary, the nature of the mean mechanism is to take all available information into account. Therefore, under the mean mechanism extreme positions influence the decision.

The main result of this paper is the identification of two symmetric Bayesian Nash equilibria of the respective games. The performance of the mechanisms depends upon the extent to which spillover effects affect the economy. With weak interdependencies, the median mechanism dominates the mean mechanism, whereas with strong interdependencies it is optimal to use the average as decision mechanism.

## 1.2 Some applications

One can think of a number of different applications of our framework: Any setting in which the individually preferred decision does not only depend on the agents' own private information but as well on the signals of the others fits well into this framework.

One important example may be the decision process in a common central bank like the European Central Bank (ECB). Here, national central banks may care about a policy that accommodates macroeconomic shocks in their own country while taking a collective decision about common monetary policy. However, due to demand spillover effects, shocks in one country may affect the desired policy in other participating countries. Moreover, it is likely that national central bankers have some private information about their national macroeconomic conditions. If interdependencies are

strong, the other central bankers' information is very important for the nationally desired policy. These aspects are the more important the closer any EU-enlargement, because on this occasion a discussion about structure and organization of the ESCB, the ECB and its council will become unavoidable to guarantee future functioning. The existing literature on decision making in this context focuses either on monetary stabilization policies comparing alternative types of appointees (i.e. having different mandates) in the ECB council (e.g. Von Hagen and Süppel [1994]), on the implications of different policy objectives of the common central bank (e.g. Gros and Hefeker [2000] and Grüner [1999]) or on equilibrium incentive contracts in a multi-principal agency framework (e.g. Dixit and Jensen [2000]). Instead, we ask how the decision mechanism of the ECB (inflation as a function of announced shocks) should be designed in order to maximize the sum of (expected) utilities. Our result translates to this context in the following way: the larger the common component between member states, i.e. the more national macroeconomic shocks affect all members of the union, the more weight should be given to extreme positions in the ECB council.

Besides decision making in the ECB council, our setting can be applied for example to international decisions about environmental policy. Basically, the nation states are interested in achieving less pollution in their own country. On the other hand, they have to take a common decision about certain environmental standards. In addition, it may be the case that national governments possess private information about the national amount of emissions, the costs to reduce emissions or the economic consequences of a reduction. However, the environmental situation in one member state is co-determined by the emissions in the neighboring countries. The nearer the location of countries, the more important becomes private information obtained in any single country. Take as a recent example the negotiations about a common European standard of reduction in  $CO_2$  emissions in preparation for the Kyoto Protocol.

Collective decision problems having the features described above can be found also

in many areas besides politics. Consider the following example taken from industrial organization: a decision about the future orientation of a firm has to be made. This decision has to be taken by the different heads of department. First of all, these heads are interested in the performance of their own department. Beside this, they possess specific knowledge about the conditions, needs or prospects of it. However, their opinion about the future development of the firm is influenced by the conditions obtaining in other departments as well.

### 1.3 Relation to literature

The mechanism design literature offers solutions to related problems, but none to our specific setting. If there are no spillovers and side-payments are allowed it is always possible to obtain (Bayesian) incentive-compatibility using an expected externality mechanism.<sup>1</sup> If informational and allocational externalities are considered but monetary transfers are allowed, the problem of efficient design has been analyzed in auction environments.<sup>2</sup> Instead, we study the case where spillovers are present and monetary transfers are excluded a priori.

Concerning the analysis of collective decisions, the setting of our paper builds an intermediate case between two frameworks commonly used in the literature: On one hand, political outcomes under individual utility maximization are analyzed, i.e. the case of zero spillovers (see Vaubel and Willet [1991] and the references therein). On the other hand, the literature deals with efficient aggregation of perfectly coordinated interests, i.e. 100% spillovers (see Piketty [1999] and the references therein). Our research focuses on the intermediate case: what kind of political outcomes under

---

<sup>1</sup>See Mas-Colell, Whinston and Green [1995] and Arrow [1979] or D'Aspremont and Gérard-Varet [1979].

<sup>2</sup>See for example Fieseler, Kittsteiner and Moldovanu [2000] or Jehiel and Moldovanu [1998].

different information aggregation mechanisms are to be expected if individual interests are correlated to a certain extent? Thus, we do not analyze political outcomes for a fixed degree of spillovers, but instead vary the extent to which individual preferences influence each other.

Related to our work is a recent paper by Casella [2000]. In a similar informational environment but with private values she proposes a simple voting scheme for deliberations taken by committees that meet regularly over time. At each meeting, committee members are allowed to store their vote for future use. Although the scheme cannot achieve the first best with more than two voters, making votes storable typically leads to ex ante welfare gains. Her paper differs from ours in that we do not consider developments over time. Instead, we study a one-shot game excluding also any reputation effects a priori.

The remainder of this paper is organized as follows: Section 2 introduces the model presenting the first-best solution and the two mechanisms we aim to study. The respective equilibria under those mechanisms are calculated in Section 3 where results about the truthful revelation properties of the equilibria are given as well. The next section compares the performance of the mean and the median mechanism for different degrees of interdependencies. Section 5 concludes. All omitted proofs can be found in the Appendix.

## 2 The Model

We consider an economy which is populated by  $i = 1, 2, 3$  individuals. A decision  $x \in \mathbb{R}$  has to be taken. Each individual receives private information  $\theta_i$ . The parameters  $\theta_i$  are distributed independently and uniformly over the support  $[-1, 1]$ . The vector of private information is  $\theta$ . An individual's preferences over outcomes are characterized



by the following von-Neumann-Morgenstern utility function

$$u_i(x, \theta) = -(x - \theta_i^*)^2 \quad (1)$$

where  $\theta_i^*$  describes the individually preferred decision. Individual utility is maximized at  $x = \theta_i^*$  (i.e. when the individually preferred decision is actually implemented). The highest attainable utility is zero. The larger the difference between the implemented policy  $x$  and the individually preferred decision  $\theta_i^*$ , the smaller is individual utility. The individually preferred policy  $\theta_i^*$  is a convex combination of  $i$ 's type and the average of all others' types, i.e.

$$\theta_i^* = (1 - \alpha) \theta_i + \frac{\alpha}{2} \sum_{j \neq i} \theta_j. \quad (2)$$

The parameter  $\alpha \in [0, \bar{\alpha}]$  measures the extent to which interdependencies align the preferences of all individuals. For the upper bound value  $\bar{\alpha} := \frac{2}{3}$  all individuals share a common utility function with a maximum at  $x = \theta_{Mean}$  where  $\theta_{Mean} = \sum_{i=1}^3 \theta_i / 3$ . For the lower bound  $\alpha = 0$  each individual has his signal  $\theta_i$  as a private bliss point. For example,  $\alpha$  might measure the degree of demand spillover effects between the members of the European Union, closeness of geographical location or the degree to which firm departments are interlinked.

## 2.1 Welfare

First, we describe the decision that maximizes welfare, when there are no informational asymmetries. Welfare is defined as the sum of individual utilities, i.e. we take an utilitarian perspective to welfare. It turns out that this decision  $x^*$  is independent of the degree of interdependency  $\alpha$  and is determined by the average of all private signals.

**Lemma 1** *The sum of all utilities is maximized at  $x^* = \theta_{Mean}$ .*

PROOF: See Appendix.

The intuition for this result is that by summing up the utilities of all individuals any spillover effects are automatically taken into account. Lemma 1 implies that the mean mechanism would yield the first best if truth-telling could be implemented for all degrees of interdependency. However, if informational asymmetries are present, this first-best solution remains no longer attainable.

## 2.2 The mechanisms

We consider the following two direct mechanisms excluding any monetary transfers and ignoring participation constraints: All individuals are asked for an announcement  $\hat{\theta}_i \in \mathbb{R}$  of their private signal. The vector of announcements is  $\hat{\theta}$ . Depending on these announcements the collective decision  $x$  is taken.

The first mechanism we study is the median mechanism. Let  $x_{Median} = x_{Median}(\hat{\theta}) := \hat{\theta}_{Median}$ , where  $\hat{\theta}_{Median}$  is the median of all announcements.<sup>3</sup> The median mechanism implements this announcement and thus replicates majority decisions for the case of zero spillovers. Another feature of this mechanism is that changes in extreme positions are disregarded, since the final decision solely depends on the median announcement.

The second mechanism we analyze is the mean mechanism. Let  $x_{Mean} = x_{Mean}(\hat{\theta}) := \frac{1}{3} \sum_{i=1}^3 \hat{\theta}_i(\theta_i)$ . This mechanism asks the individuals for their private information and implements the average of all announcements. Consequently, the mean mechanism uses all available information and thus extreme positions influence the common decision.

---

<sup>3</sup>Let  $\theta_{Median}$  denote the signal of the median individual. Note that in general  $\theta_{Median} = \hat{\theta}_{Median}$  is not true.

### 3 The Results

In this section, we present two Bayesian Nash equilibria of the games introduced above, one of the median and one of the mean mechanism. These equilibria imply truthful revelation for certain degrees of interdependencies.

#### 3.1 Equilibria

**Proposition 1** *The median mechanism has a symmetric Bayesian Nash equilibrium. The equilibrium strategy is  $\hat{\theta}_i(\theta_i) = (1 - \frac{1}{2}\alpha) \theta_i$ .*

PROOF OF PROPOSITION 1:

Without loss of generality consider individual 2's best response to linear equilibrium strategies  $\hat{\theta}_i(\theta_i) = a\theta_i$ ,  $i = 1, 3$ . Individual 2 maximizes its expected utility under the median mechanism if  $\hat{\theta}_2(\theta_2)$  maximizes

$$E\left(\hat{\theta}_2\right) := E\left[-(x_{Median} - \theta_2^*)^2\right]. \quad (3)$$

This expected utility can be decomposed into three parts in the following way:  $E\left(\hat{\theta}_2\right) = E_1\left(\hat{\theta}_2\right) + E_2\left(\hat{\theta}_2\right) + E_3\left(\hat{\theta}_2\right)$ . The first part  $E_1\left(\hat{\theta}_2\right)$  describes the situation in which the announcement of individual 2 is neither the highest nor the lowest announcement, i.e.  $\hat{\theta}_2 = \hat{\theta}_{Median}$ . Individual 2's announcement is then implemented according to the mechanism, i.e.  $x_{Median} = \hat{\theta}_2$ . The second part  $E_2\left(\hat{\theta}_2\right)$  describes the case in which the announcements of the two other agents are both below the announcement of individual 2, and the third  $E_3\left(\hat{\theta}_2\right)$  the case in which they are both above, respectively. We analyze these three cases in turn.

Consider first the situation in which the announcement of individual 2 is the median announcement. This happens if either  $\hat{\theta}_1 < \hat{\theta}_2 < \hat{\theta}_3$  or  $\hat{\theta}_3 < \hat{\theta}_2 < \hat{\theta}_1$ . Since these two cases are symmetric concerning individual 2's expected utility, assume without

loss of generality  $\hat{\theta}_1 < \hat{\theta}_2 < \hat{\theta}_3$  and multiply the resulting part of expected utility by

2. The corresponding component is then given by

$$E_1(\hat{\theta}_2) = -\frac{1}{2} \int_{-1}^{\frac{\hat{\theta}_2}{a}} \int_{\frac{\hat{\theta}_2}{a}}^1 \left( \hat{\theta}_2 - (1 - \alpha)\theta_2 - \frac{\alpha}{2}(\theta_1 + \theta_3) \right)^2 d\theta_3 d\theta_1. \quad (4)$$

Next, take the case in which the announcements of both other agents are below the announcement of individual 2, i.e. if either  $\hat{\theta}_1 < \hat{\theta}_3 < \hat{\theta}_2$  or  $\hat{\theta}_3 < \hat{\theta}_1 < \hat{\theta}_2$ . Again, these two cases are symmetric. Assume without loss of generality  $\hat{\theta}_1 < \hat{\theta}_3 < \hat{\theta}_2$  and multiply the resulting part by 2. This situation yields

$$E_2(\hat{\theta}_2) = -\frac{1}{2} \int_{-1}^{\frac{\hat{\theta}_2}{a}} \int_{\theta_1}^{\frac{\hat{\theta}_2}{a}} \left( a\theta_3 - (1 - \alpha)\theta_2 - \frac{\alpha}{2}(\theta_1 + \theta_3) \right)^2 d\theta_3 d\theta_1. \quad (5)$$

Finally, consider the situation in which the announcements of the two other agents are both above the announcement of individual 2, i.e. if either  $\hat{\theta}_2 < \hat{\theta}_1 < \hat{\theta}_3$  or  $\hat{\theta}_2 < \hat{\theta}_3 < \hat{\theta}_1$ . These two cases are symmetric as well. Thus, assume without loss of generality  $\hat{\theta}_2 < \hat{\theta}_1 < \hat{\theta}_3$  and multiply the resulting part by 2. The corresponding component of expected utility is given by

$$E_3(\hat{\theta}_2) = -\frac{1}{2} \int_{\frac{\hat{\theta}_2}{a}}^1 \int_{\theta_1}^1 \left( a\theta_1 - (1 - \alpha)\theta_2 - \frac{\alpha}{2}(\theta_1 + \theta_3) \right)^2 d\theta_3 d\theta_1. \quad (6)$$

Taking all three parts together and differentiating with respect to  $\hat{\theta}_2$  yields

$$\begin{aligned} & \frac{d(E[-(x_{Median} - \theta_2^*)^2])}{d\hat{\theta}_2} \\ &= (\hat{\theta}_2 - a)(\hat{\theta}_2 + a) \frac{2a\hat{\theta}_2 - \alpha\hat{\theta}_2 + 2\alpha a\theta_2 - 2a\theta_2}{2a^3}. \end{aligned} \quad (7)$$

An interior solution to this maximization problem requires

$$\frac{d(E[-(x_{Median} - \theta_2^*)^2])}{d\hat{\theta}_2} = 0.$$

The three solutions to this equation are given by

$$\begin{aligned}\hat{\theta}_{2,1} &= -a, \\ \hat{\theta}_{2,2} &= 2a \frac{\alpha - 1}{\alpha - 2a} \theta_2,\end{aligned}\tag{8}$$

and

$$\hat{\theta}_{2,3} = a.$$

Note that for announcements  $\hat{\theta}_2$  above  $a$  and below  $-a$  expected utility for individual 2 is not longer given by  $E_1(\hat{\theta}_2) + E_2(\hat{\theta}_2) + E_3(\hat{\theta}_2)$ . In case of individuals 1 and 3 announcing according to  $\hat{\theta}_i(\theta_i) = a\theta_i$ , the announcement  $\hat{\theta}_2$  is never the median announcement for  $\hat{\theta}_2 > a$  and  $\hat{\theta}_2 < -a$ . Then, individual 2's expected utility is constant. For  $\hat{\theta}_2 > a$ , it is given by

$$E_2(a) = -\frac{1}{2} \int_{-1}^1 \int_{\theta_1}^1 \left( a\theta_3 - (1 - \alpha)\theta_2 - \frac{\alpha}{2}(\theta_1 + \theta_3) \right)^2 d\theta_3 d\theta_1 \tag{9}$$

and for  $\hat{\theta}_2 < -a$  by

$$E_3(-a) = -\frac{1}{2} \int_{-1}^1 \int_{\theta_1}^1 \left( a\theta_1 - (1 - \alpha)\theta_2 - \frac{\alpha}{2}(\theta_1 + \theta_3) \right)^2 d\theta_3 d\theta_1. \tag{10}$$

We now return to the three possible equilibria described by (8). Since we are interested in equilibrium strategies that are linear in  $\theta_2$  we start the further analysis with concentrating on  $\hat{\theta}_{2,2}$ . In order to determine the factor  $a$  one has to solve

$$a = 2a \frac{\alpha - 1}{\alpha - 2a} \tag{11}$$

which gives the two solutions

$$\begin{aligned}a_1 &= 0 \\ a_2 &= 1 - \frac{1}{2}\alpha.\end{aligned}\tag{12}$$

Again, since we are looking for an equilibrium with linear announcement strategies<sup>4</sup>, we concentrate on  $a_2 = 1 - \frac{1}{2}\alpha =: \tilde{a}$ . For this specific linear factor two observations can be made:

(i)  $\tilde{a} > 0$  for  $\alpha \in [0, \bar{\alpha}]$  and

(ii)  $\hat{\theta}_{2,1} \leq \hat{\theta}_{2,2} \leq \hat{\theta}_{2,3}$ , since  $\hat{\theta}_{2,2} = (1 - \frac{1}{2}\alpha)\theta_2$  for  $\tilde{a}$  and  $\theta_2 \in [-1, 1]$ .

It remains to show that  $\hat{\theta}_{2,2}$  indeed yields a maximum of individual announcement behavior for  $\tilde{a}$ . Consider the first derivative (7) and define

$$f(\hat{\theta}_2) := \frac{2\tilde{a}\hat{\theta}_2 - \alpha\hat{\theta}_2 + 2\alpha\tilde{a}\theta_2 - 2\tilde{a}\theta_2}{2\tilde{a}^3} \quad (13)$$

and

$$g(\hat{\theta}_2) := (\hat{\theta}_2 - \tilde{a})(\hat{\theta}_2 + \tilde{a}). \quad (14)$$

In order to check the second order condition we consider  $f$  and  $g$  in turn. It holds that

$$f(\hat{\theta}_{2,2}) = 0, \quad (15)$$

$$f'(\hat{\theta}_2) = \frac{2\tilde{a} - \alpha}{2\tilde{a}^3} > 0 \quad (16)$$

and for  $\alpha \in [0, \bar{\alpha}]$  and  $\theta_2 \in [-1, 1]$ ,

$$g(\hat{\theta}_{2,2}) = \left( \left( 1 - \frac{1}{2}\alpha \right) \theta_2 \right)^2 - \left( 1 - \frac{1}{2}\alpha \right)^2 < 0. \quad (17)$$

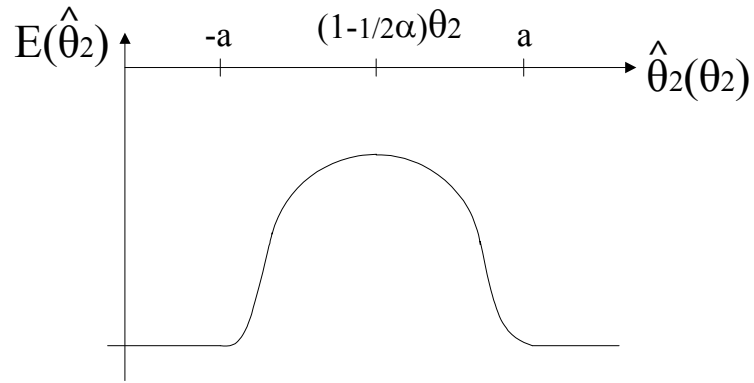
---

<sup>4</sup>Compare also Proposition 2.

The second derivative at  $\hat{\theta}_2 = \hat{\theta}_{2,2}$  is given by

$$\begin{aligned}
& \left. \frac{d \left( E \left[ - \left( x_{Median} - \theta_2^* \right)^2 \right] \right)^2}{d^2 \hat{\theta}_2} \right|_{\hat{\theta}_2 = \hat{\theta}_{2,2}} & (18) \\
& = g'(\hat{\theta}_{2,2})f(\hat{\theta}_{2,2}) + f'(\hat{\theta}_{2,2})g(\hat{\theta}_{2,2}) \\
& = f'(\hat{\theta}_{2,2})g(\hat{\theta}_{2,2}) \\
& < 0.
\end{aligned}$$

Note that a similar argument shows that  $\hat{\theta}_{2,1}$  and  $\hat{\theta}_{2,3}$  indeed yield minima of individual 2's expected utility for  $\tilde{a}$ . The following (simplified) picture shows individual 2's expected utility as a function of its announcement.



Hence, given that individuals 1 and 3 announce according to  $\hat{\theta}_i(\theta_i) = \tilde{a}\theta_i$ ,  $\tilde{a} = 1 - \frac{1}{2}\alpha$ , the strategy

$$\hat{\theta}_2(\theta_2) = \left( 1 - \frac{1}{2}\alpha \right) \theta_2 \quad (19)$$

is a best reply. Q.E.D.

Under the median mechanism individuals understate their private information. With increasing degrees of interdependency (larger  $\alpha$ ) the private signal becomes less valuable. Since individuals know that the median of all announcements will be implemented, they try to profit from the others' information. Their announcement is

closer to zero than their true signal due to the fact that zero is the expected value of the information parameters.

**Proposition 2** *i) There exists a continuum of other symmetric equilibria under the median mechanism in which all individuals announce the same type irrespective of their signal, i.e.  $\hat{\theta}_i(\theta_i) = \tilde{\theta} \forall i$ . ii) All those equilibria yield lesser expected utility for all individuals than  $\hat{\theta}_i(\theta_i) = (1 - \frac{1}{2}\alpha) \theta_i$ .*

PROOF: See Appendix.

In the following, we concentrate on equilibrium strategies  $\hat{\theta}_i(\theta_i) = (1 - \frac{1}{2}\alpha) \theta_i \forall i$ , because this equilibrium yields at least the same expected payoff than the other equilibria.

We obtain another linear equilibrium strategy for the mean mechanism. According to this strategy individuals overstate their private information.

**Proposition 3** *The mean mechanism has a symmetric Bayesian Nash equilibrium. The equilibrium strategy is  $\hat{\theta}_i(\theta_i) = 3(1 - \alpha) \theta_i$ .*

PROOF OF PROPOSITION 3:

Consider individual  $i$ 's best response to the equilibrium strategy. Individual  $i$  maximizes its expected utility if  $\hat{\theta}_i(\theta_i)$  maximizes

$$E \left[ - (x_{Mean} - \theta_i^*)^2 \right] = E \left[ - \left( \frac{\sum_{j=1}^3 \hat{\theta}_j(\theta_j)}{3} - \theta_i^* \right)^2 \right]. \quad (20)$$

Substituting for  $\theta_i^*$  yields

$$\max_{\hat{\theta}_i(\theta_i)} E \left[ - \left( \frac{\sum_{j=1}^3 \hat{\theta}_j(\theta_j)}{3} - (1 - \alpha) \theta_i - \frac{\alpha}{2} \sum_{j \neq i} \theta_j \right)^2 \right] \quad (21)$$

$$\max_{\hat{\theta}_i(\theta_i)} E \left[ - \left( \frac{\hat{\theta}_i(\theta_i)}{3} - (1 - \alpha) \theta_i + \frac{\sum_{j \neq i}^3 \hat{\theta}_j(\theta_j)}{3} - \frac{\alpha}{2} \sum_{j \neq i} \theta_j \right)^2 \right] \quad (22)$$



$$\begin{aligned}
& \max_{\hat{\theta}_i(\theta_i)} -E \left[ \frac{1}{9} \hat{\theta}_i(\theta_i)^2 \right] \\
& -2E \left[ \left( \frac{1}{3} \hat{\theta}_i(\theta_i) \right) \left( -(1-\alpha)\theta_i + \frac{\sum_{j=1, j \neq i}^3 \hat{\theta}_j(\theta_j)}{3} - \frac{\alpha}{2} \sum_{j \neq i} \theta_j \right) \right] \\
& -E \left[ \left( -(1-\alpha)\theta_i + \frac{\sum_{j=1, j \neq i}^3 \hat{\theta}_j(\theta_j)}{3} - \frac{\alpha}{2} \sum_{j \neq i} \theta_j \right)^2 \right].
\end{aligned} \tag{23}$$

Using the fact that  $\theta_j$  and  $\hat{\theta}_j(\theta_j)$  have an expected value of zero and that expectations are taken over all  $j \neq i$ , we get

$$\begin{aligned}
& \max_{\hat{\theta}_i(\theta_i)} -\frac{1}{9} \hat{\theta}_i(\theta_i)^2 - 2 \left( \frac{1}{3} \hat{\theta}_i(\theta_i) \right) (-(1-\alpha)\theta_i) \\
& -E \left[ \left( -(1-\alpha)\theta_i + \frac{\sum_{j=1, j \neq i}^3 \hat{\theta}_j(\theta_j)}{3} + \frac{\alpha}{2} \sum_{j \neq i} \theta_j \right)^2 \right].
\end{aligned} \tag{24}$$

Optimality requires

$$-\frac{2}{9} \hat{\theta}_i(\theta_i) - \frac{2}{3} (-(1-\alpha)\theta_i) = 0 \tag{25}$$

and thus,

$$\hat{\theta}_i(\theta_i) = 3(1-\alpha)\theta_i. \tag{26}$$

Q.E.D.

Under the mean mechanism individuals exaggerate their private signal in order to cancel out the average taking implied by the mean mechanism. With increasing degrees of interdependency this behavior becomes counterproductive and announcements approach the true signal.<sup>5</sup>

Although it may seem at first sight that both equilibrium strategies are independent of the underlying distribution of information parameters, this indeed is not the case and due to the specification of individual utility.

Using the above calculated equilibrium strategies, it follows that

**Corollary 1** *The median mechanism has a symmetric Bayesian Nash equilibrium in which agents announce their type truthfully if  $\alpha = 0$ .*

**Corollary 2** *The mean mechanism has a symmetric Bayesian Nash equilibrium in which agents announce their type truthfully if  $\alpha = \bar{\alpha} = \frac{2}{3}$ .*

## 4 Comparison of mean and median mechanism

We start the comparison by analyzing the properties of the two mechanisms at the corner values of  $\alpha$ , i.e. at  $\alpha = 0$  and at  $\alpha = \bar{\alpha}$ .

**Proposition 4** *For  $\alpha = 0$  the median mechanism yields a better result than the mean mechanism.*

PROOF: See Appendix.

We know that individuals reveal their type truthfully for  $\alpha = 0$  under the median mechanism (Corollary 1), but not under the mean mechanism. This yields a better result in terms of payoff than exaggeration as implied by the mean mechanism.

---

<sup>5</sup>This result extends to the case of  $n$  individuals. Then, the equilibrium strategy under the mean mechanism is given by  $\hat{\theta}_i(\theta_i) = n(1 - \alpha)\theta_i$ .

Note that the median mechanism does not implement the first-best in general, since the first-best would only be implemented if the private information of the median individual by instance is equal to the average of all types.

**Proposition 5** *For  $\alpha = \bar{\alpha}$  it holds that (i) the mean mechanism yields the first-best and (ii) the median mechanism does not yield the first-best.*

PROOF: See Appendix.

The intuition for this result is as follows: for  $\alpha = \bar{\alpha}$  individuals announce their type truthfully under the mean mechanism (Corollary 2) and we know already that the first-best solution is the average of all types (Lemma 1). This yields part (i). However, the median mechanism does neither imply truth-telling for  $\alpha = \bar{\alpha}$  nor implement the average. Thus, it does not yield the first best.

Now, we turn to the behavior of the sum of expected utilities under both mechanisms for intermediate values of  $\alpha$ .

**Lemma 2** *Consider the median mechanism. The sum of expected utilities is (i) continuous in  $\alpha$ , (ii) strictly increasing in  $\alpha$  and (iii) attains its maximum at  $\alpha = \bar{\alpha}$ .*

PROOF: See Appendix.

**Lemma 3** *Consider the mean mechanism. The sum of expected utilities is (i) continuous in  $\alpha$ , (ii) strictly increasing in  $\alpha$  and (iii) attains its maximum at  $\alpha = \bar{\alpha}$ .*

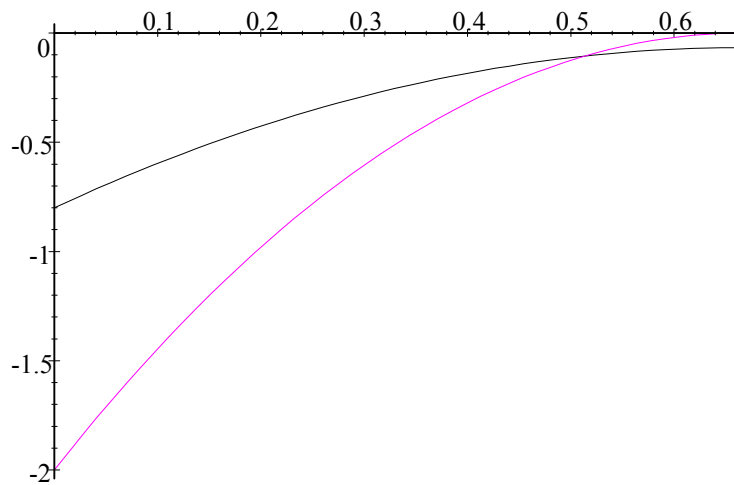
PROOF: See Appendix.

From Propositions 4 and 5 and Lemmata 2 and 3 we know that there exists an  $\alpha_1$  below which the median yields a better result than the mean mechanism and that there exists an  $\alpha_2$  above which the mean is better than the median mechanism. Our main result concerning the comparison between the median and the mean mechanism shows that these two points coincide, i.e.  $\alpha_1 = \alpha_2$ .

**Proposition 6** (i) *There exists an  $\alpha^*$  below which the median is better than the mean mechanism and above which the mean is better than the median mechanism and (ii)  $\alpha^* = \frac{2}{3} - \frac{2}{57}\sqrt{19}$ .*

PROOF: See Appendix.

The following picture shows the sum of expected utilities under the mean and the median mechanism with a unique point of intersection at  $\alpha^*$ :



If individual preferences are strongly correlated, then making all agents participate in the decision is better than restricting entry into the decision process. If there is only a small common component then it is better to use the median mechanism. The intuition is that for weak interdependencies the equilibrium strategy under the median mechanism implies announcement behavior close to truth telling whereas the equilibrium strategy under the mean mechanism leads to strong exaggeration of private information. Therefore, average taking is outperformed by ignoring some of the information available. Since the degree to which  $\alpha$  influences untruthful announcement behavior is stronger under the mean mechanism, this intuition holds for a wide range of interdependencies, only for very high degrees it is reversed.

## 5 Conclusion

The problem analyzed in this paper is one of collective decision taking. If the individuals who are supposed to take a common decision are asymmetrically informed and if there are interdependencies between the individually desired policies, how should a decision mechanism be designed that maximizes the sum of expected utilities? Our analysis of this problem concentrates on two specific mechanisms, i.e. the median and the mean mechanism, and obtains the following: Under the median mechanism individuals understate their private information, whereas under the mean mechanism they overstate it. As a result, the median mechanism performs better than the mean mechanism in terms of expected utility maximization for a wide range of weak interdependencies. Only for very high degrees of interdependency is this mechanism outperformed by the mean mechanism. The median mechanism replicates decisions taken by majority rule and this rule can be observed frequently in reality. Therefore, our results are encouraging because they suggest that the median mechanism is a good mechanism to take collective decisions - even if there are spillovers between individually desired policies.

Returning to our primary example, the decision process in a common central bank like the ECB, we can conclude that decision taking by majority rule (as done in the ECB council) performs better than taking the average. Disregarding extreme positions - as does the median mechanism - seems to be favorable as long as participating countries differ in the economic conditions they face. Only if the member states experience a very similar economic environment, it would be better to change the decision mechanism and use the average of announcements as a common policy.

Starting from our research there are four directions to proceed. The first extension is the analysis for larger  $n$ . For the mean mechanism all results obtained hold for  $n > 3$ , but for the median mechanism this is not obvious. Once there are results

for the median mechanism as well, one could introduce a class of mechanisms which relates the outcome to the average of some agents' announcements about their private information. This class includes the median and the mean mechanism as special cases.

Second, in this paper we abstracted from any individual rationality considerations, since in many collective decisions participation is not voluntary. However, if we take participation constraints into account, the traditional solution would prescribe an outside option to be implemented when an individual opts out. This in turn leads to changed interim individual behavior and to different equilibrium outcomes - with the status quo maintaining in many instances. But in our setting - due to interdependent valuations - even individuals not participating in the mechanism would be affected by the collective decision. This would imply that one has to endogenize the participation constraint (following Jehiel, Moldovanu and Stacchetti [1996]).

Third, in a modified two-stage game the issue of pre-vote communication may be analyzed. The question is if an improvement upon the equilibria of the original game is possible when people are allowed to communicate before they have to vote. It is well known that equilibrium behavior can be affected if agents have the opportunity to exchange information prior to playing some game (see Crawford and Sobel [1982]). Our intuition is that such an improvement is not possible in our framework.

Finally, another question we did not address is the design of an optimal mechanism for the class of collective decision problems studied. This would mean to find a mechanism that implements the first-best for all degrees of spillovers, not only for the maximum amount.

## 6 Appendix - Proofs

PROOF OF LEMMA 1:

The sum of all utilities is maximized if  $x^*$  maximizes

$$\sum_{i=1}^3 u_i(x, \theta) = \sum_{i=1}^3 -(x - \theta_i^*)^2. \quad (27)$$

Optimality requires

$$-\sum_{i=1}^3 2(x^* - \theta_i^*) = 0 \quad (28)$$

$\Leftrightarrow$

$$\begin{aligned} x^* &= \frac{1}{3} \sum_{i=1}^3 \theta_i^* & (29) \\ &= \frac{1}{3} \sum_{i=1}^3 \left( (1 - \alpha)\theta_i + \frac{\alpha}{2} \sum_{j \neq i} \theta_j \right) \\ &= \frac{1}{3} \left( (1 - \alpha) \sum_{i=1}^3 \theta_i + \frac{\alpha}{2} \sum_{i=1}^3 \sum_{j \neq i} \theta_j \right) \\ &= \frac{1}{3} \sum_{i=1}^3 \theta_i \\ &= \theta_{Mean}. \end{aligned}$$

Q.E.D.

PROOF OF PROPOSITION 2:

*i*) EXISTENCE: Assume without loss of generality that individuals 1 and 2 announce according to  $\hat{\theta}_i(\theta_i) = \tilde{\theta}$ ,  $i = 1, 2$ . That being so, it is a best reply for individual 3 to announce  $\tilde{\theta}$  as well, since on no account its announcement will change the implemented decision under the median mechanism.

ii) If agents announce  $\hat{\theta}_i(\theta_i) = (1 - \frac{1}{2}\alpha)\theta_i$  then  $x_{Median} = (1 - \frac{1}{2}\alpha)\theta_{Median}$ . Consider without loss of generality expected utility for individual 2. This is given by

$$\begin{aligned}
& E \left[ - (x_{Median} - \theta_2^*)^2 \right] \\
&= -\frac{1}{4} \int_{-1}^1 \int_{-1}^{\theta_2} \int_{\theta_2}^1 \left( \left(1 - \frac{1}{2}\alpha\right) \theta_2 - (1 - \alpha) \theta_2 - \frac{\alpha}{2} (\theta_1 + \theta_3) \right)^2 d\theta_3 d\theta_1 d\theta_2 \\
&\quad -\frac{1}{4} \int_{-1}^1 \int_{-1}^{\theta_2} \int_{\theta_1}^{\theta_2} \left( \left(1 - \frac{1}{2}\alpha\right) \theta_3 - (1 - \alpha) \theta_2 - \frac{\alpha}{2} (\theta_1 + \theta_3) \right)^2 d\theta_3 d\theta_1 d\theta_2 \\
&\quad -\frac{1}{4} \int_{-1}^1 \int_{\theta_2}^1 \int_{\theta_1}^1 \left( \left(1 - \frac{1}{2}\alpha\right) \theta_1 - (1 - \alpha) \theta_2 - \frac{\alpha}{2} (\theta_1 + \theta_3) \right)^2 d\theta_3 d\theta_1 d\theta_2 \\
&= -\frac{11}{20}\alpha^2 + \frac{11}{15}\alpha - \frac{4}{15}. \tag{30}
\end{aligned}$$

If agents announce  $\hat{\theta}_i(\theta_i) = \tilde{\theta}$  then  $x_{Median} = \tilde{\theta}$ . Again, consider expected utility for individual 2:

$$\begin{aligned}
& E \left[ - (x_{Median} - \theta_2^*)^2 \right] \\
&= -\frac{1}{4} \int_{-1}^1 \int_{-1}^{\tilde{\theta}} \int_{\tilde{\theta}}^1 \left( \tilde{\theta} - (1 - \alpha) \theta_2 - \frac{\alpha}{2} (\theta_1 + \theta_3) \right)^2 d\theta_3 d\theta_1 d\theta_2 \\
&\quad -\frac{1}{4} \int_{-1}^1 \int_{-1}^{\tilde{\theta}} \int_{\theta_1}^{\tilde{\theta}} \left( \tilde{\theta} - (1 - \alpha) \theta_2 - \frac{\alpha}{2} (\theta_1 + \theta_3) \right)^2 d\theta_3 d\theta_1 d\theta_2 \\
&\quad -\frac{1}{4} \int_{-1}^1 \int_{\tilde{\theta}}^1 \int_{\theta_1}^1 \left( \tilde{\theta} - (1 - \alpha) \theta_2 - \frac{\alpha}{2} (\theta_1 + \theta_3) \right)^2 d\theta_3 d\theta_1 d\theta_2 \\
&= -\frac{1}{2}\alpha^2 + \frac{2}{3}\alpha - \frac{1}{3} - \tilde{\theta}^2. \tag{31}
\end{aligned}$$

Since  $\tilde{\theta}^2 > 0$ , it suffices to show that

$$-\frac{1}{2}\alpha^2 + \frac{2}{3}\alpha - \frac{1}{3} < -\frac{11}{20}\alpha^2 + \frac{11}{15}\alpha - \frac{4}{15} \tag{32}$$

which is true  $\forall \alpha \in [0, \bar{\alpha}]$ . Q.E.D.



PROOF OF PROPOSITION 4:

For  $\alpha = 0$ , the sum of expected utilities under the mean mechanism is given by

$$\begin{aligned}
& \sum_{i=1}^3 E \left[ -(x_{Mean} - \theta_i^*)^2 \right] \\
&= -\frac{3}{8} \int_{-1}^1 \int_{-1}^1 \int_{-1}^1 (\theta_1 + \theta_2 + \theta_3 - \theta_1)^2 d\theta_1 d\theta_2 d\theta_3 \\
&= -2
\end{aligned} \tag{33}$$

and under the median mechanism by

$$\begin{aligned}
& \sum_{i=1}^3 E \left[ -(x_{Median} - \theta_2^*)^2 \right] \\
&= -\frac{3}{4} \int_{-1}^1 \int_{-1}^{\theta_2} \int_{\theta_2}^1 (\theta_2 - \theta_2)^2 d\theta_3 d\theta_1 d\theta_2 \\
&\quad -\frac{3}{4} \int_{-1}^1 \int_{-1}^{\theta_2} \int_{\theta_1}^{\theta_2} (\theta_3 - \theta_2)^2 d\theta_3 d\theta_1 d\theta_2 \\
&\quad -\frac{3}{4} \int_{-1}^1 \int_{\theta_2}^1 \int_{\theta_1}^1 (\theta_1 - \theta_2)^2 d\theta_3 d\theta_1 d\theta_2 \\
&= -\frac{4}{5}.
\end{aligned} \tag{34}$$

Hence,

$$\sum_{i=1}^3 E \left[ -(x_{Mean} - \theta_i^*)^2 \right] < \sum_{i=1}^3 E \left[ -(x_{Median} - \theta_2^*)^2 \right]. \tag{35}$$

Q.E.D.

PROOF OF PROPOSITION 5:

(i) It suffices to verify that truthful announcing is a Bayesian Nash equilibrium.

(ii) Under the mean mechanism agents announce their type truthfully if  $\alpha = \bar{\alpha}$ .

Thus  $x_{Mean} = \frac{1}{3} \sum_{i=1}^3 \theta_i$  and it holds that  $\theta_i^* = \frac{1}{3} \sum_{i=1}^3 \theta_i$ . We obtain for the sum of expected utilities

$$E \left[ \sum_{i=1}^3 -(x_{Mean} - \theta_i^*)^2 \right] = 0$$

and it remains to show that

$$0 > E \left[ \sum_{i=1}^3 - (x_{Median} - \theta_i^*)^2 \right].$$

Under the median mechanism expected utility for individual  $i$  is given by equation (30). Multiplying by 3, this yields for  $\alpha = \frac{2}{3}$

$$E \left[ \sum_{i=1}^3 - (x_{Median} - \theta_i^*)^2 \right] = -\frac{1}{15}.$$

Q.E.D.

PROOF OF LEMMA 2:

Under the median mechanism agents announce  $\hat{\theta}_i(\theta_i) = (1 - \frac{1}{2}\alpha)\theta_i$  and thus  $x_{Median} = (1 - \frac{1}{2}\alpha)\theta_{Median}$ .

(i) CONTINUITY: The sum of expected utilities is then given by

$$\sum_{i=1}^3 E \left[ - (x_{Median} - \theta_i^*)^2 \right] = 3E \left[ - (x_{Median} - \theta_i^*)^2 \right] = -\frac{33}{20}\alpha^2 + \frac{11}{5}\alpha - \frac{4}{5} \quad (36)$$

which is continuous in  $\alpha$ .

(ii) MONOTONICITY: Differentiating with respect to  $\alpha$  yields

$$\frac{d(E [\sum_{i=1}^3 - (x_{Median} - \theta_i^*)^2])}{d\alpha} = -\frac{33}{10}\alpha + \frac{11}{5} \quad (37)$$

which is larger than zero  $\forall \alpha \in [0, \bar{\alpha}]$ .

(iii) OPTIMALITY:

$$\frac{d(E [\sum_{i=1}^3 - (x_{Median} - \theta_i^*)^2])}{d\alpha} = 0 \iff \alpha = \frac{2}{3}. \quad (38)$$

Q.E.D.

PROOF OF LEMMA 3:

Under the mean mechanism agents announce  $\hat{\theta}_i(\theta_i) = 3(1 - \alpha)\theta_i$ . Thus,  $x_{Mean} = (1 - \alpha) \sum_{i=1}^3 \theta_i$ .

(i) CONTINUITY: The sum of expected utilities is then given by

$$\begin{aligned} & \sum_{i=1}^3 E [-(x_{Mean} - \theta_i^*)^2] \\ &= -\frac{3}{8} \int_{-1}^1 \int_{-1}^1 \int_{-1}^1 \left( (1 - \alpha) \sum_{i=1}^3 \theta_i - (1 - \alpha)\theta_1 - \frac{\alpha}{2}(\theta_2 + \theta_3) \right)^2 d\theta_1 d\theta_2 d\theta_3 \\ &= -\frac{9}{2}\alpha^2 + 6\alpha - 2 \end{aligned} \tag{39}$$

which is continuous in  $\alpha$ .

(ii) MONOTONICITY: Differentiating with respect to  $\alpha$  yields

$$\frac{d(E[\sum_{i=1}^n -(x_{Mean} - \theta_i^*)^2])}{d\alpha} = -9\alpha + 6 \tag{40}$$

which is larger than zero  $\forall \alpha \in [0, \bar{\alpha})$ .

(iii) OPTIMALITY:

$$\frac{d(E[\sum_{i=1}^n -(x_{Mean} - \theta_i^*)^2])}{d\alpha} = 0 \iff \alpha = \frac{2}{3}. \tag{41}$$

Q.E.D.

PROOF OF PROPOSITION 6:

(i) From Propositions 4 and 5 and Lemmata 2 and 3 we know that there exists an  $\alpha_1$  below which the median yields a better result than the mean mechanism and that there exists an  $\alpha_2$  above which the mean is better than the median mechanism.

It remains to show that  $\alpha_1 = \alpha_2 =: \alpha^*$ . The existence of a unique point of intersection can be established by comparing the slopes of the sum of expected utility under the two mechanisms, since both are strictly positive for the relevant range of

$\alpha$ . Under the median mechanism the slope is given by equation (37) and under the mean mechanism by equation (40), respectively. For all  $\alpha \in [0, \bar{\alpha}]$  it is true that

$$-\frac{33}{10}\alpha + \frac{11}{5} < -9\alpha + 6. \quad (42)$$

and therefore  $\alpha^*$  exists.

(ii) The sum of expected utilities under the median mechanism is given by equation (36) and under the mean mechanism by equation (39). The point of intersection  $\alpha^*$  is then determined by

$$-\frac{33}{20}\alpha^{*2} + \frac{11}{5}\alpha^* - \frac{4}{5} = -\frac{9}{2}\alpha^{*2} + 6\alpha^* - 2 \quad (43)$$

which yields

$$\alpha_{1,2}^* = \frac{2}{3} \pm \frac{2}{57}\sqrt{19}. \quad (44)$$

Since  $\alpha_1^* > \bar{\alpha} = \frac{2}{3}$ ,  $\alpha_2^*$  is the unique point of intersection in the relevant interval, i.e. in  $[0, \bar{\alpha}]$ . Q.E.D.

## References

- [1979] Arrow, K. (1979) "The property rights doctrine and demand revelation under incomplete information," in *Economics and Human Welfare*. edited by M. Boskin. New York: Academic Press.
- [2000] Casella, A. (2000) "Towards a theory of storable votes," Mimeo, Columbia University, New York.
- [1982] Crawford, V. and J. Sobel (1982) "Strategic information transmission," *Econometrica*, 50, 1431-1452.
- [1979] D'Aspremont, C. and L.A. Gérard-Varet (1979) "Incentives and incomplete information," *Journal of Public Economics*, 11, 25-45.
- [2000] Dixit, A. and H. Jensen (2000) "Equilibrium contracts for the central bank of a monetary union," CES Working Paper 400.
- [2000] Fieseler, K., T. Kittsteiner and B. Moldovanu (2000) "Partnerships, Lemons and Efficient Trade," Discussion Paper, University of Mannheim.
- [2000] Gros, D. and C. Hefeker (2000) "One size must fit all - national divergences in a monetary union," CEPS Working Document 149.
- [1999] Grüner, H. P. (1999) "On the role of conflicting national interests in the ECB Council," CEPR Discussion Paper 2192.
- [1998] Jehiel, P. and B. Moldovanu (1998) "Efficient Design with Interdependent Valuations," Discussion Paper, Northwestern University, forthcoming in *Econometrica*.
- [1996] Jehiel, P., B. Moldovanu and E. Stacchetti (1996) "How (not) to sell nuclear weapons," *American Economic Review*, 86(4), 814-829.

- [1995] Mas-Colell, A., M. D. Whinston and J. R. Green (1995) *Microeconomic Theory*. New York, Oxford: Oxford University Press.
- [1999] Piketty, T. (1999) "The information-aggregation approach to political institutions," *European Economic Review*, 43, 791-800.
- [1991] Vaubel, R. and T.D. Willet (1991) *The political economy of international organizations: A public choice approach*. Political Economy of Global Interdependence series, Boulder and Oxford: Westview Press.
- [1994] Von Hagen, J. and R. Süppel (1994) "Central bank constitutions for federal monetary unions," *European Economic Review*, 38, 774-782.