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(Machine) Learning What Policies Value

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Abstract

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JEL Classification: I38, Z18, H53, O10

Keywords: targeting, Welfare, Heterogeneous Treatment Effects

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(Machine) Learning What Policies Value^{*}

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Abstract

When a policy prioritizes one person over another, is it because they benefit more, or because they are preferred? This paper develops a method to uncover the values consistent with observed allocation decisions. We use machine learning methods to estimate how much each individual benefits from an intervention, and then reconcile its allocation with (i) the welfare weights assigned to different people; (ii) heterogeneous treatment effects of the intervention; and (iii) weights on different outcomes. We demonstrate this approach by analyzing Mexico's PROGRESA anti-poverty program. The analysis reveals that while the program prioritized certain subgroups — such as indigenous households — the fact that those groups benefited more implies that they were in fact assigned a lower welfare weight. The PROGRESA case illustrates how the method makes it possible to audit existing policies, and to design future policies that better align with values.

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1 Introduction

The values behind policy decisions are not always transparent. When governments decide which households receive welfare benefits, or universities select which students to admit, they do not always articulate the rationale behind those decisions. Even when policymakers do articulate a rationale, it may be difficult to verify. In particular, certain people may be prioritized either because they are expected to benefit the most from the policy, or because they are favored — irrespective of how much they are likely to benefit. This distinction has important implications (Nichols and Zeckhauser, 1982; Coate and Morris, 1995): all members of society may agree on a ranking of who benefits most along some objective metric, but may disagree on how much welfare weight to assign to different entities.

This paper develops a method to infer social preferences that are consistent with observed policies. This method relies on recent developments in machine learning, which make it possible to estimate differential treatment effects without overfitting. We show how such methods can be combined with a second stage regression to separate heterogeneous treatment effects (who benefits the most) from implied welfare weights (who is valued) and how different outcomes are valued. As a result, we can shift the debate from one about means — who should receive what — to one about ends — what are the impacts we desire, and which populations are most important?

We consider a common form of decision, an allocation based on a score or ranking. These may be poverty scores in the case of welfare programs, or explicit rankings in the case of applicants for college admission or small business grants. This ranking implies a system of inequalities between the contributions of different entities to welfare. We use this system of inequalities, and a simple and general model of welfare, to estimate the implied value on different outcomes (estimated using modern methods for heterogeneous effects) and different entities (based on observed characteristics), using ordinal logistic regression. Our method can also be used if one only observes the binary decision of who is eligible and who is not, though it will have less power.

Intuitively, if a policy allocates benefits to one type of entity who is expected to benefit little from the allocation, rather than to a different type that is expected to benefit greatly, that suggests the policy implicitly places higher welfare weight on the first type. Or, if a policy consistently allocates to applicants whose health improves as a result of the intervention — instead of applicants whose consumption increases — that implies the policy implicitly highly values health.

To illustrate how this method can be used to interrogate a real-world policy, we apply it to historical data from PROGRESA, one of the world's largest (and best-studied) anti-poverty programs. In this context, we first estimate the heterogeneous treatment effects of the program using Wager and Athey's (2018) causal forest machine learning method (though as we discuss, alternative methods for estimating treatment effects would work as well). Consistent with prior work, we find evidence of treatment effect heterogeneity — for instance, that indigenous households benefit most from the program (cf. Djebbari and Smith, 2008).

We then use our method to estimate the preferences consistent with the observed ranking of households and its heterogeneous effects on consumption, child health, and school attendance. We find that indigenous households were more likely to be allocated the program, but because they benefit so much more, that the policy is actually consistent with weighting them 11.7% *lower* than non-indigenous households. Our results also suggest that the program's design is consistent with assigning extra value to poorer, larger, and less educated households: households are weighted 0.14% lower for each 1% increase in household income, 5.7% higher for each additional person in the household, and 32.8% lower if the household head has a high school education. These valuations, estimated using our method, are similar to the stated preferences of Mexican residents, as measured by hypothetical allocation questions in a survey we conducted in 2021. We additionally recover estimates of how the policy implicitly values impacts on health and schooling relative to consumption. Confidence intervals are imprecise but admit conventional valuations.

Finally, we show how this approach can further be used to evaluate counterfactual policies and preferences. In the PROGRESA case, we show what *would have occurred* had the program designers placed higher value on certain types of impacts (e.g., health vs. education) or certain types of households (e.g., equal welfare weights). This analysis suggests that, for instance, a policymaker who cared exclusively about impacts on schooling should prefer a policy that prioritizes richer households; a policymaker that valued only health impacts would instead prioritize indigenous households. More broadly, we show where these counterfactual policies lie relative to the Pareto frontier

that characterizes improvements across the three focal welfare outcomes.

Taken as a whole, this approach makes it possible to invert the discussion about policies and programs. Rather than debate the means of the policy (who is eligible, how large are the benefits?), this framework makes it possible to debate the ends (how much do we value health, education, or consumption? Should poor families be prioritized over middle class families?). Indeed, modern econometric methods have begun to reveal that many policies benefit some groups more than others (cf. Haushofer et al., 2022); our framework suggests how policies might be reconciled with that heterogeneity. The framework can be applied to a wide range of settings where policymakers allocate scarce resources and heterogeneous treatment effects can be estimated.

The approach has three caveats. First, it requires defining which outcomes and characteristics are allowed to enter the objective function; outcomes that are not included are assumed to not be valued. While this decision is a substantive one, the method is sufficiently flexible to allow for other definitions of welfare. Second, in order to estimate how different types of people are affected by the intervention, the analyst must observe experimental variation in access to the intervention for all types of people (including both those who are ultimately eligible and ineligible under the policy). This is commonly the case with randomized controlled trials or pilots. Third, it requires a large enough dataset to estimate both heterogeneous treatment effects and the implied welfare parameters. These datasets are increasingly becoming available, particularly in settings with digital experimentation.

Related Literature

This paper contributes to literature on optimal targeting and taxation (Nichols and Zeckhauser, 1982; Barr, 2012; Fleurbaey and Maniquet, 2018), including work comparing targeted policies to universal basic income (Alatas et al., 2012; Hanna and Olken, 2018). It can be viewed as a response to Ravallion (2009), which argues that targeting poverty directly may not be sufficient for impact, and suggests that it may be better to target based on desired outcomes. In that sense, our work relates closely to Haushofer et al. (2022), which asks how targeting on treatment effects compares to targeting on baseline poverty. Their empirical analysis suggests that those who are most impacted by a Kenyan cash transfer are not always the poorest. Our paper focuses on the inverse problem of estimating the welfare function consistent with an observed policy. The two approaches are thus complementary; our also extends from a specified utility function defined over a single outcome to a general welfare function that can rationalize targeting based on household characteristics as well as impacts on multiple outcomes. Our empirical results also engage with research on the effects and allocation of cash transfer programs (Behrman and Todd, 1999; Skoufias et al., 2001a; Gertler, 2004; John Hoddinott, 2004; Coady, 2006; Djebbari and Smith, 2008; Alderman et al., 2019). We build on this work by showing how effects can be used to audit policymaker priorities, and improve the design of future policies.

Our approach also relates to a growing literature that takes a given welfare function as fixed, and considers what are the best decisions to take. Kitagawa and Tetenov (2018) computes optimal assignment of treatment with experimental data, and Athey and Wager (2020) with observational data. Gechter et al. (2019) assesses how well different ex ante treatment assignments maximize a given welfare function under ex post experimental data. Wang (2020) considers the theoretical problem of allocating resources given heterogeneous aid agency preferences over individuals, and describes allocation queues as a solution to a combinatorial problem. This literature faces a central problem: what notion of welfare do, or should, societies maximize? Our paper takes a step towards answering this question, by solving the reverse problem: estimating welfare functions consistent with observed decisions.

It is increasingly common to construct indices summarizing multiple outcomes as a more nuanced measure of welfare (Greco et al., 2019). A persistent question in assembling these indices is what weight to apply to each component. These weights have economic meaning: how valuable is one component relative to another? Common approaches are geometric: setting equal values to each component (UNDP, 1990), or analyzing how components vary together in observational data, using a principal component analysis (Filmer and Pritchett, 2001; McKenzie, 2005). We derive weights that have an economic interpretation using revealed preferences, how policies implicitly make trade-offs. A related approach is to set weights to optimally predict some gold standard measure of utility, if one is available (Jayachandran et al., 2021).

Also related is a recently expanding public finance literature on welfare weights.

Hendren (2019) infers the weight on different households implied by a tax schedule, based on the distortions required to transfer them resources. Saez and Stantcheva (2016) generalize welfare weights to reconcile popular notions of fairness with optimal tax theory. Our paper shows how similar welfare questions can be raised across a broad set of domains where heterogeneous treatment effects can be estimated.

More broadly, our efforts also connect with recent computer science scholarship on fairness in machine learning (cf. Dwork et al., 2012; Barocas et al., 2018). Several papers in this literature study the social welfare implications of algorithmic decisions, and how social welfare concerns relate to different notions of fairness (Ensign et al., 2017; Hu and Chen, 2018; Mouzannar et al., 2018; Liu et al., 2018). This relates to work on multi-objective machine learning (Rolf et al., 2020). Kasy and Abebe (2020) describe limitations of fairness constraints, and suggest that algorithms should be optimized for impacts. Also related, Noriega et al. (2018) discuss how different constraints to targeting can impact efficiency and fairness. Our approach is distinct, however, in that we show how using machine learning tools can be used to better characterize and audit the values consistent with a program's observed allocation. We hope that by providing increased visibility into these revealed preferences, future policies can be better aligned with stated preferences and explicit policy objectives.

2 Model

We consider the problem of allocating treatment among N entities, which could be, for example, individuals, households, firms, or regions. For convenience, we refer to entities as households.

A policymaker has ranked each household i in the priority order they will be allocated some benefit or treatment, $T_i \in \{0, 1\}$. This ranking z_i may include ties between households; in the extreme it could simply represent the binary decision of whether household i will be allocated treatment ($z_i \in \{0, 1\}$).

We attempt to reconcile that ranking with an implicit welfare function:

$$S = \sum_{i} S_{i}$$
$$S_{i} = \mu(\mathbf{x}_{i}) \cdot u_{i}(T_{i})$$

where each household *i* is valued according to some objective utility $u_i(T_i)$, scaled by some differential welfare weight $\mu(\mathbf{x}_i)$ based on its characteristics \mathbf{x}_i , with a functional form to be specified later. Objective utility u_i can be decomposed into components:

$$u_i(T_i) = v_{i0}(T_i) + \sum_{j>0} \lambda_j(\mathbf{x}_i)v_{ij}(T_i) + C \cdot T_i$$

where v_{ij} represents a component of utility (such as consumption, or health), and $\lambda_j(\mathbf{x}_i)$ represents j's implied value relative to the numeraire or reference outcome (j = 0), with a functional form to be specified later. C is a constant representing the net intrinsic value of providing the program, even absent impact.¹

Imagine we knew the impact of treatment on household *i*'s component of utility $j: \Delta v_{ij} \coloneqq v_{ij}(1) - v_{ij}(0)$. The welfare impact of treating household *i* could then be written

$$\Delta S_i = \mu(\mathbf{x}_i) \cdot \left(\Delta v_{i0} + \sum_{j>0} \lambda_j(\mathbf{x}_i) \Delta v_{ij} + C \right)$$

The ranking could then be reconciled with ordering households according to their implied welfare impact from receiving treatment,

$$z_i = f(\Delta S_i + \epsilon_i) \tag{1}$$

where f is a weakly increasing transformation, which preserves the ranking of households. The shock ϵ_i may represent measurement error in estimates of welfare, or mistakes in the allocation.

2.1 Measuring Utility Impacts

Reconciling the observed ordering of households with the welfare impacts of the policy requires that we have an estimate of the impact of treatment on utility for each household. We will assume that each utility component v_{ij} is a function of an observed outcome y_{ij} ,

$$\Delta v_{ij} \coloneqq v_{ij}(T_i = 1) - v_{ij}(T_i = 0) = g_j(y_{ij}^1) - g_j(y_{ij}^0)$$

¹For intuition: if C is very large, the ranking between households is explained mostly by differences in welfare weights; if C is small or zero, the ranking depends also on impacts.

where g_j represents the utility function for j (which could be, for example, $g_j(y) = \log(y)$, or $g_j(y) = y$).² Additionally, we assume that we have an experimental design that makes it possible to predict the heterogeneous effects of treatment on each household and each outcome $\Delta \hat{v}_{ij}$.

2.2 Intuition

To demonstrate the intuition behind our method, we illustrate with a simple example in Figure 1. Consider the case of a single outcome and one dimension of heterogeneity, x, which corresponds to income. A policymaker allocates a program by ordering households by the function z(x), prioritizing poor households. As shown in Figure 1, depending on how treatment effects vary with x, the same allocation could result from (1) higher welfare weights on the poor, (2) equal welfare weights, or (3) higher welfare weights on the rich. Likewise, in the case where x is binary, an allocation to one group can result from (i) higher welfare weights, if that group benefits the same or less; (ii) equal welfare weights, if that group benefits more; or (iii) lower welfare weights, if that group benefits much more.

The next section demonstrates how to empirically recover welfare and impact weights from data in when there are multiple dimensions of heterogeneity and multiple outcomes of interest.

²We assume that these functional forms are known, but they could be estimated within our setup. If the $g_j(\cdot)$ utility functions are incorrectly specified to be linear, then welfare weights $\mu(\mathbf{x}_i)$ and the vector of impact weights $\lambda(\mathbf{x}_i)$ can measure the combination of the underlying welfare weights and curvature in utility to first approximation. See Appendix Section A1.

An allocation rule that prioritizes the poor $(low x_i)$





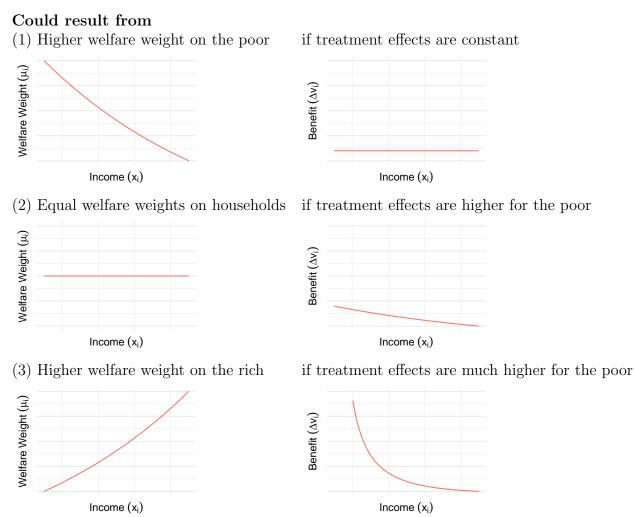


Figure 1: Intuitive Example

3 Estimation

Estimation proceeds in two steps:

We first predict the effect of treatment on each outcome $\Delta \hat{v}_{ij} = \Delta \hat{v}_j(\tilde{\mathbf{x}}_i)$, which may be heterogeneous as a function of covariates $\tilde{\mathbf{x}}_i$. This can be done using a variety of methods for estimating heterogeneous treatment effects, such as Wager and Athey's (2018) machine learning approach, which works well when there is experimental variation in treatment assignment.³

Then, given that the policy achieves effects estimated to be $\Delta \hat{v}_{ij}$, we ask what preferences (i.e., $\mu(\mathbf{x}_i)$, the vector $\boldsymbol{\lambda}(\mathbf{x}_i)$, and C) would be consistent an allocation according to the given ranking (\boldsymbol{z})? If household i is prioritized over i' ($z_i > z_{i'}$), equation (1) implies:

$$\mu(\mathbf{x}_i) \cdot \left(\Delta \hat{v}_{ij} + \sum_{j>0} \lambda_j(\mathbf{x}_i) \Delta \hat{v}_{ij} + C\right) + \epsilon_i > \mu(\mathbf{x}_{i'}) \cdot \left(\Delta \hat{v}_{i0} + \sum_{j>0} \lambda_j(\mathbf{x}_{i'}) \Delta \hat{v}_{ij} + C\right) + \epsilon_i$$

This problem can be modeled with an ordinal logit likelihood if we make the common assumption that the ranking error is distributed extreme value type-I: $\epsilon_i \sim \sigma \cdot EV(1)$. Then, the logit likelihood of this particular placement of *i* in the ranking *z* is:

$$l_{i} = \frac{\exp\left[\frac{1}{\sigma} \cdot \mu(\mathbf{x}_{i}) \left(\Delta \hat{v}_{i0} + \sum_{j>0} \lambda_{j}(\mathbf{x}_{i}) \Delta \hat{v}_{ij} + C\right)\right]}{\sum_{i' \epsilon \Lambda_{i}} \exp\left[\frac{1}{\sigma} \cdot \mu(\mathbf{x}_{i'}) \left(\Delta \hat{v}_{i'0} + \sum_{j>0} \lambda_{j}(\mathbf{x}_{i'}) \Delta \hat{v}_{i'j} + C\right)\right]}$$
(2)

where $\Lambda_i = \{i' | z_{i'} < z_i\}$ represents the set of households ranked lower than household *i*.

The logit likelihood of the full observed ranking \boldsymbol{z} is therefore

$$L(\boldsymbol{z}, \mathbf{x}, \boldsymbol{\mu}, \boldsymbol{\lambda}, C, \sigma) = \prod_{i} l_{i}$$

We use maximum likelihood to estimate the functions $\mu(\mathbf{x}_i)$ and $\lambda(\mathbf{x}_i)$ and parameters C and σ that best match the observed data $\{\mathbf{z}, \mathbf{x}, \{\Delta \hat{v}_{ij}\}_{ij}\}$. Unlike standard discrete choice settings where partial orderings are observed for multiple decisionmakers, we observe a single ordering of all alternatives. For this type of ranked data, we

³For treatment effect heterogeneity, covariates need only be correlated with impacts, so one may wish to include a large set of covariates in $\tilde{\mathbf{x}}_i$. In contrast, the choice of \mathbf{x}_i determines which characteristics to allow favoritism over, so one may wish to justify a smaller set.

follow the exploded logit likelihood described by Train (2009).

Standard errors are computed by bootstrapping the entire procedure (accounting for uncertainty in both treatment effects and preference parameters). Individuals are drawn with replacement, and these bootstrapped samples are used to compute treatment effects, and then welfare and impact weights.

In many settings, we may not observe a full ranking or score, but rather a binary allocation of beneficiaries and non-beneficiaries $(T_i \in \{0, 1\})$. This corresponds to a ranking with two levels. In such settings, the same procedure described above can be applied.

3.1 Parameterization

Our framework will work with general functional forms for $\mu(\mathbf{x}_i)$ and $\lambda_j(\mathbf{x}_i)$. In the empirical application that follows in Section 4, we model welfare weights as multiplicative:

$$\mu(\mathbf{x}_i) = \prod_k \omega_k^{x_{ik}}$$

We model the relative weight on outcome j as the same for all households, $\lambda_j(\mathbf{x}_i) \equiv \lambda_j$, because our sample is not large enough to differentiate heterogeneity on these dimensions.

3.2 Identification

Preferences are identified based on how the policy's ranking (z_i) varies with characteristics (\mathbf{x}_i) and with treatment effects on components of utility $(\Delta \hat{v}_{ij})$.

Unobservables Our approach estimates the preferences that are consistent with the implemented policy z_i , given the estimates of impact Δv_{ij} . This can be thought of as an ex-post audit. Our estimates will recover an observed component of welfare, ΔS_i , that is uncorrelated with any unobserved component, ϵ_i . There are several reasons why these implied preferences might differ from the actual preferences of the policymaker.

First, implied preferences could differ from policymaker preferences if the policymaker based the ranking on correlated unobservables. For example, if a policymaker is racially biased but an analyst does not allow race to enter modelled preferences, the policy may be found to be consistent with a preference for an income level that is correlated with race. In such settings, the method still reveals preferences that are *consistent* with the policy's values, under the given specification of preferences.⁴ The specification of preferences (i.e., which variables they are defined over and their functional form) is thus a substantive decision. For this reason, practical applications should include both characteristics that policymakers wish to prioritize as well as characteristics for which there may be concerns of bias.

Second, implied preferences could differ from policymaker preferences if the policymaker has incorrect beliefs about these impacts at the time of the decision. If that were the case, upon observing the results of our method, the policymaker could change the policy to better align with their preferences. The method thus provides a tool for course correction.

The method can also be applied in cases where there is no single policymaker—for example, where allocations are the result of deliberations between constituents. In that case, our method will reveal social preferences consistent with the final allocation.

Sufficient variation Identification also requires sufficient variation. It requires that some households benefit more than others. Welfare weights $\boldsymbol{\omega}$ are primarily identified based on heterogeneity in impacts on the numeraire utility $\Delta \hat{v}_{i0}$. If treatment effects were homogenous, it would not possible to separately identify $\boldsymbol{\omega}$ and $\boldsymbol{\lambda}$ (their combination may be identified, in which case our method would collapse down to a standard exploded logit that does not account for treatment effects).

Identification of λ also requires that treatment has different impacts on different components of utility. Impact weight λ_j is identified from the relative ranking of households that are impacted more or less on utility component j > 0 than on the numeraire (j = 0). If the treatment effects were heterogeneous but colinear between different components of utility, it would be possible to identify $\boldsymbol{\omega}$ but not $\boldsymbol{\lambda}$, because the data would not reveal how different components of utility influence the ranking.

The resulting parameters $\boldsymbol{\omega}$ reveal which characteristics \mathbf{x} are correlated with being prioritized. If \mathbf{x} includes both a relevant variable x_{ik} as well as an irrelevant but collinear variable $x_{ik'}$, the method will have imprecise estimates of the contribution

⁴This is analogous to the way that ordinary least squares recovers the best linear predictor given included variables, even in the presence of omitted variables.

of both, in a similar manner as a standard regression would. In that sense, one may want to restrict analysis to characteristics \mathbf{x} that one believes may be relevant for differential preference. In our application, we use survey data to narrow down factors that should enter the targeting rule.

4 Application

To illustrate how our method can be used in applied settings, we use the case of PROGRESA, a large conditional cash transfer program in Mexico.

4.1 Background on PROGRESA

First implemented by the Mexican federal government in 1997, PROGRESA provided cash transfers to poor households. Transfers, which averaged 197 pesos per month (approximately \$20 USD at the time), were conditioned on regular doctor's visits and/or regular school attendance (John Hoddinott, 2004). Roughly 99% of enrolled households met these conditions (Simone Boyce, 2003).⁵

Within poor communities, PROGRESA ranked households based on a 'household poverty score' that incorporated a variety of different characteristics (such as household structure, indigenous languages, occupation, income, housing materials, etc.).⁶ The score was computed in three steps. First, each household was classified as poor or not poor based on per capita income. Second, that poverty classification was approximated using discriminant analysis based on household characteristics (Skoufias et al., 1999). Third, the list of eligible households was presented in meetings in each community for review; a small number of households changed classification as a result. Our focus is on understanding which underlying values are consistent with the allocation resulting from this method of determining eligibility for the program.

⁵For simplicity, our analysis does not account for the conditionality of the transfer. For a more detailed discussion of PROGRESA and its background, see Emmanuel Skoufias (2008), and Simone Boyce (2003).

⁶The program defined poor communities as those with a high 'village marginality index', computed based on the proportion of households living in poverty, population density, and health and education infrastructure. We focus on the preferences implied by household poverty scores, which were the basis for determining which households within a community eligible for the program.

During its initial implementation, PROGRESA administrators used a staggered roll-out to randomize when villages could enroll in the program: of the 506 villages included in the evaluation, 320 were randomly assigned to treatment, and initiated into the program in summer 1998. 186 communities were assigned to control and were not initiated into the program until 2000. Behrman and Todd (1999) show that the randomization across communities was successful in that treatment and control communities were statistically indistinguishable across a wide array of observable covariates.

Data

Our analysis relies on two distinct sources of data. The first is a standard household survey conducted in October 1998 (baseline) and November 1999 (endline). These capture household demographics, socioeconomic characteristics, health care utilization, and educational attendance for 14,333 households over the entire experiment period – see Appendix Table A1 for summary statistics. We focus on the sample of 6,642 households over which our outcomes are defined, who have at least one child aged 5 or below and at least one child aged 6-16. Thus, our estimates will reveal the values implied by the rankings within households with children, and not between households with and without children in the relevant ages.

The second data source is a survey that we conducted in 2021 to understand the preferences of Mexican residents over how households should be prioritized for social assistance. We surveyed a sample of 315 Mexican residents to elicit preferences for which types of households should receive transfers, and what types of program impacts were most desirable, in a manner similar to Saez and Stantcheva (2016). The survey asked respondents which household attributes should be considered in the design of such a program, and relied on multiple price lists to elicit indifference points. For a complete description of this survey, see Appendix A3.

We focus on three welfare outcomes that were monitored in the household surveys: (i) logarithm of *per-capita consumption*; (ii) *child health*, measured as the average number of sick days per child aged 0-5; and (iii) *school attendance*, calculated as the average number of school days missed per child aged 6-16. We treat log consumption as our numeraire $(g_0(y_{consumption})) = \log(y_{consumption}))$, and allow the other two outcomes to enter the welfare function linearly $(g_j(y_j) = y_j \text{ for } j > 0)$.⁷ Previous studies have estimated significant treatment effects on all three outcomes using the same survey data (John Hoddinott, 2004; Emmanuel Skoufias, 2008; Simone Boyce, 2003; Djebbari and Smith, 2008). Note that the program could also have impacted other outcomes not measured; our method will assume that such impacts are either zero or not valued. In Section 4.3.2, we discuss implications and extensions of this simplifying assumption.

We define welfare weights $\mu(\mathbf{x}_i)$ over the top five characteristics that Mexican residents in our survey reported should be considered when targeting cash transfers (\mathbf{x}_i) : income; number of people; and age, education, and indigenous status of the household head.

4.2 Characterizing the Decision Rule

As a first step, we characterize the decision rule, by indicating which types of households are observed to be ranked higher than others. Table 1 column 1 reports these results, where the contribution of household characteristics to the final ranking \boldsymbol{z} is estimated with a logit ranking model (i.e., our model's likelihood equation (2) with constraints $\Delta \hat{v}_{ij} \equiv 0$ and C = 1, estimating the constrained weights $\tilde{\boldsymbol{\omega}}$). We report coefficients transformed by log base 1.01 (log_{1.01}($\tilde{\boldsymbol{\omega}}$)), which can be interpreted as the number of successive 1% increments implied. This suggests that households that are indigenous are ranked 47% higher (1.01^{38.6}). It also suggests that each 10% increase in income corresponds with a 2% decrease in ranking. Each additional household member is associated with a 14% (1.01^{13.0}) increase in ranking. However, the conventional regression in column 1 does not describe *why* these households are ranked highly; it could be that they benefit more (higher treatment effects) or that they are favored (higher welfare weights), as suggested in Figure 1.

4.3 Results: Estimating What Policies Value

Our main results from the PROGRESA example show how our method can decompose an observed allocation into the values implied by the decision rule.

⁷Gandelman and Hernandez-Murillo (2015) fails to reject a level of risk aversion consistent with logarithmic utility in Mexico, based on self-reported wellbeing.

	Household Poverty Score 1999			
	Decision Rule Implied Preference			
	(Prioritization)	Welfare Weights $log_{1.01}(\boldsymbol{\omega})$		
(number of 1% increments)				
Indigenous	38.57(5.0)	-12.4 (4.2)		
$\log(\text{Income})$	-24.9(1.9)	-14.3(5.4)		
Household Size	13.0(0.8)	5.6(2.1)		
Head Age	-2.31(0.2)	-1.0 (0.6)		
Education (HS or above)	-240.2(848.5)	-39.9(21.5)		
		Impact Weights		
(log points of daily consumption)				
Missed Schooling (per day)	λ_1	-0.03 (0.17)		
Sickness (per child sick day)	λ_2	$0.08\ (0.05)$		
Value Regardless of Impact	C	0.47 (3.75)		
σ		$0.17 \ (0.17)$		
N	6642	6642		

Table 1: What Values are Consistent with the PROGRESA Decision Rule?

Notes: Left column is computed using our method, without treatment effects included in the estimation. Right column is calculated using causal forests to estimate heterogeneous treatment effects (see Figure 2). In all columns, standard errors are computed using a two-step bootstrap procedure that accounts for uncertainty in both treatment effects and preference parameters. Observations are drawn with replacement before estimation of the treatment effects and the welfare and impact weights. Treatment effects are then estimated from these bootstrapped samples, and welfare and impact weights estimated from these bootstrapped treatment effect estimates; the standard errors reported are the standard deviation across bootstrapped welfare and impact weight estimates.

4.3.1 Heterogeneity in Treatment Effects

As has been documented in prior work, the PROGRESA program significantly increased household welfare. On average over our sample, PROGRESA increased log household monthly consumption by 0.135, reduced the number of sick days per child by 0.18, and reduced the number of school days missed per child by 0.005.

However, these treatment effects were heterogeneous. We estimate this heterogeneity $\Delta \hat{v}_j(\tilde{\mathbf{x}}_i)$ using Wager and Athey's (2018) causal forest method, which recovers heterogeneous treatment effects nonparametrically, and includes restrictions to limit overfitting. Figure 2 shows that different households benefit by different amounts across the three outcomes. In particular, the program increased the consumption of indigenous households more than non-indigenous households. This can be seen in the fact that indigenous status is the most important feature in the causal forest (Appendix Table A2, column 1). The heterogeneity by indigenous status is also evident in Appendix Figure A1, which shows residualized treatment effects, estimated after removing variation explained by the other covariates.

While our main analysis relies on causal forests, which allow for more flexible and precise estimates of heterogeneity than linear models, the approach described in Section 3 can be used with alternative methods for estimating heterogeneous treatment effects. Corresponding results for OLS are reported in Appendix Section A4 and Appendix Figure A2.⁸

4.3.2 Implied Policy Preferences

Next, given that we predict the policy would have impacts $\Delta \hat{v}_{ij}$ on household *i*, we use our method to back out the implied preferences consistent with ranking that household at position z_i . Table 1 column 2 reports the preferences that are consistent with the ranking \boldsymbol{z} . The first block of rows shows the implied welfare weights ($\boldsymbol{\omega}$), and the second block shows implied impact weights ($\boldsymbol{\lambda}$ and C) and the standard deviation of the error term (σ).

We find that when the differential benefit that indigenous households face is

⁸Comparing the causal forest estimates in Appendix Figure A1 with the OLS estimates in Appendix Figure A2, the relative flexibility of causal forests is apparent. While the general pattern of heterogeneity is often consistent across both methods, the causal forest method better captures non-linearity.

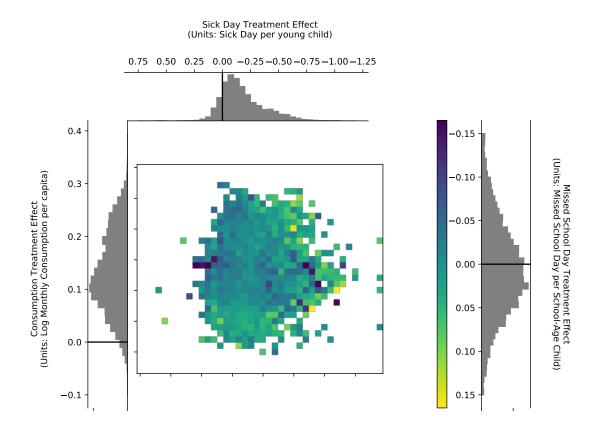


Figure 2: Distribution of Estimated Treatment Effects

Notes: Heterogeneous treatment effects of PROGRESA, estimated using causal forests Wager and Athey (2018). Histograms show marginal treatment effects on log Consumption (left), Health (top), and School Attendance (right). Center figure shows joint distribution, where each cell corresponds to a combination of consumption and health treatment effects, and is colored according to average treatment effect on attendance. Households without at least one young and one school-age child are omitted from the figure.

accounted for, the decision rule actually implicitly places *lower* welfare weight on indigenous households (by $11.7\% = 1.01^{-12.4}$). Likewise, part of the negative weight on higher-income households can be explained by slightly lower marginal treatment effects for consumption for those households, and so the model infers moderately less negative implicit welfare weight on income when taking these heterogeneous treatment effects into account.

Our estimates of weights on different impacts are imprecise, so we focus on the bounds implied by 95% confidence intervals. These suggest that the Mexican government's initial allocation rule is consistent with valuing each day of school attendance at less than 36% of daily per capita consumption (the point estimate suggests a positive value of 3%). They also suggest that the rule is consistent with valuing each prevented sick day per young child at less than 2% of daily per capita consumption (the point estimate actually suggests a negative value of 8%). The bounds for the value of schooling cover estimates of the returns to schooling from the literature; based on a review of multiple studies, Psacharopoulos and Patrinos (2018) suggest a 9% average return to a year of schooling.

Most of the implied value of the program comes from its impact on consumption, followed by the effect of providing the program independent from its effect on measured outcomes (the constant term C). The value of C of 0.47 log points corresponds with an average of 179.4 pesos of consumption per person per month. The fact that this is larger than the average transfer of 33.9 pesos per person per month (John Hoddinott, 2004) suggests that the policy may implicitly value a peso of recipient consumption less than a peso of transfer. (Our estimates denominated in pesos are relative to the value placed on consumption gains.)

4.3.3 Alternative Preferences

Our framework also makes it possible to compare the preferences consistent with alternative policies. For instance, in the PROGRESA case, the Mexican government expanded the program in 2003, using a different poverty score to increase the priority of older and smaller households (Skoufias et al., 2001b). As shown in column 2 of Table 2, our method reveals that this new poverty score implicitly placed more welfare weight on richer households, and slightly less weight on larger and younger households. The

	(1)	(2)	(3)						
	Implied Preferen	Implied Preferences (Estimated)							
	(1999 Pov. Score)	(2003 Pov. Score)	(Resident survey)						
Welfare Weights $log_{1.01}(\boldsymbol{\omega})$ (number of 1% increments)									
Indigenous	-12.4 (4.2)	1.5 (3.0)	-6.1(6.4)						
$\log(\text{Income})$	-14.3(5.4)	-1.8 (1.4)	-20.2(8.5)						
Household Size	5.6(2.1)	1.9(1.3)	1.6(2.0)						
Head Age	-1.0(0.6)	-0.03 (0.07)	0.4~(0.3)						
Education (HS or higher)	-39.9(21.5)	-9.8(7.8)	-6.3(3.6)						
Impact Weights (log points of daily consumption)									
Missed Schooling (per day) λ_1	-0.03(0.17)	$0.02 \ (0.2)$	-0.35 (0.15)						
Sickness (per child sick day) λ_2	0.08 (0.05)	$0.16 \ (0.12)$	-0.34 (0.15)						
Value Regardless of Impact C	0.47 (3.75)	2.82(12.52)							
σ	0.17 (0.17)	$0.31 \ (0.28)$							
Ν	6642	6642	310						

Table 2: Assessing Decision Rules

Notes: Columns 1-2 are estimated using our method, using causal forests to estimate heterogeneous treatment effects. Column 1 estimates model using 1999 poverty scores; column 2 using 2003 poverty scores. Column 3 indicates stated preferences based on a survey of Mexican residents. Standard errors in columns 1-2 are computed using a two-step bootstrap procedure that accounts for uncertainty in both treatment effects and preference parameters. We exclude bootstrap draws (0 draws for the 1999 ranking, 1 draw for the 2003 ranking, out of 50 for each) that converged to corner solutions against the zero lower bound for omega. Standard errors in column 3 are computed directly from survey responses.

impact weights are also imprecisely estimated; the 95% confidence intervals suggest the valuation of a missed day of school below 36% of consumption and of a young child sick day below 7% of consumption.

Table 2 also illustrates how the implemented policy (column 1) compares to the median stated preferences of residents, as reported in the survey we conducted in 2021 (column 3). The welfare weights implied by the implemented policy are similar to resident preferences: we fail to reject differences in all but age of the household head (which is small in magnitude). On average, survey respondents value impacts on children more: sick days at 34% of daily consumption and school attendance at 35% of daily consumption, though both of these estimates are imprecise.

4.4 Counterfactuals

We next consider the reverse problem: given preferences, what would the resulting policy look like? In the PROGRESA example, Table 3 compares the policy's true allocation (column 1) to counterfactual allocations that would have resulted from alternative preferences (columns 2-6). Panel A indicates which preferences are used. We allow the welfare weights to be those estimated from the 1998 policy (columns 1, 4-6), those elicited from the resident survey (column 2), or fixed to weight all households equally (column 3). We allow the impact weights to be those estimated from the 1998 policy (column 2), or to only value one outcome (columns 4-6). Panel B indicates the decision rule implied by those preferences. Panel C shows the average outcomes that would be expected under the hypothetical policy, assuming it treated the same number of households as the implemented policy.

	(1)	(2)	(3)	(4)	(5)	(6)
	HH Poverty Resident		Equal Welfare	Policy only values impact on:		
	Score	Preferences	Weights	Education	Health	Consumption
Panel A: Preferences						
Welfare Weights $\boldsymbol{\omega}$	Estimated	From survey	Unity	Estimated	Estimated	Estimated
Impact Weights $\boldsymbol{\lambda}$	Estimated	From survey	Estimated	Only education	Only health	Only consumption
Panel B: Implied decision rule	e (priority over	covariates, in	1% increments)			
Indigenous	38.6	17.2	143.3	-48.2	53.0	176.2
$\log(\text{Income})$	-24.9	-88.4	-10.0	89.8	-28.5	-26.4
Household Size	13.0	15.0	2.31	-13.8	4.3	8.9
Head Age	-2.3	3.3	-0.6	-10.8	-1.1	-1.6
Education	-240.2	32.4	12.7	24.2	-93.9	-49.8
Panel C: Counterfactual outco	omes (monthly)	I				
Log Consumption (pesos)	4.852	4.853	4.875	4.849	4.843	4.874
Missed school (days/child)	0.168	0.167	0.164	0.140	0.171	0.165
Sickness (sick days/child)	0.637	0.609	0.655	0.647	0.567	0.635
Ν	6642	6642	6642	6642	6642	6642

Table 3: Designing Decision Rules

Notes: Table shows the distributional and outcome effects of designing decision rules using our framework. Panel A indicates which weights are used to prioritize households. Column 1 uses the ranking assigned by PROGRESA. Column 2 uses preferences elicited in a survey we conducted of Mexican residents. Column 3 projects the ranking as though the policy did not prioritize certain types of households, and was based on preferences over outcomes estimated in Table 2. Columns 4-6 indicate what would have happened if the policy used the estimated weights over households but only valued about impacts on education/health/consumption. Panel B shows the distributional effects of each column's preferences, by estimating the implied priority ranking across households. Panel C shows each policy's expected average outcomes, calculated using estimates of heterogeneous treatment effects.

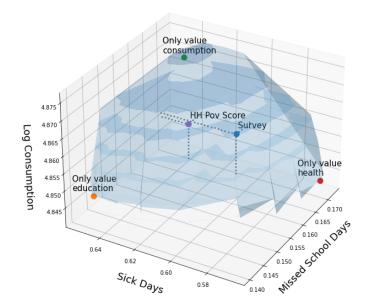
Survey-based estimates of resident preferences Column 2 shows the allocation that would result from imposing the preferences of residents as revealed by the survey. Relative to the actual policy in column 1, the hypothetical policy in column 2 reduces the prioritization of indigenous households, and increases the prioritization of poor households. Other household attributes are similarly prioritized under the two policies. In Panel C, we see that the policy consistent with resident preferences would slightly reduce child sickness relative to the implemented policy.

Alternate welfare weights When welfare weights are set equal across households (column 3), the resulting score prioritizes indigenous households by a much larger factor, and lowers the priority given to lower income and larger households.

Prioritizing specific welfare outcomes While in practice implemented policies may balance multiple outcomes, in columns 4-6 of Table 3, we present counterfactual allocations that would result in the extreme case where a policy was designed to improve only a single outcome. For instance, a policy designed to maximize education would prioritize smaller households and those with *higher* income (column 4). On the other hand, if only health effects were valued, the policy would slightly increase the prioritization of indigenous households (column 5). Finally, a policy that maximized consumption with no explicit consideration of health or education (column 6) would place much greater priority on households where the head is indigenous and reduce the penalty on education.

Understanding the policies that would result from extreme preferences can help in understanding the full set of potential policies, and what those policies imply. In the PROGRESA case, Figure 3 characterizes the frontier of possible average welfare impacts that would result from different allocations of the program. This frontier is shown as a convex hull with contour lines; the labeled points correspond to the policies given in the columns of Table 3. Policies that only value a single outcome lie at the corners of the outcome space. The implemented program ('HH Poverty Score') is close to the allocation consistent with the survey of Mexican residents preferences; neither are quite on the frontier with respect to unweighted outcomes, but both are close. (They are on the frontier of outcome spaces scaled by the corresponding welfare





Notes: Figure shows the frontier of possible average welfare impacts that would have resulted from different allocations of PROGRESA. Each axis indicates the expected average impacts for a given welfare outcome. Labeled points correspond to particular allocations described in Table 3. Appendix Figure A5 shows the frontier when outcomes are scaled by welfare weights.

weights, see Appendix Figure A5.) More broadly, this method makes it possible to navigate program design in outcome space, rather than implementation space.

4.5 Extensions

If only an allocation is observed In many settings, priority rankings are not available. Our method can still be used when the analyst observes only the final allocation (e.g., who receives the program, or who is admitted). This is because the binary indicator of whether a household received an allocation represents a (short) ranking. In the PROGRESA example, Table A3 demonstrates that when our method is applied to a binary allocation $(z(\mathbf{x}_i) = 1\{i \text{ above median rank}\})$, point estimates are similar to those reported in Table 1. Though the estimates are much less precise under the binary allocation, the qualitative insights are the same.

Testing models of welfare The method can also be used to test whether policies are internally consistent with a postulated welfare function. If there is more than one potential treatment or policy, one could test the hypothesis that they apply the same welfare weights for each one. If that hypothesis is rejected, one can rule out that the policies are consistent with utilitarianism, given ex post information.

5 Conclusion

Policy discussions commonly revolve around the mechanics of implementation, rather than more fundamental notions of utility and welfare weights. This paper demonstrates how these discussions can be inverted. We provide a method to recover the primitives consistent with observed policies, using a model of preferences in conjunction with modern methods for estimating heterogeneous treatment effects, and demonstrate how to convert between welfare and allocation space.

We develop this approach and apply it to a large anti-poverty program in Mexico, to estimate the preferences consistent with the program's implementation. This analysis reveals that, after accounting for heterogeneity in treatment effects, the program's allocation placed higher weight on the welfare of poor and large families, and lower weight on indigenous households. The implied value of each missed school day and child sick day is estimated imprecisely but our confidence intervals do not rule out valuations estimated in prior work.

This framework could be used in several ways. To begin, it could be used to characterize the realized allocations of an existing program, to provide an indication of the preferences they imply. This, in turn, can provide a way to audit an existing program, to help hold policymakers accountable for past decisions – and in particular, to evaluate whether the implemented allocation reflects the stated goals of the policy. Perhaps most importantly, this approach can be used to adjust existing policies to better align with those goals.

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Appendices

A1 Generalized curvature in utility components

This section considers what will be measured if the utility functions are assumed to be linear $(\tilde{g}_j(y) = y)$ but in fact the true utility functions $g_j(y)$ have curvature. The true impact of the program on component of utility j is then:

$$\Delta v_{ij} = g_j(y_{ij}^1) - g_j(y_{ij}^0)$$

Taking a Taylor approximation from the factual level y_{ij} , we have $g_j(y_{ij} + \delta) \approx g_j(y_{ij}) + \delta \cdot g'_j(y_{ij})$. Thus for any $g_j(\cdot)$ we have:

$$\Delta v_{ij} \approx g_j(y_{ij}) - g_j(y_{ij}) + \Delta y_j(\tilde{\mathbf{x}}_i) \cdot g'_j(y_{ij}) = \Delta y_j(\tilde{\mathbf{x}}_i) \cdot g'_j(y_{ij})$$

We can then express the utility benefit of treating i as:

$$\Delta S_i \approx \underbrace{\mu(\mathbf{x}_i)g_0'(y_{i0})}_{\tilde{\mu}(\mathbf{x}_i, \{y_{i0}\})} \left[\hat{\Delta y_0}(\tilde{\mathbf{x}}_i) + \sum_j \underbrace{\lambda_j(\mathbf{x}_i)g_j'(y_{ij})}_{\tilde{\lambda}_j(\mathbf{x}_i, \{y_{ij}\})} \hat{\Delta y_j}(\tilde{\mathbf{x}}_i) \right]$$

This implies that if we do not specifically account for curvature and estimate a linear model, the welfare and impact weights we estimate ($\tilde{\mu}$ and $\tilde{\lambda}$) are approximately a combination of the underlying welfare and impact weights (μ and λ) and any curvature in the utility functions (g'_j) , as long as the baseline value of the outcome (y_{ij}) is included as a characteristic along which these weights can vary ($\tilde{\mathbf{x}}_i$). If the true utility is linear, then $\tilde{\mu}$ coincides with μ and $\tilde{\lambda}$ with λ . Otherwise, utility curvature multiplies the weights.

A2 Data Cleaning Process

The data for the evaluation of PROGRESA is composed of household survey responses from a sample of 506 villages from seven states across multiple years. Three different survey years are used: a baseline survey in October 1997, and two follow-up surveys in October 1998 and November 1999. Villages were randomly assigned to a treatment group which received the program at the beginning, and a control groups, which received it two years later. Within villages in the treatment group, a poverty index score is computed based on household income and assets, and all households meeting the score requirement are eligible to receive the program's conditional transfers.

We compute a measure of average household monthly consumption per member based on the survey responses. The October 1998 and November 1999 surveys ask households about the quantity consumed, quantity purchased and amount of money expended on 36 common food items, as well as expenditure for several nonfood categories (in weekly/monthly/semi-annual amounts). We use the information regarding quantity purchased and amount of money expended to construct householdspecific prices which are then multiplied by quantity consumed (this helps to account for the fact that households consume food that is self-produced in addition to bought). If household-specific information is missing, we use locality, municipality or state average prices (the smallest level available).

A3 Preference survey

We additionally survey Mexican residents to elicit their preferences for different allocations of social welfare programs. We solicited responses to a survey from a nationally representative sample of computer users in Mexico, through a Qualtrics survey panel.

A3.1 Survey design

After obtaining consent and an initial information screen, participants were asked their preferences for allocating benefits to different types of households. The survey was translated in Mexican Spanish. First, respondents were asked to select which attributes the government should consider when prioritizing which households receive cash transfers, from a list (age, income, household size, education, agricultural, indigenous, and gender). Second, subjects were asked to make monetary allocation decisions between different households using multiple price lists (see Figure A3 for an example). In each, one focal attribute differed between the households, and two other control attributes were held fixed. We randomized which controls were included, the order they were presented, and the scale of the tradeoff.⁹ Each subject filled in one price list for each focal attribute. Third, for a particular household, subjects were asked to make allocation decisions between money and education and child health using multiple price lists (see Figure A4). The description of the household included three randomly selected control attributes. Finally, subjects were asked for basic demographics.

A3.2 Estimation

We use the survey responses to estimate $\boldsymbol{\omega}$ and $\boldsymbol{\lambda}$:

To identify $\boldsymbol{\omega}$, compare impacts in dollars of consumption (where other impacts $\Delta g_i(x_i) = 0$). If individual *i* differs from *i'* only in attribute *j* and the crossover point

⁹Each participant saw base tradeoff numbers multiplied by 1x, 2x, or 3x, selected at random.

is $\Delta g_0(x_i) = a$ and $\Delta g_0(x_{i'}) = b$, then

$$\omega_{-j}^{x_{i,-j}}\omega_{j}^{x_{i,j}}a = \omega_{-j}^{x_{i',-j}}\omega_{j}^{x_{i',j}}b$$
$$\omega_{j} = \left(\frac{b}{a}\right)^{\frac{1}{x_{i,j}-x_{i',j}}}$$

To identify λ , now instead hold fixed individual attributes, and consider impacts on different outcomes. If the crossover point is $\Delta g_0(x_i) = a$ and $\Delta g_j(x_i) = b$ then $\lambda_j = \frac{a}{b}$.

A3.3 Validation

The design included several checks to ensure that respondents took the survey seriously. First, prior to the survey, participants were asked, 'We care about the quality of our survey data and hope to receive the most accurate measure of your opinions, so it is important to us that you thoughtfully provide your best answer to each question in the survey. Do you commit to providing your thoughtful and honest answers to the questions in this survey?' Only participants who answered 'I will provide my best answers' were invited to continue with the survey. Second, after reading the instructions, participants responded to five simple questions to validate understanding of the study. In order to complete the study, participants had to respond correctly. Third, the survey included controls to ensure that participants spent adequate time on each question. The submit button for the main exercises appeared only after a 5 second delay.¹⁰ Additionally, participants who were completing the survey too quickly (less than half the median elapsed time in the pilot survey) were removed from our sample, following a standard quality protocol used by Qualtrics. Fourth, in the final demographic survey, respondents were asked to rate the following three statements along the same Likert scale ranging from 'Strongly Disagree' to 'Strongly Agree': 'I made each decision in this study carefully', 'I made decisions in this study randomly'. and 'I understood what my decisions meant.' A careful respondent should agree with the first and last statement but disagree with the middle; agreement or disagreement with all statements reveals that a respondent made careless decisions. We restrict the

¹⁰The implementation of this in Qualtrics made it possible for participants to advance if this time had elapsed, even if a multiple price list question had not been answered. For this reason, a handful of participants did not respond to all questions.

sample to only respondents who disagreed that they had made decisions randomly.¹¹ 91% of respondents agreed with the first and last statement, and disagreed with the middle; 58% did so strongly.

There was an optional comment box at the conclusion of the survey; 49% of respondents filled in a comment, suggesting a high level of engagement with the survey. Although some respondents used the box to indicate some confusion with the selector interface, several respondent affirmatively to the approach of basing policy on resident preferences, such as (translated to English):

- 'Excellent that they do these surveys to assess the policies of support to families'
- 'I think this survey was very important since the benefits that sometimes come are the same for all people and the situations of each person are not considered. For some it may be enough but for others it is too little.'
- 'excellent survey, hopefully and we could society decide these support, because that is how we would eradicate poverty'

¹¹Apart from two pilot respondents.

A4 OLS Treatment Effect Estimates

A4.1 Estimation: OLS

One can also use linear regression to estimate heterogeneous treatment effects. We follow Djebbari and Smith (2008), allowing treatment effects to vary by age and gender composition of the household, total household size, and several characteristics of the household head: education level, indigenous status, gender, working in the agricultural sector, and age.¹² Formally, we estimate:

$$g_{ij} = \beta_0 + \boldsymbol{\beta}_{\mathbf{x}} \mathbf{x}_i + (\beta_T + \boldsymbol{\beta}_{T\mathbf{x}} \mathbf{x}_i) T_i + e_i \tag{3}$$

where g_{ij} is the endline outcome, \mathbf{x}_i is the vector of baseline covariates, and $T_i \in \{0, 1\}$ is a dummy variable for treatment status of household *i*. This model allows endline outcomes to differ systematically according to household covariates, and additionally allows the treatment effect of PROGRESA to differ across households according to their covariates.

We construct our variables for treatment effects from the predicted values from our estimated equation (3), as

$$\Delta \hat{g}_j(\mathbf{x}_i) = \hat{\beta}_T + \hat{\boldsymbol{\beta}}_{T\mathbf{x}} \mathbf{x}_i$$

A4.2 Results

On average over our sample, using OLS PROGRESA increased household log monthly consumption by 0.07, to have reduced the number of sick days per child by 0.22, and slightly increased the number of school days missed per child by 0.026 (very close to zero).

However, the effects of the program differ across households. The overall distributions of treatment effects by outcome for OLS, are presented in Figure A6. The distribution of estimated effects estimated under causal forest is tighter, in particular

 $^{^{12}}$ We depart from Djebbari and Smith (2008) in that we omit poverty scores and village marginality index and their respective interactions in the list of covariates, to avoid potential correlated errors from using these rankings in both the treatment effect estimates and in the preference-learning method.

for the schooling and health outcomes. With OLS, we see a fairly strong correlation between health treatment effect estimates and schooling treatment effect estimates, but with causal forest this correlation is much less apparent.

OLS coefficient estimates are presented in Table A4, with standard errors in parentheses. Similar to Djebbari and Smith (2008), our OLS point estimates show that log consumption treatment impacts are higher for households with indigenous status.¹³

 $^{^{13}}$ Note that our specification differs from Djebbari and Smith (2008) in that we exclude the ranking metrics from the list of covariates.

Appendix Exhibits

	October 1998 mean
Head of household:	
Is indigenous	0.41
Age	41.13
Education (HS or higher)	0.005
Is male	0.94
Is an agricultural worker	0.65
Household size	
Number of children less than 6 years old	1.97
Number of children 6-16 years old	2.81
\dots Number of adults 17+ years old	2.54
Log monthly average per capita consumption (log pesos)	5.08
Average number of days a school-age child misses school	0.32
Average number of days a young child is sick	1.07
Assigned to treatment group	0.61
Ν	6537

Table A1: Descriptive Statistics

Notes: Table shows the average levels in October 1998 of households matched to November 1999 survey sample. HS education defined as 12 years or more of education. Number of days a young child is sick, and number of days a school-age child misses school, are computed as an average over the number of children in the respective age group in the household. Sample restricted to only households with children in the targeted categories for health and schooling intervention (0-5 y.o., 6-16 y.o.) during the November 1999 survey.

	Log Consumption Monthly per capita (pesos)	Schooling # days missed school per child	Health # Sick days per child
head age	0.112	0.308	0.228
household income 97	0.198	0.163	0.263
head indigenous	0.362	0.009	0.011
num child 3 to 5 yrs	0.01	0.072	0.162
num child less than 2 yrs	0.017	0.143	0.035
num adults	0.079	0.059	0.044
num child 6 to 10 yrs	0.074	0.02	0.044
num men at least 55 yrs	0.014	0.052	0.007
head agricultural worker	0.023	0.035	0.014
num women 20 to 34 yrs	0.009	0.026	0.037
num boys 11 to 14 yrs	0.011	0.03	0.023
num men 20 to 34 yrs	0.009	0.012	0.042
num girls 11 to 14 yrs	0.013	0.014	0.031
num girls 15 to 19 yrs	0.027	0.007	0.015
num boys 15 to 19 yrs	0.016	0.007	0.02
male head of household	0.005	0.023	0.004
num women 35 to 54 yrs	0.006	0.01	0.008
num men 35 to 54 yrs	0.008	0.006	0.007
num women at least 55 yrs	0.008	0.004	0.004
head education	0	0	0
Ν	6642	6642	6642

Table A2: Feature Importance Estimates: Causal Forest

Notes: Feature importances as estimated from causal forest estimation of heterogeneous treatment impacts of PROGRESA on three outcome dimensions: log consumption (log monthly per capita consumption), schooling (number of missed school days per child), and health (number of sick days per child). Schooling and health sick days / missed school days measured over 28 days prior to survey. Estimates reflect 3 separate causal forest estimations for each respective outcome.

	Household Poverty Score		
	Observe full ranking	Observe only binary allocation	
-	Log Welfare Weights $log_{1.01}(\boldsymbol{\omega})$		
Indigenous	-12.4 (4.2)	-9.71(61.1)	
$\log(\text{Income})$	-14.3(5.4)	-8.16(32.7)	
Household Size	5.6(2.1)	3.3(18.8)	
Head Age	-1.0 (0.6)	-0.53(17.0)	
Education	-39.9(21.5)	-19.2(34.2)	
	Impact Weights λ		
Missed Schooling (per day)	-0.03(0.17)	0.02(1.26)	
Sickness (per child sick day)	$0.08 \ (0.05)$	$0.11 \ (0.07)$	
Value Regardless of Impact	0.47(3.75)	0.75(109.21)	
σ	$0.17 \ (0.17)$	0.10(0.1)	
Ν	6642	6642	

Table A3: If Only the Allocation is Observed

Notes: Both columns computed using our method, using heterogeneous treatment effects estimated with causal forest (see Figure 2). Standard errors are computed using a two-step bootstrap procedure that accounts for uncertainty in both treatment effects and preference parameters. We exclude bootstrap draws (0 draws for full ranking, 1 draw for binary ranking, out of 50 for each) that converged to corner solutions against the zero lower bound for omega.

	Log Consumption	Schooling	Health
	(Monthly avg. per	(Avg. days school	(Avg. sick days per
	person, in pesos)	missed per child)	child)
Treatment	-0.0271 (0.115)	-0.3527(0.249)	-0.8111(0.456)
Treatment X head indigenous	$0.1462 \ (0.027)$	$0.0323\ (0.058)$	$0.0389\ (0.106)$
Treatment X log(Income 1997)	-0.0027(0.02)	$0.0141 \ (0.042)$	$0.06 \ (0.077)$
Treatment X num adults	-0.0157(0.012)	$0.0134\ (0.027)$	$0.0086 \ (0.05)$
Treatment X head age	$0.0017 \ (0.002)$	$0.0067 \ (0.004)$	$0.0046\ (0.007)$
Treatment X head education	$0.0208\ (0.003)$	-0.0102(0.007)	$0.0121 \ (0.014)$
Treatment X male head of household	-0.0379(0.063)	$0.1006\ (0.137)$	$0.1513\ (0.251)$
Treatment X head agricultural worker	$0.0523\ (0.029)$	-0.11 (0.062)	-0.0803(0.114)
Treatment X num child less than 2 yrs	-0.0297(0.016)	$0.0907 \ (0.034)$	$0.0019 \ (0.063)$
Treatment X num child 3 to 5 yrs	-0.0307(0.019)	-0.0604(0.041)	$0.1187 \ (0.075)$
Treatment X num child 6 to 10 yrs	$0.0451 \ (0.015)$	$0.015\ (0.032)$	-0.0178(0.058)
Treatment X num boys 11 to 14 yrs	$0.0139\ (0.021)$	-0.0495(0.045)	-0.0218(0.082)
Treatment X num girls 11 to 14 yrs	$0.0212 \ (0.021)$	-0.0279(0.045)	$0.0315\ (0.082)$
Treatment X num boys 15 to 19 yrs	-0.024 (0.023)	$0.001 \ (0.051)$	-0.0633(0.093)
Treatment X num girls 15 to 19 yrs	-0.0243(0.023)	$0.0035\ (0.049)$	$0.0558\ (0.09)$
Treatment X num men 20 to 34 yrs	$0.0037 \ (0.027)$	-0.0224 (0.058)	-0.2424 (0.106)
Treatment X num women 20 to 34 yrs	$0.0044 \ (0.028)$	$0.0439\ (0.062)$	0.1897(0.113)
Treatment X num men 35 to 54 yrs	$0.0479\ (0.039)$	-0.0492(0.084)	$0.0115 \ (0.153)$
Treatment X num women 35 to 54 yrs	-0.0225(0.037)	$0.0198\ (0.079)$	-0.0142(0.145)
Treatment X num men at least 55 yrs	-0.0416(0.053)	-0.3011 (0.116)	-0.0174(0.212)
Treatment X num women at least 55 yrs	-0.0283(0.041)	0.0372(0.089)	-0.0739(0.163)
Baseline Covariates	X	X	X
R^2	0.180	0.0132	0.03
Ν	6642	6642	6642

Table A4: Treatment Effect Coefficient Estimates: OLS

Notes: OLS coefficients of household characteristics interacted with treatment effects on three outcome dimensions: log consumption (log monthly per capita consumption), schooling (number of missed school days per child), and health (number of sick days per child). Schooling and health sick days / missed school days measured over 28 days prior to survey. Baseline covariates here includes the covariates without interaction with treatment effects, e.g. head age, as well as a constant term.

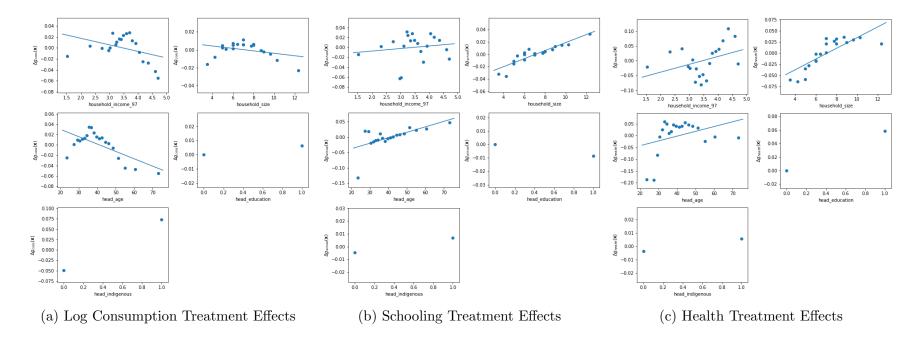


Figure A1: Binscatter Plots of Treatment Effect Heterogeneity: Causal Forest

Notes: Binscatter plots of treatment effects from causal forest over a selected group of five covariates: household size; household head education; household head indigenous status; household head age; and log household income in the pre-period of 1997. Figures shown for treatment effects over per-person monthly consumption, number of sick days per child, and number of missed school days per child. Treatment effects shown are residualized against remaining covariates in the regression (the other graphed covariates).

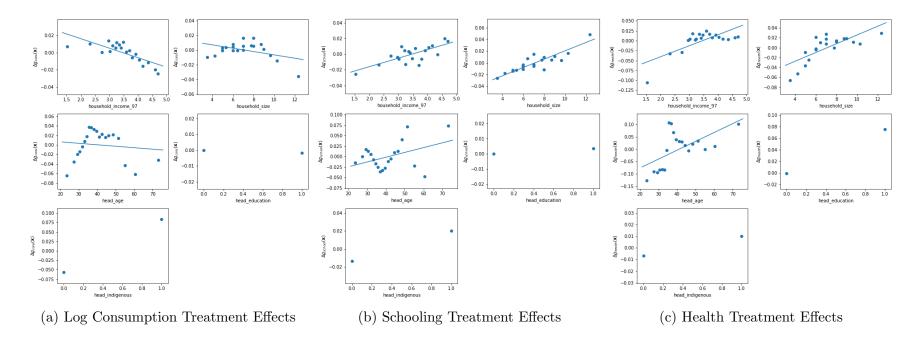
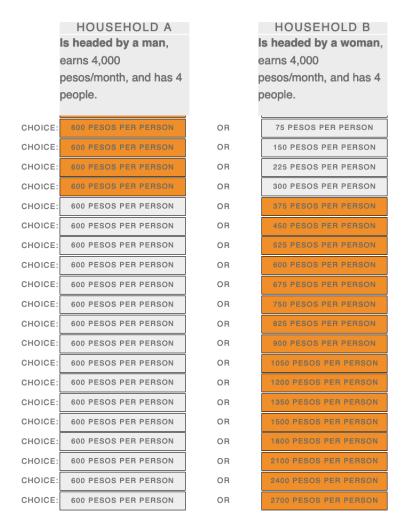


Figure A2: Binscatter Plots of Treatment Effect Heterogeneity: OLS

Notes: Binscatter plots of treatment effects from OLS over five covariates: household size; household head education; household head indigenous status; household head age; and log household income in the pre-period of 1997. Figures shown for treatment effects over per-person monthly consumption, number of sick days per child, and number of missed school days per child. Treatment effects shown are residualized against remaining covariates in the regression (the other graphed covariates).

Figure A3: Welfare Weight Survey Question Example

On each row, click on a cell to indicate whether you prefer household A to receive the benefits listed on the left hand side, or household B to receive the benefits listed the right hand side:



Notes: Respondents saw a version of this question translated into Spanish.

Figure A4: Impact Weight Survey Question Example

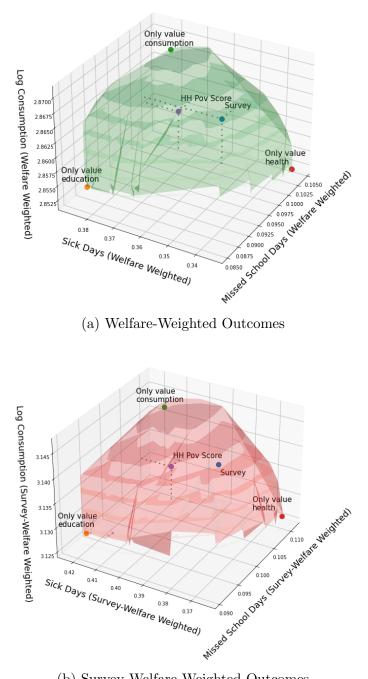
A household earns 4,000 pesos/month, has 4 people, and has a head of household that has graduated high school.

Would it be better for this household's child to be healthier, or for them to receive the amount of money shown?



Notes: Respondents saw a version of this question translated into Spanish.

Figure A5: Expected Program Impacts under Alternative Preferences, in Welfare Space



(b) Survey Welfare-Weighted Outcomes

Notes: Figure shows the frontier of outcomes resulting from all possible allocations, weighted by welfare weights. Panel (a) weights outcomes by the welfare weights consistent with the implemented PROGRESA program, derived using our method. Panel (b) uses welfare weights consistent with the inferred preferences from the implemented survey. Labeled points correspond to particular allocations described in Table 3.

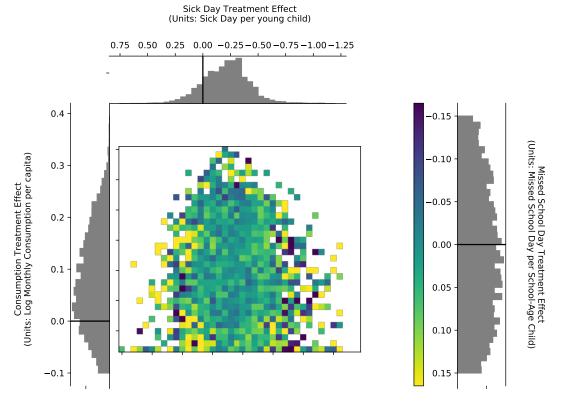


Figure A6: Distribution of Estimated Treatment Effects (OLS)

Notes: Joint and marginal distributions of estimated treatment effects of PROGRESA conditional cash transfer on schooling, health, and consumption, estimated using OLS. Schooling treatment effects are measured over the number of missed school days per school-age child in a given household. Health treatment effects are measured over the number of sick days per young (0-5 years old) child in a given household. Consumption treatment effects are measured over per-person consumption in pesos in a given household. Marginal distributions for consumption and health treatment effects are shown over the y and x axes, respectively, and are binned together in the center figure. Average schooling treatment effects in each consumption-health-treatment-effect bin is shown by the fill color of the bin, according to the index of the legend on the right. The marginal distribution of schooling treatment effects is shown in parallel to this legend. Note that missed school days and sick days are inferred to be "bads", according to our estimated weights, and so higher negative values for these treatment effects are associated with higher social utility. Note also that we drop households without children in the relevant age range for health and schooling treatment effects; the above graphs show only TEs for households for which these TEs are defined.