

DISCUSSION PAPER SERIES

DP13568

ON THE ECONOMICS OF SCIENCE PARKS

Wen-Jung Liang, Chao-Cheng Mai, Jacques-
François Thisse and Ping Wang

**INTERNATIONAL TRADE AND
REGIONAL ECONOMICS**

ON THE ECONOMICS OF SCIENCE PARKS

Wen-Jung Liang, Chao-Cheng Mai, Jacques-François Thisse and Ping Wang

Discussion Paper DP13568
Published 04 March 2019
Submitted 01 March 2019

Centre for Economic Policy Research
33 Great Sutton Street, London EC1V 0DX, UK
Tel: +44 (0)20 7183 8801
www.cepr.org

This Discussion Paper is issued under the auspices of the Centre's research programme in **INTERNATIONAL TRADE AND REGIONAL ECONOMICS**. Any opinions expressed here are those of the author(s) and not those of the Centre for Economic Policy Research. Research disseminated by CEPR may include views on policy, but the Centre itself takes no institutional policy positions.

The Centre for Economic Policy Research was established in 1983 as an educational charity, to promote independent analysis and public discussion of open economies and the relations among them. It is pluralist and non-partisan, bringing economic research to bear on the analysis of medium- and long-run policy questions.

These Discussion Papers often represent preliminary or incomplete work, circulated to encourage discussion and comment. Citation and use of such a paper should take account of its provisional character.

Copyright: Wen-Jung Liang, Chao-Cheng Mai, Jacques-François Thisse and Ping Wang

ON THE ECONOMICS OF SCIENCE PARKS

Abstract

Science parks play a growing role in knowledge-based economies by accommodating high-tech firms and providing an environment that fosters location-dependent knowledge spillovers and promotes R&D investments by firms. Yet, not much is known about the economic conditions under which such entities may form in equilibrium without government interventions. This paper develops a spatial equilibrium model with a competitive final sector and a monopolistic competitive intermediate sector, which allows us to determine necessary and sufficient conditions for a science park to emerge as an equilibrium outcome. We show that strong localized knowledge spillovers, high startup costs, skilled labor abundance, or low commuting costs make intermediate firms more likely to cluster and a science park more likely to form. We also show that the productivity of the final sector is highest when intermediate firms cluster. As the decay penalty, firms' startup and workers' commuting costs become lower, science parks will eventually be fragmented.

JEL Classification: D51, L22, O33, R13

Keywords: science parks, Knowledge Spillovers, intermediate inputs, Land use, research & development

Wen-Jung Liang - wjliang@gms.ndhu.edu.tw
National Dong Hwa University

Chao-Cheng Mai - xwizard@gate.sinica.edu.tw
Academia Sinica and Tamkang University

Jacques-François Thisse - jacques.thisse@uclouvain.be
Higher School of Economics (St Petersburg) and CEPR

Ping Wang - wangp6@gmail.com
Washington University in St. Louis

Acknowledgements

We are grateful for comments by M. Berliant, M. Fujita, E. Rossi-Hansberg, and participants at the Midwest Economic Theory Meeting, North American Regional Science Association Meeting, and the Society for Advanced Economic Theory Conference. Financial support from Academia Sinica, the National Science Council, Tamkang University, the Russian Science Foundation under the grant N° 18-18-00253, and the Weidenbaum Center on the Economy, Government, and Public Policy to enable this international collaboration is gratefully acknowledged. The usual disclaimer applies.

On the Economics of Science Parks

Wen-Jung Liang, National Dong Hwa University

Chao-Cheng Mai, Academia Sinica and Tamkang University

Jacques-François Thisse, CORE-Université catholique de Louvain,

National Research University Higher School of Economics, and CEPR

Ping Wang, Washington University in St. Louis and NBER

January 27, 2019

Abstract: Science parks play a growing role in knowledge-based economies by accommodating high-tech firms and providing an environment that fosters location-dependent knowledge spillovers and promotes R&D investments by firms. Yet, not much is known about the economic conditions under which such entities may form in equilibrium *without* government interventions. This paper develops a spatial equilibrium model with a competitive final sector and a monopolistic competitive intermediate sector, which allows us to determine necessary and sufficient conditions for a science park to emerge as an equilibrium outcome. We show that strong localized knowledge spillovers, high startup costs, skilled labor abundance, or low commuting costs make intermediate firms more likely to cluster and a science park more likely to form. We also show that the productivity of the final sector is highest when intermediate firms cluster. As the decay penalty, firms' startup and workers' commuting costs become lower, science parks will eventually be fragmented. (JEL Classification Numbers: D51, L22, O33, R13.)

Keywords: science parks, knowledge spillovers, intermediate inputs, land use, research & development.

Acknowledgments: We are grateful for comments by M. Berliant, M. Fujita, E. Rossi-Hansberg, and participants at the Midwest Economic Theory Meeting, North American Regional Science Association Meeting, and the Society for Advanced Economic Theory Conference. Financial support from Academia Sinica, the National Science Council, Tamkang University, the Russian Science Foundation under the grant N°18-18-00253, and the Weidenbaum Center on the Economy, Government, and Public Policy to enable this international collaboration is gratefully acknowledged. The usual disclaimer applies.

Correspondence: J.-F. Thisse, CORE, Université catholique de Louvain; jacques.thisse@uclouvain.be

1 Introduction

The concept of *science park* seems to have gained the favor of many analysts and policy-makers (see, e.g., Katz and Bradley, 2013). Even though the idea of industrial district has been around for a long time (Marshall, 1890, ch. X), it was not until the 1980s that the related concept of science park has been developed (Castells and Hall, 1994; Saxenian, 1994). As emphasized by Saxenian (1994, pp. 32-33 and 118-119), many firms (such as those in the Information and Communications Technology, or in short ICT, industry) clustering in the Silicon Valley produce high-tech intermediate goods and make big R&D investments, which are beneficial to all firms because ideas and knowledge can be transferred more quickly and seamlessly through various channels.¹

There is a rich variety of science parks, which is well illustrated by the many histories of parks. However, a science park is always associated with the development of a geographic area which is primarily designed (i) to accommodate high-tech firms, including particularly interrelated *intermediate firms* at various production stages, (ii) to provide an environment that fosters location-dependent *knowledge spillovers*, and (iii) to encourage *R&D investments by firms*, while researchers and high-skilled workers can be drawn from nearby universities/research institutes. A science park also offers an *urban environment* to its workers, including housing, retail, restaurants and other leisure facilities (Katz and Bradley, 2013). Using urban economic theory, we may view a science park as a monocentric city whose center is determined endogenously by the interaction between multiple stakeholders through the above-mentioned channels. Thus, there are both demand and supply forces at work in the formation of a science park.

Despite the importance of science parks in the real world (see, e.g., Link and Scott, 2003, for documenting the historical growth of U.S. science parks), it is fair to say that this concept has attracted little attention in economic theory (Link and Scott, 2007). This is where we hope to contribute by providing a full-fledged general equilibrium model that allows us to determine under which conditions a science park emerges as a *decentralized equilibrium outcome*. It is our hope that our setting will contribute to a better understanding of the formation of science parks and will allow for a more precise quantification of their economic consequences and a better evaluation of relevant policies.

To achieve our goal, we develop a model that captures the following basic features: (i) a

¹See Arzaghi and Henderson (2008), Buzart *et al.* (2017), Cassi and Plunket (2015), Greenstone *et al.* (2010), as well as critical reviews by Audretsch and Feldman (2004) and Carlino and Kerr (2015).

composite consumption good is produced by using production-line designers and an endogenous range of inputs provided by intermediate firms; (ii) workers are hired to produce intermediate goods or to conduct R&D in the intermediate sector; (iii) the productivity of intermediate firms may be enhanced by R&D investments and inter-firm spillovers, the intensity of which depends on how intermediate firms are distributed across space; and (iv) workers and intermediate firms are spatially mobile. Firms' R&D investments and the existence of knowledge spillovers determine the agglomeration force. On the other hand, the clustering of firms increases the average commuting distance of workers which, in turn, gives rise to higher wages and land rent in the residential area surrounding the cluster. Such high wages and land rents act as a dispersion force. The equilibrium distribution of firms and workers is determined as the balance between these two opposite forces.

The main tenet of this paper is that *the emergence and efficiency of a science park is intimately related to the spatial structure of the area that hosts it*. More specifically, we view a science park as a spatial cluster formed by firms which interact to determine endogenously the intensity of knowledge spillovers. Such a city structure accommodates the largest number of researchers and the highest level of R&D. Recall that the clustering of firms is also associated with other agglomeration economies, such as a large pool of high-skilled and specialized workers and the provision of knowledge-intensive business services and sophisticated infrastructures, which enhances firms' productivity.² To understand better how these various forces interact to give rise to a science park, we consider the other extreme of the spectrum, i.e., a city where activities are dispersed across locations and the level of R&D is low. In this paper, we determine the conditions under which a city *with* or *without* a science park is formed.

Our main results may be summarized as follows. We begin by identifying necessary and sufficient conditions for a science park to emerge as an equilibrium outcome. These conditions show that the efficiency of both the intermediate and final sectors varies with the spatial distribution of firms and workers. This in turn will allow us to uncover the reasons explaining why science parks may or may not be formed. In particular, we identify three key rationales for firms to have incentives for clustering in a science park: (i) location-dependent knowledge decays, (ii) costly startup, and (iii) skilled labor abundance. These are all typical features of new high-tech industries that make a science park, which accommodates more intermediate firms and fosters research activities, more likely to emerge. This may explain

²For surveys, see Duranton and Puga (2004), Rosenthal and Strange (2004), and Combes and Gobillon (2015).

why firms bearing high innovation costs are often clustered in science parks such as the Silicon Valley, the Hsinchu Science-Based Industrial Park in Taiwan or the Cambridge Science Park in the U.K. (Saxenian, 1994; Chen, 2008; Helmers, 2019). A science park is also more likely to emerge when spillovers are strongly localized. Thus, unlike what some analysts and development agencies believe, simple cluster policies are not sufficient for a science park or a local innovative system to develop (see Duranton *et al.*, 2010, for a critical appraisal of such policies).

Even though our model is static, it captures an important dynamic feature which is worth emphasizing. Indeed, knowledge spillovers being crucial in the formation of science parks, our results suggest that knowledge-based economies are likely to be those in which these parks emerge. However, knowledge spillovers are both local and global in scope. Beyond a certain threshold the role of distance becomes secondary, as the most innovative firms are increasingly combining their local knowledge potential with a high level of international connectivity associated with the development of new communication devices. In this case, we may expect cities with a more dispersed pattern of innovation to emerge. When such developments are not strong enough, science parks would remain to be centralized.

Related literature. A handful of related models have been developed in urban economics. Their common aim is to explain the emergence of business centers within cities. They include O’Hara (1977), Ogawa and Fujita (1980), Fujita and Ogawa (1982), Berliant *et al.* (2002), and Lucas and Rossi-Hansberg (2002). However, these models focus on gravity-like reduced forms in which knowledge spillovers and/or spatial externalities are mechanically presumed. They ignore firms’ R&D policies and the supply of intermediate inputs and knowledge-intensive business services, which affect the overall productivity of firms. Although spatial externalities have attracted a lot of attention in urban economics (see Carlino and Kerr, 2015, for a survey), we are not aware of a microeconomic model developed to investigate how spatial externalities emerge from intentional firms’ R&D and location decisions. Our paper may thus be viewed as an attempt to penetrate the black box of spatial externalities in a setting that take firms’ behavior as the driving force.

The remainder of the paper is organized as follows. The model is presented in Section 2, while Section 3 describes the optimizing conditions of the different groups of agents. Our equilibrium concept is defined in Section 4. The necessary and sufficient conditions for a science park to emerge are derived and its properties are characterized in Section 5. Section 6 concludes.

2 The model

We consider a small open economy, which consists of (i) a featureless one-dimensional space Z , (ii) two sectors, one producing the final good and the other producing intermediate inputs, and (iii) three production factors, i.e., land, capital and labor. The economy is populated by a continuum H of workers. Land is owned by absentee landlords. Without loss of generality, the land density and the opportunity cost of land are normalized to one.

Workers are used to enhance the efficiency of the intermediate sector by performing the following three tasks: (i) to undertake firm-specific R&D, (ii) to design the production line in the final sector, and (iii) to produce intermediate goods. A unit mass of firms produce the final good, which is homogeneous and sold to the larger economy at a given price; this good is chosen as the numéraire. Intermediate firms and workers are mobile and consume a fixed amount of land normalized to one. The final and intermediate goods are shipped within the city at no costs, thus implying that the prices of intermediate goods are independent of where intermediate and final producers are located. Dealing with shipping costs is fairly straightforward and does not add much to our results. Since our focus is on the intermediate sector, it is convenient to assume that the final producers are located and do not consume land.

Apart from land, workers consume only the final good. Each worker is endowed with one unit of labor that she supplies inelastically. Commuting costs are crucial for the city shape. Commuting between the residence $y \in Z$ and workplace $z \in Z$ requires $t|y - z|$ units of the numéraire., where $t > 0$ measures the unit commuting cost..

2.1 The spatial structure of the economy

In this paper, we focus on the following two configurations.

- (i) The agglomerated configuration (denoted $j = A$) features a science park where all firms are clustered, which is flanked by two residential areas.
- (ii) The dispersed configuration (denoted $j = D$) features workers and intermediate firms that cohabit at each location. Firms and workers are uniformly distributed across the city. We refer to such a configuration as a *flat city*.

Since each worker and each firm consumes one unit of land, the total demand for land is equal to $N + H$ where N is the exogenously given mass of intermediate firms. Therefore, the

city is given by the interval

$$Z = \left[-\frac{N+H}{2}, \frac{N+H}{2} \right],$$

which implies that the city size varies with the mass of intermediate firms. As will be seen, the spatial extent of a high-tech city depends on the way the intermediate sector is spatially organized.

(i) In the agglomerated configuration, there are N intermediate producers who are uniformly distributed within the science park whose spatial extend is given by

$$Z_A^F = [-N/2, N/2],$$

with density $h_A^F = 1$. Workers are uniformly distributed over the residential area

$$Z_A^W = \left[-\frac{N+H}{2}, -\frac{N}{2} \right] \cup \left[\frac{N}{2}, \frac{N+H}{2} \right]$$

with density $h_A^W = 1$.

(ii) In the dispersed configuration, there are N_D^* intermediate firms while both the firm and worker densities are uniform across the city. Since the total demand for land is $N+H$, the worker density is equal to $h_D^W = H/(N+H)$, while the firm density is $h_D^F = N/(N+H)$.

2.2 The intermediate sector

The *intermediate sector* supplies a range of differentiated inputs produced under monopolistic competition and constant returns, using both labor and land. The productivity of intermediate firms is also affected by a spatial externality according to details that will be made clear below. Since there is a one-to-one correspondence between firms and intermediate goods, we can use $i \in [0, N]$ to describe an intermediate good and its producer.

Consider a firm located at $z \in Z$ and producing good $i \in [0, N]$ by using one unit of land, $K(i, z)$ units of capital, and $L(i, z)$ units of labor. Under the configuration j , firm i produces the quantity $x_j(i, z)$ of good i at location z according to a Cobb-Douglas technology:

$$x(i, z) = A_j(i, z)K(i, z)^\alpha L(i, z)^\beta l^{1-\alpha-\beta} \quad (1)$$

with $\beta \in (0, 1-\alpha)$ and $l = 1$.

Two remarks are in order. First, ignoring $A_j(i, z)$, the production function displays constant returns with respect to all private inputs, labor, capital and land. Second, the total

factor productivity (TFP) of an intermediate firm, A_j , is given by a Cobb-Douglas aggregator of the firm's R&D employment $R(i, z)$ and a *spatial externality* $\bar{R}S_j(z)$ that combines a Romer-Lucas external effect weighted by a spatial decay function:

$$A_j(i, z) = [R(i, z)]^\theta [\bar{R}S_j(z)]^{1-\theta}, \quad (2)$$

where \bar{R} is the mass of workers involved in R&D activities, while $\theta \in (0, 1)$. Our definition of the TFP captures Romer's idea that externalities enter the system through an aggregator of individual firms' decisions, while firm i 's TFP is also influenced by this firm's R&D policy.

One of the distinctive features of our setting is that a firm's TFP is endogenized through the following three channels: (i) the number of researchers hired to conduct R&D in each firm, (ii) the total number of researchers working the economy, and (iii) the spatial distribution of firms/researchers. This modeling strategy is consistent with the idea that spillovers increase the level and productivity of R&D investments (Aghion and Jaravel, 2015; Helmets, 2019). It is also in line with Chyi *et al.* (2012) who find that knowledge spillovers are especially strong across intermediate firms located in science parks. That said, it is worth stressing that *what distinguishes a science park from a conventional city center is the presence of the endogenous R&D shifter $R^\theta \bar{R}^{1-\theta}$ in (2)*. In this context, the efficiency of an intermediate firm depends on its level of R&D activities, as well as on the total mass of researchers whose productivity rises with their number (this was highlighted by Romer, 1986, and Lucas, 1988). While the urban economics literature highlights the existence of various types of agglomeration economies, the impact of the spatial structure on the endogenous R&D shifter $R^\theta \bar{R}^{1-\theta}$ is often overlooked although its importance is stressed by empirical evidence (e.g., Siegel *et al.*, 2003).

In (2), the spatial externality is generated by both the size of the researcher pool in the intermediate sector (\bar{R}) and the spatial distribution of intermediate firms (S_j). More specifically, the interfirm spillover effect is defined by the following expression (Berliant *et al.*, 2002):³

$$S_j(z) \equiv S_{\max} - (z - \mu_j)^2 - \varepsilon\sigma_j^2, \quad (3)$$

where $S_{\max} > 0$ is assumed to be sufficiently high for the function S_j to be positive over the whole city, while $\varepsilon > 0$ measures the distance-decay effect generated by the dispersion of firms. Under the configuration j , μ_j denotes the mean of the distribution of firms over Z_j^F :

$$\mu_j = \int_{Z_j^F} zh_j^F dz,$$

³Ogawa and Fujita (1980) work with spillovers linear in distance, while Fujita and Ogawa (1982) and Lucas and Rossi-Hansberg (2002) follow a similar approach but use an exponential distance-decay function.

while σ_j is the absolute dispersion given by

$$\sigma_j = \frac{2}{N_j} \int_{Z_j^F} |z - \mu_j| h_j^F dz.$$

The specification (3) satisfies the following desirable properties: (i) S_j is consistent with the idea that the intensity of spillovers varies with the firm's location and the whole distribution of firms, (ii) S_j is allowed to decrease at an increasing rate with the overall dispersion of intermediate firms, and (iii) the more concentrated firms are, the more effective knowledge spillovers will be.

Since we will focus on symmetric firm distributions, we set $\mu_j = 0$ for $j = A, D$. In the case of an agglomerated configuration ($j = A$), we have

$$\sigma_A = \frac{4}{N} \int_0^b z dz = \frac{N}{2}. \quad (4)$$

Under a dispersed configuration ($j = D$), it is readily verified that the absolute dispersion is given by

$$\sigma_D = \frac{4}{N} \int_0^{\frac{H+N}{2}} \frac{N}{H+N} z dz = \frac{H+N}{2}. \quad (5)$$

The expressions (4)-(5) imply that *the intensity of the spillover effect changes with the spatial organization of the intermediate sector* in a nontrivial way. Indeed, the mass of intermediate firms affects the value of the dispersion index, which in turn affects firms' behavior.

With these, we are able to write out the expression S_j for each configuration for any given reference location z :

$$\begin{aligned} S_A(z) &\equiv S_{\max} - z^2 - \varepsilon \left(\frac{N}{2} \right)^2, \\ S_D(z) &\equiv S_{\max} - z^2 - \varepsilon \left(\frac{H+N}{2} \right)^2 < S_A(z). \end{aligned}$$

While $S_j(z)$ is decreasing in knowledge decay ε for $j = A, D$, the effect of N_j on $S_j(z)$ depends on the configuration j . In the case of an agglomerated configuration, $S_A(z)$ is independent of the mass H of workers. However, in the case of a dispersed configuration, a higher H lowers $S_D(z)$ for all locations because the intensity of the knowledge decay effect rises with the city size.

Finally, to operate an intermediate firm must incur a startup cost which is proportional to the average capital invested in the local economy, i.e., $F \equiv f\bar{K}/N$ where $f > 0$ measures

the magnitude of the startup cost and \bar{K} the total amount of capital invested in the area when the rate of return is ρ .

In sum, *the efficiency of the intermediate and final sectors is herein endogenized through the R&D activities undertaken by intermediate firms and the size of the researcher pool, which both vary with the spatial configuration adopted by firms and workers.*

Because workers bear commuting costs, the equilibrium wage rate $w_j(z)$ is location-specific. The immobility of land implies that the land rent $r_j(z)$ is also location-specific. By contrast, the capital rental ρ is determined in the larger economy and constant across all locations. Taking wages and land rents as given, firm i chooses its location, output price, capital input, and the numbers of workers allocated to its production and R&D activities to maximize profits:

$$\pi_j(i, z) = p_j(i, z)x_j(i, z) - \rho K(i, z) - w_j(z) [R(i, z) + L(i, z)] - r_j(z) - F. \quad (6)$$

2.3 The final sector

The *final sector* consists of a unit mass of identical and perfectly competitive producers. Firms belong to absentee shareholders. Under a quasi-concave technology, they produce a homogeneous composite good consumed by workers or traded in the larger economy in exchange of other consumption goods, using intermediate goods. Following Becker and Murphy (1992), we acknowledge that combining new and specialized inputs limits the division of labor within the final sector. More specifically, we assume that (i) final producers must hire designers whose job is to coordinate the use of a large number N of intermediate goods in the production process and (ii) the number of designers rises with the number of intermediates. In this model, this is done by assuming that the final sector also employs

$$M = \phi_j N \quad (7)$$

workers, where $\phi_j > 0$ is the production-line designer requirement needed to use one additional intermediate input under the configuration j . Since coordination costs typically rise with the dispersion of intermediate firms, we find it natural to assume that $\phi_A < \phi_D$.

For any given N , the production function of a final producer is as follows (Peng *et al.*, 2006):

$$Y = \delta \int_0^N x(i) di - \frac{\eta}{2} \int_0^N [x(i)]^2 di - \frac{\gamma}{2} \left[\int_0^N x(i) di \right]^2, \quad (8)$$

The parameters in this expression are such that $\delta > 0$, $\eta > 0$ and $-\eta < \gamma$ where the inequality must hold for the production function to be concave. To illustrate the role of N ,

suppose that the final sector uses a total mass of Nx of intermediate goods. If the use of intermediate inputs is uniform over $[0, q]$ and zero on $(q, N]$, then the density on $[0, q]$ is Nx/q . Expression (8) evaluated for this consumption pattern is

$$Y(q) = \delta Nx - \frac{\eta}{2q} N^2 x^2 - \frac{\gamma}{2} N^2 x^2, \quad (9)$$

which is strictly increasing in q since $\eta > 0$. Hence, regardless of the values of x and N , (9) is maximized at $q = N$ where *input variety* is maximal. We may thus conclude that the output of the final sector is higher when production involves a higher number of intermediate inputs. In (8), α expresses the intensity of production for the intermediate goods. Our production function exhibits enough flexibility to account for fairly contrasted patterns of intermediate goods since, for a given value of η , these goods are substitutes (resp., complements) when $\gamma > 0$ (resp., $-\eta < \gamma < 0$). Note that the input variety effect is stronger when the intermediate inputs are complements, rather than substitutes, because the third term in the right hand side (9) is now positive. The production function (8) has additional features that are suitable to this study: (i) it allows for variable markups incurred by intermediate producers and (ii) it yields analytically solvable input demands and intermediate goods prices.

Taking both the wage rates and the prices of intermediate goods as given, the final sector firms located at $z = 0$ maximize profits given by

$$\Pi_j = Y - \int_0^N p_j(i)x(i)di - w_j(0)\phi_j N,$$

subject to (8). Note that $w_j(0)\phi_j N$ has the nature of an endogenous fixed cost, which depends on the mass of intermediate goods.

2.4 Workers

Each worker chooses her residential site y and workplace z . Since workers' utility is increasing in the final good consumption, maximizing consumption amounts to maximizing her net income given by

$$\max_{y,z} I_j(y, z) = w_j(z) - t|y - z| - r_j(y). \quad (10)$$

At the residential equilibrium, workers reach the same utility level, whence earn the same net income I_0 :

$$I(y, z) = I_0, \quad (11)$$

where I_0 is endogenous. This condition implies that a worker has no incentive to change either her residential or working places.

Labor is allocated to the following three activities:

- (i) the mass M of workers involved in designing the supply chain of the final sector,
- (ii) the mass \bar{R} of workers involved in R&D activities, and
- (iii) the mass $\bar{L} \equiv \int_0^N L(i)di$ of workers producing the intermediate goods.

Labor market clearing implies the following condition:

$$H = M + \bar{R} + \bar{L}. \quad (12)$$

3 The programs of firms and workers

In this section, we solve the equilibrium conditions for the final and intermediate producers, as well as for workers.

3.1 The final sector

Since shipping inputs to the final sector is costless, the price of an input is the same throughout within the city. Therefore, the optimization conditions for the final sector firms may be written as follows:

$$\begin{aligned} \frac{dY}{dx(i)} &= p(i), \\ \frac{dY}{dN} &= w_j(0)\phi_j + p(N)x(N), \end{aligned} \quad (13)$$

while differentiating (8) implies

$$\frac{dY}{dx(i)} = \delta - \eta x(i) - \gamma \int_0^N x(k)dk, \quad (14)$$

$$\frac{dY}{dN} = \left[\delta - \frac{\eta}{2}x(N) - \gamma \int_0^N x(k)dk \right] x(N), \quad (15)$$

where we do not label variables by the configuration j whenever it does not cause confusion. Thus, the final sector's inverse demand for the intermediate good i is independent of firm i 's location:

$$p(i) = \delta - \eta x(i) - \gamma \int_0^N x(k)dk. \quad (16)$$

The above expressions can be combined to yield the following two expressions:

$$\begin{aligned} p(i) - p(N) &= -\eta [x(i) - x(N)] \\ x(N) &= \sqrt{\frac{2w_j(0)\phi_j}{\eta}}, \end{aligned} \quad (17)$$

where $x(N)$ is obtained by plugging (13) into (15) and using (16). Thus, the final sector's demand for the intermediate good i becomes:

$$x(i) = \sqrt{\frac{2w_j(0)\phi_j}{\eta}} - \frac{1}{\eta} [p(i) - p(N)].$$

3.2 The intermediate sector

We now turn to the optimization program of intermediate firms. An intermediate firm i at location z determines the mass of research and production workers, output price and location conditional upon the final producers' inverse demands (16) and input prices. Since an intermediate firm has a single location, there is no need to label intermediate goods by their production sites.

It follows from (16) that

$$\begin{aligned} \frac{d[p(i)x(i, z)]}{dx(i, z)} &= p(i) + x(i, z) \frac{d}{dx(i, z)} \left[\delta - \eta x(i, z) - \gamma \int_0^N x(k, z) dk \right] \\ &= p(i) - (\eta + \gamma) x(i, z). \end{aligned}$$

Using the first-order condition (14) and the production function (8), we obtain:

$$\frac{dY}{dx(i, z)} = \delta - \eta x(i, z) - \gamma \int_0^N x(k, z) dk = p(i, z).$$

We may then derive the profit-maximizing conditions with respect to $R(i, z)$, $K(i, z)$, $L(i, z)$, and z :

$$\theta \frac{x(i, z)}{R(i, z)} [p(i) - (\eta + \gamma) x(i, z)] = w_j(z), \quad (18)$$

$$\alpha \frac{x(i, z)}{K(i, z)} [p(i) - (\eta + \gamma) x(i, z)] = \rho, \quad (19)$$

$$\beta \frac{x(i, z)}{L(i, z)} [p(i) - (\eta + \gamma) x(i, z)] = w_j(z), \quad (20)$$

$$-2(1 - \theta) \frac{zx(i, z)}{S_j(z)} [p(i) - (\eta + \gamma) x(i, z)] = \frac{dw_j(z)}{dz} [R(i, z) + L(i, z)] + \frac{dr_j(z)}{dz}. \quad (21)$$

The first three expressions are standard. The last one means that, by moving away from the mean location, a firm incurs a decrease in the benefit generated by spillovers, which is exactly compensated by a decrease in wage and land rent. This condition is the counterpart of the Alonso-Muth equation obtained in the monocentric city model of urban economics (Fujita, 1989).

We can combine these various conditions to obtain the following conditions:

$$\frac{R(i, z)}{L(i, z)} = \frac{\theta}{\beta}, \quad (22)$$

$$\frac{K(i, z)}{L(i, z)} = \frac{\alpha w_j(z)}{\beta \rho}, \quad (23)$$

$$\frac{dr_j(z)}{dz} = -\frac{L(i, z)}{\beta} \left[2(1 - \theta) \frac{w_j(z)z}{S_j(z)} + (\theta + \beta) \frac{dw_j(z)}{dz} \right]. \quad (24)$$

The first condition means that the research-labor ratio is equal to the ratio of their output elasticities, while the second states that the capital-labor ratio is inversely proportional to their price ratio. The third condition implies that the land rent gradient depends negatively on the wage gradient (dw_j/dz). If the wage gradient is positive and steeper, then the land rent gradient must be negative and steeper to dampen firms' cost. Furthermore, the land rent gradient is flatter when the spillover S_j is stronger because the benefit for firms to cluster is higher. Since the left-hand side of (20) is U-shaped, only the upward-sloping segment satisfies the second-order condition for profit maximization and describes the supply schedule of the intermediate good i .

Using (18)-(20), the maximum profit earned by firm i located at z is given by

$$\pi_j^*(i, z) = \frac{\Theta}{\beta} w_j(z) L(i, z) + (\eta + \gamma) [x(i, z)]^2 - r_j(z) \quad (25)$$

where

$$\Theta \equiv 1 - \alpha(1 + f/\rho) - \beta - \theta.$$

It follows from (25) that a higher Θ gives rise to a higher markup to intermediates. Note also that the intermediates find it profit-maximizing to undertake R&D activities if and only if $\Theta > 0$. This inequality shows that θ cannot be too large for firms to invest in R&D, i.e., firms must enjoy a sufficiently strong externality in R&D.

Since firms are symmetric and mobile, they earn identical equilibrium profits π_j^* . Therefore, using (25), the maximum bid that firm i can offer to set up at z , denoted by $r_j^F(z)$, is derived from the zero-profit condition $\pi_j^* = 0$:

$$r_j^F(z) = \frac{\Theta}{\beta} w_j(z) L(i, z) + (\eta + \gamma) [x(i, z)]^2. \quad (26)$$

Observe that an intermediate firm's bid rent is negatively affected by the level of startup cost f . Therefore, f does not pin down the equilibrium mass of firms but their bid rent at each location.

3.3 Workers

It is convenient to define a mapping J_j from Z to Z associating a (potential) job site $J_j(y) = z$ with a (potential) residential location y . This mapping J_j describes the commuting pattern of workers. More specifically, a worker residing at y works at the location $J_j(y) = z$ that maximizes her net income:

$$w_j[J_j(y)] - t|y - J_j(y)| = \max_{z \in Z} [w_j(z) - t|y - z|], \quad y \in Z. \quad (27)$$

Solving workers' program is straightforward. More specifically, the maximum bid a worker can offer to reside at location y is given by

$$r_j^W(y) = \max_z \{w_j[J_j(y)] - t|y - J_j(y)| - I(y, J_j(y)) \mid I(y, J_j(y)) = I_0\}. \quad (28)$$

Combining (10) and (11) with (28), we obtain

$$r_j^W(y) = w_j(z) - t|y - J_j(y)| - I_0, \quad (29)$$

which is linear and downward slopping.

4 The spatial equilibrium

We describe the concept of spatial equilibrium in two stages. In Stage 1, we determine the mass of intermediate firms or, equivalently, the boundaries of the city. In Stage 2, given N , we pin down the equilibrium configuration j . Solving backward, we first determine the equilibrium configuration for given N . We then turn to Stage 1, solving for the equilibrium mass of intermediate firms.

Definition 1. A *spatial equilibrium* is defined by the quantity vector $\{K_j, L_j, R_j, x_j, Y_j, N_j\}$, price vector $\{p_j, w_j(z), r_j(z)\}$, and population densities $\{h_j^F(z), h_j^W(z)\}$ for $z \in Z$, together with the sets of firm and worker locations Z_j^F and Z_j^W such that the following conditions are satisfied:

- (i) profits are zero in the final and intermediate sectors;
- (ii) the sets of intermediate firm and worker locations are such that $Z_j^F = \{z \in Z \mid h_j^F(z) > 0\}$ and $Z_j^W = \{z \in Z \mid h_j^W(z) > 0\}$ under the commuting function $J_j(y)$;
- (iii) land and labor markets clear;
- (iv) market clearing for intermediate goods pins down the mass of intermediate firms;
- (v) population constraint: $\int_{Z_j^W} h_j^W(z) dz = H$.

The Walras Law implies that the final good market clears.

4.1 Stage 2. The market outcome under a given mass of intermediates

We first characterize the equilibrium when the mass of intermediate goods is given and equal to N . To produce clear-cut comparative results, we focus on symmetric firm distributions around the city center. For every $z \in Z_j^F$ and $j = A, D$, (7), (12) and (22) imply that the equilibrium number of production workers and researchers is the same at every location z and given by the expressions:

$$L_j^*(N) \equiv \frac{\beta}{\theta + \beta} \left(\frac{H}{N} - \phi_j \right), \quad (30)$$

and

$$R_j^*(N) \equiv \frac{\theta}{\theta + \beta} \left(\frac{H}{N} - \phi_j \right) = \frac{\theta}{\beta} L_j^*(N). \quad (31)$$

In other words, for a given configuration, *intermediate firms have the same number of researchers regardless of their location z* . Furthermore, the higher the elasticity of a firm's TFP with respect to its own R&D investment, the higher the number of researchers employed by this firms. To put it differently, as the spatial externality matters less ($\theta \uparrow$), each firm invests more in R&D, which makes the R&D shifter NR_j^* stronger.

The above expressions also show that a given configuration is associated with a particular allocation of workers between the intermediate and final sectors, as well as between research and production activities within the intermediate sector. Clearly, we have:

$$L_A^*(N) > L_D^*(N) \quad R_A^*(N) > R_D^*(N) \quad M_A^*(N) < M_D^*(N).$$

Thus, for any given mass of intermediate firms, there are more production workers and more researchers, hence fewer designers, in a city with a science park than in a city without a science park.

Since L_j^* and R_j^* are independent of z , the city is geographically symmetric and centered at $z = 0$. Consequently, we can restrict ourselves to the right half of Z . However, note that (23) implies that $K_j^*(z)$ is proportional to $w_j^*(z)$ and, therefore, location-specific. In other words, firms' output and capital differ across locations. In particular, plugging (2) and (23) into (1) yields the equilibrium output of an intermediate firm at z :

$$x_j^*(z) = \left[\frac{\alpha w_j(z)}{\beta \rho} \right]^\alpha (L_j^*)^{\alpha+\beta} R_j^\theta [\bar{R}_j S_j(z)]^{1-\theta}, \quad (32)$$

which varies with z through the wage rate and the spillover effect.

For the intermediate producers to be able to undertake R&D activities, it is required that

$$\Theta \equiv 1 - \alpha(1 + f/\rho) - \beta - \theta > 0.$$

This constraint becomes more binding when f increases, but less binding when ρ increases. Furthermore, θ cannot be too large, that is, firms enjoy a sufficiently strong externality $[\bar{R}_j S_j(z)]^{1-\theta}$, for otherwise they do not undertake R&D. This result is in the spirit of Romer's (1990) growth model.

Substituting the above expressions in the bid-rent function (26), which solves the zero-profit condition, leads to the following expression:

$$r_j^F(z) = \frac{\Theta}{\beta} w_j(z) L_j + (\eta + \gamma) \left\{ \left[\frac{\alpha w_j(z)}{\beta \rho} \right]^\alpha L_j^{\alpha+\beta} R_j^\theta [\bar{R}_j S_j(z)]^{1-\theta} \right\}^2. \quad (33)$$

This shows that the bid rent of an intermediate firm at z depends upon the wage it pays at this location, while stronger spillovers at z allow this firm to bid higher. It follows from (30) and (31) that a higher number of intermediate goods leads firms to produce more and to pay more for a location because of the magnification effect of spillovers generated by the R&D shifter.

The equilibrium land rent $r_j^*(z)$ is the upper envelope of the two bid rent functions $r_j^F(z)$ and $r_j^W(z)$. In other words, whenever a firm or a worker locates at z , its bid rent must be

equal to the equilibrium land rent:

$$\begin{aligned}
r_j^*(z) &= \max \{r_j^F(z), r_j^W(z), 1\} \\
r_j^*(z) &= \begin{cases} r_j^F(z) & \text{if } h_j^F(z) > 0 \\ r_j^W(z) & \text{if } h_j^W(z) > 0 \end{cases} \\
r_j^*(-(N_j + H)/2) &= r_j^*((N_j + H)/2) = 1,
\end{aligned} \tag{34}$$

where the bid rents $r_j^W(z)$ and $r_j^F(z)$ are given by (29) and (33), respectively. Moreover, when a location is populated with firms and workers, we must have $r_j^F(z) = r_j^W(z) = r_j^*(z)$.

4.2 Stage 1. The equilibrium mass of intermediate firms

We now focus on the determination of the equilibrium number of intermediate firms, and hence the equilibrium boundaries of the city. Setting $z = 0$ in (32) and using (17), (30) and (31), the equilibrium value of N under the configuration j is pinned down by the intermediate goods market clearing condition:

$$\frac{(H - \phi_j N)^{1+\alpha+\beta}}{\phi_j^{1/2} N^{\alpha+\beta+\theta}} = \left(\frac{2}{\eta}\right)^{1/2} \frac{\rho^\alpha (\theta + \beta)^{1+\alpha+\beta}}{\theta \alpha^\alpha \beta^\beta} \frac{1}{(S_{\max})^{1-\theta}} [w_j(0)]^{1/2-\alpha}. \tag{35}$$

Thus, the equilibrium wage prevailing at the city center ($w_j(0)$) and the equilibrium city size ($H + N_j$) are interdependent. In order to obtain an analytical solution for the equilibrium rent and wage schedules, we consider the special case where $\alpha = 1/2$. It is worth noting here that Acemoglu and Guerrieri (2008) found that the capital intensity of a high-tech industry such as ICT is about 0.53 in the U.S. over 1948-2005. Moreover, we have solved the model numerically for different values of $\alpha \neq 1/2$, confirming the robustness of our findings (see Appendix D).

Under $\alpha = 1/2$, which will be assumed to hold throughout the paper, (35) simplifies to:

$$\frac{(H - \phi_j N)^{3/2+\beta}}{\phi_j^{1/2} N^{1/2+\beta+\theta}} = 2 \left(\frac{\rho}{\eta}\right)^{1/2} \frac{(\theta + \beta)^{3/2+\beta}}{\theta \beta^\beta} \frac{1}{(S_{\max})^{1-\theta}}. \tag{36}$$

The right-hand side of this expression is now a positive constant independent of the configuration j . Since the left-hand side of this expression is strictly decreasing in N and has the horizontal axis as an asymptote when $N \rightarrow \infty$, the above equation has a single solution denoted $N_j^* > 0$ for $j = A, D$. Observe that, regardless of the configuration j , N_j^* is independent of the value of f , hence of the fixed cost F . This is to be contrasted with

most economic geography models where the mass of firms is pinned down by the level of fixed cost. Furthermore, when capital is more expensive ($\rho \uparrow$), then N_j^* decreases in both configurations. Similarly, when the input variety effect gets stronger ($\eta \downarrow$), the mass of intermediates decreases. By contrast, when the spillover effect is stronger ($S_{\max} \uparrow$) and the mass of workers higher ($H \uparrow$), the mass of intermediate firms rises.

Since $\phi_A < \phi_D$, *the mass of intermediate firms is higher in a city with a science park than in a city without it* ($N_A^* > N_D^*$). Observe that

$$\frac{(H - \phi N)^{3/2+\beta} \phi^{\beta+\theta}}{(\phi N)^{1/2+\beta+\theta}} = \frac{(H - \phi N)^{3/2+\beta}}{\phi^{1/2} N^{1/2+\beta+\theta}}.$$

It follows from (36) that $\phi_j N_j^*$ increases with ϕ_j . As a result, $\phi_A < \phi_D$, (7) and (12) imply that *the science park hosts more researchers and production workers than the flat city*. By implication, the final sector is more productive when a science park is formed because more intermediate inputs are available while fewer designers are required. In other words, the final sector benefits from a finer division of labor when a science park exists. This may explain why it is rewarding for a city to host a science park, as suggested by the empirical evidence provided by Delgado *et al.* (2012). Furthermore, combining (31) and (36) shows that *each firm hires fewer researchers*. In sum, even though each firm employs fewer researchers in a science park, this one involves a larger number of researchers. Since it accommodates more intermediate firms, the size of the city that hosts a science park is larger than that of a city without a science park. Note also from (36) that an increase in total labor (H) raises the number of intermediate firms and of researchers.

Summarizing yields the following proposition.

Proposition 1 (Agglomeration and size). *A city with a science park hosts more researchers and production workers, but fewer designers, than a flat city. Furthermore, the intermediate sector involves more firms while the final sector is more productive with a science park than without it. Last, a larger pool of high-skilled workers leads to a bigger science park.*

4.3 Bid rent and wage schedules

It remains to determine firms' bid rent and wage schedules. By setting $\alpha = 1/2$, the right hand side of (33) becomes linear in $w_j(z)$, so that

$$\frac{w_j(z)}{r_j^F(z)} = \frac{\beta}{g_j(z)L_j^*}, \quad (37)$$

where

$$g_j(z) \equiv \Theta + \frac{\eta + \gamma}{2\rho} \left\{ (L_j^*)^\beta (R_j^*)^\theta [R_j^* N S_j(z)]^{1-\theta} \right\}^2 \quad (38)$$

strictly decreases with z through S_j . This expression shows that the parameters η and γ of the final sector's production function affect the wage-bid rent ratio. In particular, when the input variety effect in the final sector is stronger (a lower η), workers are relatively better paid.

Observe that (37) can be rewritten as $g_j(z) = \beta r_j^F(z) / [w_j(z) L_j^*]$, so that $g_j(z)$ is proportional to the land rent-wage ratio at location z . Since $g_j(z)$ is the main driver of the equilibrium land rent and wage schedules, we find it useful to determine how it varies with its parameters. The expressions (30), (31) and (38) imply

$$g_j(z) = \Theta + \frac{\eta + \gamma}{2\rho} \left\{ \frac{\theta}{\beta} \left[\frac{\beta}{\theta + \beta} \left(\frac{H}{N} - \phi_j \right) \right]^{1+\beta} [N S_j(z)]^{1-\theta} \right\}^2.$$

As shown in Appendix A, the land rent-wage ratio decreases with the number of intermediate firms (N), the distance-decay effect (ε), the requirements for design (ϕ), and the startup cost (f) because Θ decreases with f , whereas it increases with the size of the high-tech labor pool (H) when the equilibrium configuration is agglomerated.

Differentiating (37) with respect to z and plugging the resulting expression into (21) yields a first-order ordinary differential equation in r_j^F with respect to z . Under $\alpha = 1/2$, this differential equation can be integrated explicitly to determine the intermediate firms' bid rent schedule (see (A.4) in Appendix A):

$$r_j^F(z) = \left\{ c_j^0(z_j^0) [S_j(z)]^{1-\theta} [g_j(z) L_j^* / \beta]^{\theta+\beta} \right\}^{\frac{1}{\theta+\beta+g_j(z)}}. \quad (39)$$

The constant of integration is given by

$$c_j^0(z_j^0) = \frac{[r_j^F(z_j^0)]^{\theta+\beta+g_j(z_j^0)}}{[S_j(z_j^0)]^{1-\theta} [g_j(z_j^0) L_j^* / \beta]^{\theta+\beta}},$$

where the initial condition $r_j^F(z_j^0)$ depends on the choice of the reference location z_j^0 , i.e., $z_A^0 = N/2$ and $z_D^0 = (N + H)/2$.

Plugging (39) into (37) yields the equilibrium wage schedule:

$$w_j^*(z) = \left\{ c_j^0(z_j^0) S_j(z)^{1-\theta} [g_j(z) L_j^* / \beta]^{-g_j(z)} \right\}^{\frac{1}{\theta+\beta+g_j(z)}}. \quad (40)$$

It is readily verified that $w_j(z)/r_j^F(z)$ reduces to (37). It then follows from (23) that

$$K_j^*(z) = \frac{\alpha}{\beta} L_j^* \frac{w_j^*(z)}{\rho}.$$

Hence, unlike its labor input, a firm's capital input varies with its location through the wage it pays to workers.

The strict concavity of the firms' bid rent $r_j^F(z)$ vastly simplifies the analysis of the spatial equilibrium (see Figure 1). We show in Appendix A that this function is decreasing and strictly concave in z when the following sufficient condition holds:

Condition R.

$$1 + \frac{\theta}{\beta} > \frac{r_j^F(0)}{w_j(0)L_j^*} \cdot \ln r_j^F(0).$$

It follows from (6) that a higher fixed cost F , which shifts the bid rent schedule $r_j^F(z)$ downward, makes Condition R more likely to hold. We assume that this condition holds throughout the remainder of the paper.

5 The spatial structure of R&D activities

In this section, we identify necessary and sufficient conditions under which the equilibrium outcome involves an agglomerated or a dispersed configuration.

5.1 The science park

In the case of an agglomerated configuration ($j = A$), all intermediate firms cluster within a science park spread over $[-N_A^*/2, N_A^*/2]$, whereas workers reside in the outskirts of the central park and commute to the workplace. We assume without loss of generality that the commuting function $J_A(y)$ is given by

$$z = J_A(y) = \frac{N_A^*}{H}(y - N_A^*/2), \quad y \in [N_A^*/2, (H + N_A^*)/2] \quad (41)$$

so that workers living at $y = N_A^*/2$ work at $z = 0$, while those at $y = (H + N_A^*)/2$ work at $z = N_A^*/2$. In other words, a worker living in the residential area $[N_A^*/2, (H + N_A^*)/2]$ is

assigned to a unique location belonging to $[0, N_A^*/2]$ with y and $J_A(y)$ varying in the same direction. To support this commuting pattern, (27) requires:

$$w_j^*[J_A(y)] = w_j^*(0) - ty, \quad y \in [0, (H + N_A^*)/2].$$

The reference location is given by $z_A^0 = N_A^*/2$ and the constant of integration by

$$c_A^0(N_A^*/2) = \frac{\{1 + t(H/2)\}^{\theta+\beta+g_A(N_A^*/2)}}{[S_A(N_A^*/2)]^{1-\theta} [g_A(N_A^*/2)L_A^*/\beta]^{\theta+\beta}}.$$

Moreover, we have $r_A^F(N_A^*/2) = r_A^W(N_A^*/2) = 1 + tH/2$ and

$$r_A^F(0) = \left\{ (1 + tH/2)^{\theta+\beta+g_A(N/2)} \left[\frac{g_A(0)}{g_A(N_A^*/2)} \right]^{\theta+\beta} \right\}^{\frac{1}{\theta+\beta+g_A(0)}}.$$

To ensure the existence of a science park, the following two conditions are necessary and sufficient:

- (i) firms' bid rent is steeper than workers' at $z = N_A^*/2$;
- (ii) firms outbid workers at $z = 0$.

When firms' bid rent schedule is decreasing and strictly concave in z , condition (i) is necessary and sufficient to guarantee that workers outbid firms outside the science park, while condition (ii) means that firms outbid workers within the park. It remains to check what conditions (i) and (ii) become for a science park to emerge as an equilibrium outcome.

First, equalizing the derivatives of firms' bid rent and workers' bid rent at $z = N/2$, we obtain the following equation in t :

$$\frac{(1 - \theta) N \left\{ 1 + 2 \left[\frac{\theta+\beta}{g_j(N/2)} - \ln(1 + tH/2) \right] [g_j(N/2) - \Theta] \right\}}{[\theta + \beta + g_j(N/2)] S_j(N/2)} = \frac{t}{1 + tH/2} \quad j = A, D. \quad (42)$$

Since the left hand side of this expression is decreasing in t whereas its left hand side is increasing and equal to 0 at $t = 0$, (42) has a unique solution in t , which is denoted T_j^1 . It is then readily verified that condition (i) is equivalent to $t < T_A^1$.

Let us now come to condition (ii). Equalizing firms' bid rent and workers' bid rent at $z = 0$ yields the expression:

$$\left[\frac{S_j(0)}{S_j(N/2)} \right]^{1-\theta} \left[\frac{g_j(0)}{g_j(N/2)} \right]^{\theta+\beta} = \frac{(1 + t\frac{H+N}{2})^{\theta+\beta+g_j(0)}}{(1 + tH/2)^{\theta+\beta+g_j(N/2)}}. \quad (43)$$

Since the left hand side of (43) is independent of t and larger than 1, while the right hand side is increasing and equal to 1 at $t = 0$, (43) has a unique solution in t ; it is denoted T_j^2 . Condition (ii) thus amounts to $t < T_A^2$. As a result, we have the following proposition.

Proposition 2 (Existence of a science park). *There exists a science park if and only if $t \leq \min \{T_A^1, T_A^2\}$.*

Figure 1 plots the land rent under an agglomerated configuration. Given the strict concavity of firms' bid rent and the linearity of workers' bid rent, the former may intersect the latter at most twice. When firms' bid rent is sufficiently steep and the slope of the workers' bid rent (i.e., t) is sufficiently flat, there is a unique intersection point. In this case, firms outbid workers in the inner area, whereas workers outbid firms in the outer areas. Hence, the equilibrium configuration features a science park.

Insert Figure 1 about here

When Θ is sufficiently small, it is readily verified that T_A^1 and T_A^2 are decreasing in $g_A(N_A^*/2)$. In this case, it is shown in Appendix B that both T_A^1 and T_A^2 increase with ε and f . Furthermore, the impact of H and ϕ_A on T_A^2 may be unambiguously determined (see Appendix B). Since numerical analysis undertaken for reasonable parametrization suggests that $T_A^2 < T_A^1$ (see Appendix D), we are able to derive additional comparative static results (see Appendix B).

To sum up, we have:

Proposition 3 (Characterization of a science park). *If Θ is sufficiently small, then a more localized spillover effect ($\varepsilon \uparrow$) or a higher startup cost ($f \uparrow$) makes a science park more likely to emerge. Furthermore, when $T_A^2 \leq T_A^1$ holds, a lower labor requirement for design ($\phi_A \downarrow$) increases the likelihood of a science park, while a bigger labor pool ($H \uparrow$) has a similar impact when H is large enough.*

The magnitude of the distance-decay effect on the clustering of high-tech firm is dampened when the requirement for designers is lower or when more high-tech workers are available. Thus, when ϕ_A rises, design productivity reduces, which lowers the advantage of knowledge spillovers and, therefore, decreases the incentives for intermediate firms to cluster. This also leads to a smaller number of researchers and lower volume of R&D, hence a smaller science park. In addition, a more localized spatial externality fosters the clustering of intermediate firms because firms benefit from increased spillovers by being located together. With a greater

mass of skilled labor, the positive scale effect implies stronger spillovers, thus raising firms' incentive to cluster.

We stress that more effective designers and an increased availability of high-tech workers, which make a science park more likely to emerge, are *entirely* channelized through employment of researchers and designers, as well as by the total size of the researcher pool in the science park. Moreover, these two effects are reinforced by the magnitude of the spillover effect, which takes on its highest values when firms cluster in a single science park. These results may serve to explain why the extent of the proximity effect may vary by location or by industry (see the survey by Carlino and Kerr, 2015, Section 4.3). Last, since a higher fixed cost requires larger operating profits to balance it, this can be achieved when firms cluster to take advantage of stronger spillovers.

One might expect a higher cost of capital (ρ) to have a negative impact on the occurrence of a science park because it reduces the marginal productivity of R&D. However, this argument disregards that a higher ρ also implies more expenditure on capital, thus reducing intermediates' profits. This in turn incentivizes intermediate firms to cluster in a science park. Consequently, the final effect is a priori undetermined. Nevertheless, simulations suggest that the latter effect overcomes the former one, so that a science park is more likely to emerge when ρ is higher, but it has a smaller size.

Inspecting the profit-maximizing conditions (18)-(20) shows that using complementary rather than substitutable inputs, i.e., shifting γ from positive to negative values, affects all the equilibrium values of output, inputs and prices. Therefore, predicting its impact is next to impossible. However, it follows from (38) that this downward shift in γ has the same impact as an increase in ρ . Our numerical analysis (see Appendix D) suggests that *a science park is more likely to pump up when intermediate goods are complements*.

5.2 The dispersion of R&D activities

A flat city involves the uniform dispersion of workers and intermediate firms, hence the uniform distribution of R&D activities. In this case, it must be that $r_D^F((H + N_D^*)/2) = 1$ while $J(y) = y$. Therefore, it is natural to select $z_D^0 = (H + N_D^*)/2$, which implies the following initial condition:

$$c_D^0((H + N_D^*)/2) = \frac{1}{[S_D((H + N_D^*)/2)]^{1-\theta} [g_D((H + N_D^*)/2) L_D^*/\beta]^{\theta+\beta}}.$$

To ensure the existence of a flat city, the following two conditions must be met:

- (i) firms and workers have identical bid rents;
- (ii) a worker's residence and workplace are the same.

These are equivalent to conditions that bid rents and wage schedules are (weakly) flatter than the commuting cost schedule across all locations.

Using the argument developed in section 5.2 shows that condition (i) is equivalent to $t > T_D^1$ where

$$T_D^1 = \frac{(1 - \theta)(H + N) \left\{ 1 + \frac{2(\theta + \beta)}{g_D((H + N)/2)} [g_D((H + N)/2) - \Theta] \right\}}{[\theta + \beta + g_D((H + N)/2)] S_D((H + N)/2)} > 0.$$

Moreover, equalizing the derivatives of firms' bid rent and workers' bid rent at $z = (H + N)/2$ yields the equation:

$$t = \frac{2(1 - \theta) z_j^0 w_j(z_j^0) \left\{ 1 - 2 \left[1 + \ln \left(1 + t \left(\frac{H + N}{2} - z_j^0 \right) \right) \right] \cdot [g_j(z_j^0) - \Theta] \right\}}{[\theta + \beta + g_j(z_j^0)] S_j(z_j^0)}, \quad (44)$$

which has a unique solution in t given by T_j^3 . Using (44) where $z_D^0 = (H + N)/2$, we obtain the threshold:

$$T_D^3 = -\frac{(1 - \theta)(N + H)[g_D((N + H)/2) - \Theta]}{[\theta + \beta + g_D((N + H)/2)] S_D((N + H)/2)} < 0,$$

which implies that condition (ii) never binds. Consequently, the following result holds.

Proposition 4 (Existence of a flat city). *A flat city arises if and only if $t \geq T_D^1$.*

We show in Appendix C that an increase in the distance-decay effect ($\varepsilon \uparrow$), a stronger labor requirement for design ($\phi_D \uparrow$), or a higher startup cost ($f \uparrow$), all raises T_D^1 when Θ is not too large. Thus, for a given value of commuting cost, any of these changes reduces the likelihood for a flat city. The size of the labor pool has the same impact when H is big enough. Hence, we have:

Proposition 5 (Characterization of a flat city). *If Θ and θ are sufficiently small, then a more localized spillover effect ($\varepsilon \uparrow$) or a higher startup cost ($f \uparrow$) or a lower labor requirement for design ($\phi_D \downarrow$) makes a flat city less likely to emerge. Furthermore, a bigger labor pool ($H \uparrow$) has a similar impact when H is large enough.*

Finally, it is readily verified that the right hand side of (42) is a decreasing function of g_j . Since $g_A > g_B$, we have $T_A^1 < T_D^1$. Therefore, the two configurations studied in this paper do

not coexist. Moreover, there is a range of commuting cost values such that the city has several smaller science parks separated by residential areas. Indeed, in modern high-tech industries, startup costs are typically high, while advanced or tacit knowledge depends crucially on face-to-face contacts. As a consequence, science parks are the most likely outcome. Nevertheless, commuting costs rise fast as a result of higher time costs. Eventually, the equilibrium outcome should change and involve the decentralization of the R&D activities. This fragmentation of science parks may serve to explain the evolution of the Silicon Valley, which began with Palo Alto Industrial Park in 1951, expanded to Mountain View, then to Sunnyvale, Santa Clara and, finally, San Jose (Saxenian 1994, pp. 29-30).

6 Concluding remarks

We have identified necessary and sufficient conditions for the emergence of a city endowed with a science park and characterized the flat city without science parks. The former occurs when knowledge spillover decay are severe and starting up is costly, which are typical features of new high-tech industries. These results suggest that science parks are more likely to form in advanced knowledge-based economies, allowing final firms to enjoy higher productivity gains.

Notwithstanding the social desirability of science parks, it is worth stressing that the most common instruments used by governments or universities to promote science parks is to reduce firms' startup costs (lower f) by subsidizing capital investments. Our analysis suggests that implementing such policies need not achieve their goals because they do not incite firms to move to large and productive science parks. By contrast, subsidizing land incentivizes firms to cluster in large science parks. Indeed, since $r_j(z) = \max \{r_j^F(z) + \Delta r, r_j^W(z)\}$, the subsidy Δr generates a discontinuity in firms' bid rents at the border between industrial and residential areas, thus enabling firms to outbid other land-users and to occupy more land within the inner area of the high-tech city.

A final remark is in order. Our model is isomorphic to a setting in which the intermediate sector is replaced by a final sector that produces a differentiated good sold to consumers endowed with linear-quadratic preferences (8), as in Ottaviano *et al.* (2002). Proposition 2 thus states a necessary and sufficient condition for the final producers to form a central high-tech district.

Appendix

A. The concavity of firms' bid rent schedule

(i) Manipulating (24) and (33) yields the following equations:

$$\begin{aligned}\frac{dr_j^F(z)}{dz} &= -\frac{L_j^*}{\beta} \left[2(1-\theta) \frac{w_j(z)z}{S_j(z)} + (\theta + \beta) \frac{dw_j(z)}{dz} \right] \\ \frac{dr_j^F(z)}{r_j(z)dz} &= -\frac{L_j^*w_j(z)}{\beta r_j(z)} \left[2(1-\theta) \frac{z}{S_j(z)} + (\theta + \beta) \frac{dw_j(z)}{w_j(z)dz} \right] \\ \frac{\beta r_j^F(z)}{w_j(z)L_j^*} &= \Theta + \frac{\eta + \gamma}{\rho} \left\{ (L_j^*)^\beta R_j^\theta [\bar{R}_j S_j(z)]^{1-\theta} \right\}^2 \equiv g_j(z).\end{aligned}$$

Substituting the third equation into the second one, we obtain:

$$g_j(z)d\ln(r_j^F(z)) + (\theta + \beta)d\ln(w_j(z)) = -\frac{2(1-\theta)z}{S_j(z)}dz, \quad (\text{A.1})$$

while the third equation becomes (37).

Since $dS_j(z) = -2zdz$, integrating (A.1) yields:

$$g_j(z)\ln(r_j^F(z)) + (\theta + \beta)\ln(w_j(z)) = \ln c_j^0 + (1-\theta)\ln(S_j(z)),$$

where c_j^0 is the constant of integration. Rewriting the above expression gives

$$r_j^F(z) = \left[\frac{c_j^0 S_j(z)^{1-\theta}}{w_j(z)^{\theta+\beta}} \right]^{\frac{1}{g_j(z)}}. \quad (\text{A.2})$$

Choosing a reference location z_j^0 and using (37), we can determine c_j^0 :

$$c_j^0(z_j^0) = \frac{[r_j^F(z_j^0)]^{\theta+\beta+g_j(z_j^0)}}{[S_j(z)]^{1-\theta} [g_j(z)L_j^*/\beta]^{\theta+\beta}},$$

which can be substituted into (A.2) to get the intermediate firms' bid rent (39). We can then use (37) to obtain the wage schedule (40).

(ii) Differentiating $g_j(z)$, it is readily verified that

$$\frac{dg_j(z)}{dz} = -\frac{4(1-\theta)z}{S_j(z)}[g_j(z) - \Theta] < 0.$$

Differentiating (39) with respect to z yields:

$$\frac{dr_j^F(z)}{dz} = -\frac{r_j^F(z)}{\theta + \beta + g_j(z)} \left\{ \frac{2(1-\theta)z}{S_j(z)} + \left[\frac{\theta + \beta}{g_j(z)} - \ln(r_j^F(z)) \right] \left[-\frac{dg_j(z)}{dz} \right] \right\}. \quad (\text{A.3})$$

Since $g_j(z)$ is decreasing, (A.3) is negative if

$$\max_z \{ \ln r_j^F(z) \} = \ln r_j^F(0) \leq (\theta + \beta) / g_j(0).$$

Using (37), this inequality is equivalent to condition **R**.

Further differentiating (A.3) and using the derivative of $g_j(z)$, we get:

$$\begin{aligned} \frac{d^2 r_j^F(z)}{dz^2} &= -\frac{1}{\theta + \beta + g_j(z)} \frac{dr_j^F(z)}{dz} \frac{dg_j(z)}{dz} - \frac{r_j^F(z)}{\theta + \beta + g_j(z)} \\ &\quad \left\{ 2(1 - \theta) \left(\frac{1}{S_j(z)} + \frac{2z^2}{S_j(z)^2} \right) + \left[\frac{\theta + \beta}{g_j(z)} - \ln r_j^F(z) \right] \left(-\frac{dg_j(z)}{dz} \right) \right. \\ &\quad \left. + \left[\frac{\theta + \beta}{g_j(z)^2} \left(-\frac{dg_j(z)}{dz} \right) + \frac{1}{r_j^F(z)} \left(-\frac{dr_j^F(z)}{dz} \right) \right] \left(-\frac{dg_j(z)}{dz} \right) \right\}, \end{aligned}$$

which is negative under condition **R**.

(iii) It remains to characterize the rent-wage ratio schedule $g_j(z)$. For ϕ, ε, f , it is trivial that

$$\frac{dg_j(z)}{d\phi_j} < 0 \quad \frac{dg_j(z)}{d\varepsilon} = \frac{dg_j(z)}{dS_j(z)} \cdot \frac{dS_j(z)}{d\varepsilon} < 0 \quad \frac{dg_j(z)}{df} < 0.$$

Moreover, we have

$$\begin{aligned} \frac{dg_j(z)}{dN} &\propto \frac{d}{dN} \left(\frac{H}{N} - \phi_j \right)^{1+\beta} [NS_j(z)]^{1-\theta} \\ &\propto - \left[(\theta + \beta) \frac{H}{N} + (1 - \theta) \phi_j \right] < 0. \end{aligned}$$

Furthermore, for $j = A$ and $z_A^0 = N/2$, it follows from $S_A(z)$ that $dS_A(0)/dH = 0$, so that

$$\frac{dg_A(0)}{dH} > 0 \quad \frac{dg_A(b)}{dH} > 0.$$

When $j = D$, we have $z_D^0 = (H + N)/2$. It then is straightforward to show that

$$\begin{aligned} \frac{dg_D}{dH} &\propto \frac{d}{dH} \left[\left(\frac{H}{N} - \phi_D \right)^{1+\beta} S_D^{1-\theta} \right] \\ &= \left(\frac{H}{N} - \phi_D \right)^\beta S_D^{-\theta} \left[(1 + \beta) \frac{1}{N} S_D^2 - (1 - \theta) (1 + \varepsilon) \left(\frac{H}{N} - \phi_D \right) \frac{H + N}{2} \right], \end{aligned}$$

which is negative when H is sufficiently high. Q.E.D.

B. Proof of Proposition 3

(i) Let us first study how T_A^1 varies with the main parameters. Differentiating the LHS of (42) with respect to g_A leads to, aside from a positive multiplier,

$$-\frac{\ln(1+tH/2)}{\theta + \beta + g_A(N_A^*/2)} - \frac{(\theta + \beta)[g_A(N_A^*/2) - \Theta]}{g_j(N_A^*/2)} + \frac{\theta}{[\theta + \beta + g_A(N_A^*/2)]g_A(N_A^*/2)} \quad (\text{B.1})$$

which is negative when θ is small enough. The effects via g_A derived in Appendix A together with the direct effects in (B.1) yield the desired comparative static results about T_A^1 .

(ii) We now turn to the impact of parameter changes on T_A^2 .

(a) Consider first the LHS of (43). Note that S_A is decreasing in ε while

$$\frac{S_A(0)}{S_A(N/2)} = \frac{S_{\max} - \varepsilon \left(\frac{N}{2}\right)^2}{S_{\max} - (N/2)^2 - \varepsilon \left(\frac{N}{2}\right)^2} = \frac{1}{1 - \frac{(N/2)^2}{S_{\max}/(N/2)^2 - \varepsilon}} > 1$$

is increasing in ε and N .

Recall from Appendix A that $g_A(z)$ is decreasing in ϕ_A, ε, f , and N , but increasing in H , which allows us to characterize the ratio:

$$\frac{g_A(0)}{g_A(N/2)} = \frac{\Theta + \frac{\eta+\gamma}{2\rho} \left\{ \frac{\theta}{\beta} \left[\frac{\beta}{\theta+\beta} \left(\frac{H}{N} - \phi_A \right) \right]^{1+\beta} N \right\}^2 \left[S_{\max} - \varepsilon \left(\frac{N}{2} \right)^2 \right]^{2(1-\theta)}}{\Theta + \frac{\eta+\gamma}{2\rho} \left\{ \frac{\theta}{\beta} \left[\frac{\beta}{\theta+\beta} \left(\frac{H}{N} - \phi_A \right) \right]^{1+\beta} N \right\}^2 \left[S_{\max} - (1+\varepsilon) \left(\frac{N}{2} \right)^2 \right]^{2(1-\theta)}}.$$

Differentiating this expression with respect to N leads to

$$\begin{aligned} \frac{d}{dN} \frac{g_A(0)}{g_A(N/2)} &\propto \frac{g_A(0) - \Theta}{g_A(0)} \left\{ \frac{-2(1+\beta)H}{N^2(H/N - \phi_A)} + \frac{2(1-\theta)}{N} - 2(1-\theta)\varepsilon N \left(S_{\max} - \varepsilon \frac{N^2}{4} \right)^{-1} \right\} - \\ &\frac{2[g_A(N/2) - \Theta]}{g_A(N/2)} \left\{ \frac{-(1+\beta)H}{N^2(H/N - \phi_A)} + \frac{1-\theta}{N} - (1-\theta)(1+\varepsilon)N \left[S_{\max} - (1+\varepsilon) \frac{N^2}{4} \right]^{-1} \right\} \\ &\propto \frac{2\Theta(1+\beta)H}{N(H/N - \phi_A)} \left[\frac{1}{g_A(0)} - \frac{1}{g_A(N/2)} \right] + \\ &\frac{2(1-\theta)}{N} \left\{ \left[1 - \frac{\varepsilon N^2}{S_{\max} - \varepsilon (N/2)^2} \right] \left[1 - \frac{\Theta}{g_A(0)} \right] - \left[1 - \frac{(1+\varepsilon)N^2}{S_{\max} - (1+\varepsilon)(N/2)^2} \right] \left[1 - \frac{\Theta}{g_A(N/2)} \right] \right\}, \end{aligned}$$

which is negative when Θ is sufficiently small.

By inspection, we have

$$\frac{d}{df} \frac{g_A(0)}{g_A(N/2)} \propto - \left\{ [S_{\max} - (1+\varepsilon)(N/2)^2]^{2(1-\theta)} - [S_{\max} - \varepsilon(N/2)^2]^{2(1-\theta)} \right\} > 0.$$

Similarly,

$$\frac{d}{dH} \frac{g_A(0)}{g_A(N/2)} > 0 \quad \frac{d}{df} \frac{g_A(0)}{g_A(N/2)} > 0 \quad \frac{d}{d\phi_A} \frac{g_A(0)}{g_A(N/2)} < 0.$$

The effect of ε is a bit more involved. Set

$$\Delta(N) \equiv \frac{\theta}{\beta} (L_A^*)^{1+\beta} N^{1-\theta}.$$

Then,

$$\frac{d}{d\varepsilon} \frac{g_A(0)}{g_A(N/2)} \propto \frac{\eta + \gamma}{2\rho} [\Delta(N)]^2 [S_A(0)S_A(N/2)]^{1-2\theta} \frac{N^2}{4} - \Theta [S_A(0)^{1-2\theta} - S_A(N/2)^{1-2\theta}],$$

which is positive when Θ sufficiently small.

Thus, given the city boundaries, an increase in H or f , or a decrease in ϕ , leads to a higher ratio $g_A(0)/g_A(N/2)$. The effect of ε is similar to f if Θ is not too large.

(b) Consider now the RHS of (43). Set

$$\Psi \equiv \frac{[1 + t(H + N)/2]^{\theta + \beta + g_A(0)}}{(1 + tH/2)^{\theta + \beta + g_A(N/2)}}$$

For $v = f, \phi_A, \varepsilon$ we have

$$\frac{d\Psi}{dv} \propto \frac{dg_A(0)}{dv} \cdot \ln \left(1 + t \frac{H + N}{2} \right) - \frac{dg_A(N/2)}{dv} \cdot \ln \left(1 + t \frac{H}{2} \right)$$

where

$$\begin{aligned} g_A(0) &= \Theta + \frac{\eta + \gamma}{2\rho} [\Delta(N)]^2 [S_{\max} - \varepsilon(N/2)^2]^{2(1-\theta)} \\ g_A(N/2) &= \Theta + \frac{\eta + \gamma}{2\rho} [\Delta(N)]^2 [S_{\max} - (1 + \varepsilon)(N/2)^2]^{2(1-\theta)}. \end{aligned}$$

Clearly,

$$\frac{d\Psi}{df} \propto -\ln [1 + t(H + N)/2] + \ln (1 + tH/2) < 0$$

$$\frac{d\Psi}{d\phi_A} \propto -(S_{\max} - \varepsilon N^2/4)^{2(1-\theta)} \ln [1 + t(H + N)/2] + [S_{\max} - (1 + \varepsilon) N^2/4]^{2(1-\theta)} \ln(1 + tH/2) < 0.$$

The effect of ε is similar to f when Θ is not too large.

As for the effect of H , we have

$$\begin{aligned}
& \frac{d\Psi}{dH} \\
&= \ln\left(1+t\frac{H+N}{2}\right) \frac{d}{dH}g_A(0) - \ln\left(1+t\frac{H}{2}\right) \frac{d}{dH}g_A(N/2) + \frac{[\theta+\beta+g_A(0)]t/2}{1+t(H+N)/2} - \frac{[\theta+\beta+g_A(N/2)]t/2}{1+tH/2} \\
&> \ln\left(1+t\frac{H+N}{2}\right) \frac{d}{dH}g_A(0) - \ln\left(1+t\frac{H}{2}\right) \frac{d}{dH}g_A(N/2) + [\theta+\beta+g_A(0)] \left[\frac{t/2}{1+t(H+N)/2} - \frac{t/2}{1+tH/2} \right] \\
&= \frac{d}{dH}g_A(0) \ln\left[\frac{1+t(H+N)/2}{1+tH/2} \right] + [\theta+\beta+g_A(0)] \cdot \left[\frac{t/2}{1+t(H+N)/2} - \frac{t/2}{1+tH/2} \right]
\end{aligned}$$

which is positive if H is sufficiently large. Finally, the impact of N is ambiguous.

(iii) Combining the analyses in (i) and (ii) above, we can conclude that an increase in ε or f , or a decrease in ϕ_A leads to a higher T_A^2 when Θ is not too large. Furthermore, the impact of H on T_A^2 is positive when H is high enough. This yields the desired comparative static results. Q.E.D.

C. Proof of Proposition 5

Since T_A^1 and T_D^1 differ only by the reference location $z_A^0 = N/2$ and $z_D^0 = (H+N)/2$, all the comparative static derived in Appendix B holds true but for H . Differentiating T_D^1 with respect to H yields

$$\frac{d}{dH}T_D^1 = \frac{\partial T_D^1}{\partial H} + \frac{\partial T_D^1}{\partial S_D} \frac{\partial S_D}{\partial H} + \frac{\partial T_D^1}{\partial g_D} \frac{dg_D}{dH},$$

where

$$\frac{\partial T_D^1}{\partial S_D} = -\frac{T_D^1}{S_D} < 0$$

and

$$\frac{\partial T_D^1}{\partial g_D} = -\frac{(1-\theta)(H+N)[1+2(\theta+\beta)] - \frac{2(\theta+\beta)\Theta}{g_D((H+N)/2)} \left[1 + \frac{\theta+\beta+g_D((H+N)/2)}{g_D((H+N)/2)}\right]}{S_D [\theta+\beta+g_D((H+N)/2)]^2},$$

which is negative when Θ is small enough. Moreover, it is trivial that

$$\frac{\partial T_D^1}{\partial H} = \frac{T_D^1}{H+N} > 0.$$

Since $S_D(\frac{H+N}{2}) = S_{\max} - (1+\varepsilon)\left(\frac{H+N}{2}\right)^2$, we have

$$\frac{\partial S_D}{\partial H} = -(1+\varepsilon)(H+N) < 0.$$

Using Appendix A shows that $dT_D^1/dH > 0$ when Θ is sufficiently small and H sufficiently high. This yields the desired comparative static result. Q.E.D.

D. Numerical analysis

We begin by describing the parametrization of our model. Using Acemoglu and Guerrieri (2008) who found that capital intensity of a high-tech industry such as ICT is about 0.53 in the U.S. over 1948-2005, we set in the benchmark $\alpha = 0.5$. Since land share is generally set as 0.06 (Caselli and Coleman, 2001), we obtain $\beta = 1 - 0.5 - 0.06 = 0.44$. Also standard is to set the capital cost to be $\rho = 0.1$ (Hsieh and Klenow, 2009) and the R&D intensity of high-tech industry to be $\theta = 0.03$, which is higher than the overall R&D share in the US (0.026).

By normalizing the final good scaling parameter $\delta = 10$, we choose $S_{\max} = 20$ and $\eta = 1$ to regulate proper intermediate good demand slope so that the choke price is sufficiently high to avoid degenerate equilibria. We then set $\gamma = 0.5$ to capture mild substitution between intermediate good varieties. We normalize $H = 2$, so the mass of skill workers over the right half of the city is 1. We also choose $\varepsilon = 1$, which yields a comfortable range for positive knowledge spillovers. In this case, Condition **R** holds. We set $f = 0.001$, hence $f/\rho = 0.01$, and the design requirement parameter $\phi_A = 0.5$, under which $\Theta > 0$ and all firms' profits are positive. For convenience, we choose $\phi_D = 1.2 \cdot \phi_A$.

We now summarize the key results based on the numerical benchmark model. First of all, the mass of intermediate firms under each configuration is $N_A^* = 2.42$ and $N_D^* = 2.22$, thus $N_A^* > N_D^*$. Second, for $t \leq 0.053 = T_A^2$, the equilibrium involves a science park; for $t \geq 0.49 = T_D^1$, the city is flat. Third, the thresholds satisfy: $T_A^2 < T_A^1$ and $T_A^2 < T_D^1$. Fourth, the comparative static results stated in Propositions 3 and 5 all hold true. Finally, when $\gamma = -0.5$ (intermediate goods are complements), T_A^2 becomes bigger and hence a science park is more likely to emerge in equilibrium.

We have perturbed the following parameters $\{\alpha, \theta, \delta, \eta, \gamma, S_{\max}, \varepsilon, f, \phi_D/\phi_A\}$ one by one up and down by 20% around their benchmark values (with necessary adjustments to ensure $\Theta > 0$ and that Condition **R** holds). Our main findings summarized in the previous paragraph are robust to such changes.

References

- [1] Acemoglu, D. and V. Guerrieri (2008) Capital deepening and nonbalanced economic growth. *Journal of Political Economy* 116: 467-98.
- [2] Aghion, P. and X. Jaravel (2015) Knowledge spillovers, innovation and growth. *Economic Journal* 125: 533-73.
- [3] Arzaghi, M. and J.V. Henderson (2008) Networking off Madison Avenue. *Review of Economic Studies* 75: 1011-38.
- [4] Audretsch, D. and M. Feldman (2004) Knowledge spillovers and the geography of innovation. In: J.V. Henderson and J.-F. Thisse (eds.) *Handbook of Urban and Regional Economics, Volume 4*. North-Holland, Amsterdam, 2713-39.
- [5] Becker, G.S and K.M. Murphy (1992) The division of labor, coordination costs, and knowledge. *Quarterly Journal of Economics* 107: 1137-60.
- [6] Berliant, M., S.-K. Peng and P. Wang (2002) Production externalities and urban configuration. *Journal of Economic Theory* 104: 275-303.
- [7] Buzard, K., G.A. Carlino, R.M. Hunt, J.K. Carr, and T.E. Smith (2017) The agglomeration of American R&D labs. *Journal of Urban Economics* 101: 14-26.
- [8] Carlino, G.A. and W.R. Kerr (2015) Agglomeration and innovation. In: G. Duranton, J.V. Henderson and W. Strange (eds.) *Handbook of Regional and Urban Economics, Volume 5*. Amsterdam, Elsevier, 349-404.
- [9] Caselli, F. and W.J. Coleman II (2001) The U.S. structural transformation and regional convergence: A reinterpretation. *Journal of Political Economy* 109: 584-616.
- [10] Cassi, L. and A. Plunket (2015) Research collaboration in co-inventor networks: Combining closure, bridging and proximity. *Regional Studies* 49: 936-54.
- [11] Castells, M. and P.G. Hall (1994) *Technopoles of the World: The Making of Twenty-first-century Industrial Complexes*. London, Routledge.
- [12] Chen, T.-J. (2008) The emergence of Hsinchu Science Park as an IT cluster. In: S. Yusuf, K. Nabeshima and S. Yamashita (eds.) *Growing Industrial Clusters in Asia: Serendipity and Science*. Washington, DC, The World Bank, 67-89.
- [13] Chyi, Y. L., Y.M. Lai and W.H. Liu (2012) Knowledge spillovers and firm performance in the high-technology industrial cluster. *Research Policy* 41: 556-564.

- [14] Combes, P.-P. and L. Gobillon (2015) The empirics of agglomeration economies. In: G. Duranton, J.V. Henderson and W. Strange (eds.) *Handbook of Regional and Urban Economics. Volume 5*. Amsterdam, Elsevier, 247-348.
- [15] Delgado, M., M.E. Porter and S. Stern (2014) Clusters, convergence, and economic performance. *Research Policy* 43: 1785-99.
- [16] Duranton, G. and D. Puga (2004) Micro-foundations of urban increasing returns: Theory. In: J.V. Henderson and J.-F. Thisse (eds.) *Handbook of Urban and Regional Economics. Volume 4*. Amsterdam, North-Holland, 2063-117.
- [17] Duranton, G., Ph. Martin, T. Mayer, and F. Mayneris (2010) *The Economics of Clusters*. Oxford, Oxford University Press.
- [18] Fujita, M. (1989) *Urban Economic Theory*. Cambridge, Cambridge University Press.
- [19] Fujita, M. and F. Ogawa (1982) Multiple equilibria and structural transition of non-monocentric urban configurations. *Regional Science and Urban Economics* 12: 161-96.
- [20] Greenstone, M., R. Hornbeck and E. Moretti (2010) Identifying agglomeration spillovers: Evidence from winners and losers of large plant openings. *Journal of Political Economics* 118: 536-98.
- [21] Helmers, C. (2019) Choose the neighbor before the house: Agglomeration externalities in a UK science park. *Journal of Economic Geography* 19: 31-55.
- [22] Hsieh, C.-T. and P.J. Klenow (2009) Misallocation and manufacturing TFP in China and India. *Quarterly Journal of Economics* 124: 1403-48.
- [23] Katz, B. and J. Bradley (2013) Katz, B. and J. Bradley (2013) *The Metropolitan Revolution. How Cities and Metros Are Fixing Our Broken Politics and Fragile Economy*. Washington, DC, Brookings.
- [24] Link, A.N. and J.T. Scott (2003) U.S. science parks: The diffusion of an innovation and its effects on the academic missions of universities. *International Journal of Industrial Organization* 21: 1323-56.
- [25] Link, A.N. and J.T. Scott (2007) The economics of university research parks. *Oxford Review of Economic Policy* 23: 661-74.
- [26] Lucas, R.E. Jr. (1988) On the mechanics of economic development. *Journal of Monetary Economics* 22: 3-22.

- [27] Lucas, R.E. Jr. and E. Rossi-Hansberg (2002) On the internal structure of cities. *Econometrica* 70: 1445-76.
- [28] Marshall, A. (1890) *Principles of Economics*. London, Macmillan. 8th edition published in 1920.
- [29] Ogawa, M. and M. Fujita (1980) Equilibrium land use patterns in a nonmonocentric city. *Journal of Regional Science* 20: 455-75.
- [30] O'Hara, D.J. (1977). Location of firms within a square central business district. *Journal of Political Economy* 85: 1189-207.
- [31] Ottaviano G.I.P., T. Tabuchi, T. and J.-F. Thisse (2002) Agglomeration and trade revisited. *International Economic Review* 43: 409-36.
- [32] Peng, S.-K., J.-F. Thisse and P. Wang (2006) Economic integration and agglomeration in a middle product economy. *Journal of Economic Theory* 131: 1-25.
- [33] Romer, P. (1986) Increasing returns and long-run growth. *Journal of Political Economy* 94: 1002-37.
- [34] Romer, P. (1990) Endogenous technological change. *Journal of Political Economy* 98: 71-102.
- [35] Rosenthal, S. and W. Strange (2004) Evidence on the nature and sources of agglomeration economies. In: J.V. Henderson and J.-F. Thisse (eds.) *Handbook of Urban and Regional Economics. Volume 4*. Amsterdam, North-Holland, 2119-71.
- [36] Saxenian, A. (1994) *Regional Advantage: Culture and Competition in Silicon Valley and Route 128*. Cambridge, MA, Harvard University Press.
- [37] Siegel, D.S., P. Westhead and M. Wright (2003) Assessing the impact of university science parks on research productivity: Exploratory firm-level evidence from the United Kingdom. *International Journal of Industrial Organization* 21: 1357-69.

Figure 1. Bid Rent Schedules with a Science Park

